# **Coherent X-rays & applications**



# The European Synchrotron

#### Vincent Favre-Nicolin Algorithms & scientific Data Analysis

on leave from Univ. Grenoble Alpes



#### **COHERENT X-RAYS**?



Friedrich, Knipping, Laue



Illustrations from Authier « Early days of crystallography, Oxford University Press



#### **COHERENT X-RAYS ?**



Illustrations from Authier « Early days of crystallography, Oxford University Press

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#### **COHERENT X-RAYS**?

X-rays can produce (Bragg) diffraction even from "low-quality" X-ray sources :

- Large source size
- Non-monochromatic (but discrete spectrum)

#### **Diffraction implies interferences => coherence**



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#### WAVE PROPAGATION BASICS



$$A_0 \cos(\omega t - kz) = A_0 \cos\left(\omega t - \frac{2\pi z}{\lambda}\right) = A_0 \cos(\varphi)$$

• 
$$\lambda$$
: wavelength (0.01 to 1 nm for X-rays)

- $\omega$ : pulsation =  $2\pi/v$
- v: frequency
- φ: phase



Definition (from Malcolm Howells):

 "Optical coherence exists in a given radiating region if the phase differences between all pairs of points in that region have definite values which are constant with time"

#### Two types of coherence must be considered:

- Transverse coherence, between points in plane perpendicular to the wavevector
- Longitudinal (temporal) coherence between points along the wavevector

# 



# LONGITUDINAL COHERENCE

- Longitudinal (temporal) coherence
- Related to the monochromaticity
- For a beam with  $\delta\lambda$  spectrum width (typical  $\delta\lambda\lambda$ =10<sup>-4</sup>: for Si 111 monochromator)

$$A_{0}\cos\left(\omega t - \frac{2\pi z}{\lambda}\right) = A_{0}\cos(\varphi)$$

$$\lambda = 0$$

$$\lambda =$$

#### LONGITUDINAL COHERENCE & SCATTERING

Towards detector Towards detector λ-δλ

There is a phase difference between the beginning and the end of the particle.

As long as this difference is small, it does not affect the scattering signal For crystallography, the coherence length is much larger than a unit cell (~1nm), which is why we can always see Bragg diffraction with 'low' coherence



# **TRANSVERSE COHERENCE**

- Transverse coherence, between points in plane perpendicular to the wavevector
- Related to the source size
- X-ray sources (tubes, bending magnet, undulators, XFEL) are incoherent (different points within the source emit with random phase shifts)
- For a source width d (a few 10's of µm), seen from a distance D (50-120m):



Page 10 Coherent X-rays and Applications I ESRF-ILL Summer school 2021 I Vincent Favre-Nicolin

# **TRANSVERSE COHERENCE: YOUNG SLITS**

• Transverse coherence can be evaluated by fringe visibility:



Optics Communications 195, 79 (2001)



#### **COHERENT SCATTERING: 1 PARTICLE**



The scattering from a **coherently illuminated** particle can be simply computed using a Fourier transform



#### **COHERENT SCATTERING: 5 PARTICLES**



If the particles were *not* coherently illuminated, the detector image would be exactly the same as for a single particle.

#### + 'speckles' due to interferences between the scattering of all particles



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#### **COHERENT SCATTERING: 100 PARTICLES**



Features which can be extracted:

- Average particle size from oscillations
- Average distance between particles from speckles
- Time evolution

between the scattering of all particles

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# COHERENT ILLUMINATION



A coherent diffraction experiment is only achieved if :

- The sample is smaller than the coherent length
- Or the beam is collimated to a smaller size than the coherent length

In 3D, the term 'coherent volume' can be used



# **COHERENT X-RAYS: DYNAMICS & IMAGING**



- Study the frame-by frame evolution of the diffraction pattern (image crosscorrelation)
- Information about the evolution of relative position between particles
- Study **diffusion coefficients**, from atomistic to mesoscopic to length scales (colloids, glasses, magnetic systems, etc...)

The diffraction pattern is the sum of the interference of the scattering from all particles

$$A(\vec{s}) = \sum \rho_i e^{2i\pi \vec{s}.\vec{r}_i}$$

# **High-resolution imaging**

- The diffraction image obtained by Fourier Transform(s) of the illuminated object
- Once the phase has been recovered (algorithms), the object can be reconstructed (in 2D or 3D)
- The resolution is inversely proportional to the angular extent of the scattering (far field)

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### **COHERENT ILLUMINATION**

If the object is too complex (too many parameters vs available information), then the experiment will only at best yield a 'speckle pattern'



From Oleg Shpyrko web page

Statistical information :

- Width of speckle pattern ↔ average particle size
- Number of speckles peaks along one
  - dimension ↔ number of particles

Time-resolved experiments : XPCS





C. Gutt

#### XPCS:

• Measure the correlation of the scattered intensity as a function of time

Not a spectroscopy technique





- Movement of particles (molecules, atoms..) induce changes in the speckles
- Higher angular momentum (far from the centre) are more sensitive to smaller displacements
- Movement (diffusion) can be quantified by correlation

Page 19 Coherent X-rays and Applications I ESRF-ILL Summer school 2021 I Vincent Favre-Nicolin



Temporal intensity auto-correlation function:

$$g^{(2)}(\boldsymbol{Q},t) = \frac{\langle I(\boldsymbol{Q},\tau)I(\boldsymbol{Q},\tau+t)\rangle}{\langle I(\boldsymbol{Q},\tau)\rangle^2}$$

*Example 1*: Dynamics of silica colloidal nano-particles in super-cooled propanediol

- Tf = 245K for propanediol
- T<Tf => supercooled liquid, towards a glass transition



PRL 100, 055702 (2008)



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#### *Example 2*: atomic-scale dynamics & in a metallic glass (Mg<sub>65</sub>Cu<sub>25</sub>Y<sub>10</sub>)



Phys. Rev. Lett. 109, 165701 (2012)

- Glasses are seen as 'frozen liquids'
- ... they are *still* liquids, but with a *very* large viscosity
- Tg = 405K
- There is still atomic motion below Tg
- The ß value changes between above and below Tg – different motion regimes

$$g^{(2)}(\boldsymbol{Q},t) = 1 + Ae^{-2\left(\frac{t}{\tau}\right)^{\beta}}$$





XPCS also applies to protein solutions

Phys. Chem. Chem. Phys. 22, 19443 (2020)



Dynamics can be probed on a wide range of time-scales, which increases with modern synchrotron sources and XFEL

Pawel Kwasniewski PhD (Grenoble)



## **COHERENT X-RAYS: DYNAMICS & IMAGING**



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Page 23 Coherent X-rays and Applications I ESRF-ILL Summer school 2021 I Vincent Favre-Nicolin

#### **COHERENT VS INCOHERENT IMAGING**





#### **COHERENT X-RAY IMAGING TECHNIQUES**

#### **Propagation distance**





#### **COHERENT X-RAY IMAGING: ALGORITHMS ?**

#### **Propagation distance**



Object



#### The Phase problem

- Only the intensity is measured
- Complex algorithms required to reconstruct the object
- Iterative processes are used to yield the highest resolution

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#### **AMPLITUDE & PHASE**



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Lovelace Phase + Fourier Amplitude



#### THE PHASE PROBLEM

To compute the inverse Fourier Transform, both the phase and the amplitude are needed  $\rightarrow$  Phase Retrieval algorithms are required



# Algorithms: Hybrid Input/Output (HIO) Error Reduction Charge Flipping

NB : the 'Fourier recycling' algorithms are essentially the same as those used to obtain electronic density from anomalous (or isomorphous) diffraction data for macromolecular crystallography.

Page 28 Coherent X-rays and Applications I ESRF-ILL Summer school 2021 I Vincent Favre-Nicolin

#### **IMAGING: FIELD-OF VIEW VS RESOLUTION**





Page 30 Coherent X-rays and Applications I ESRF-ILL Summer school 2021 I Vincent Favre-Nicolin



# Projection





Only absorption, faint contrast





# Projection



50 µm

#### Better contrast



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# Projection



50 µm

#### Stronger contrast





Projection



Most contrast from phase <u>50 μm</u>



Page 34 Coherent X-rays and Applications I ESRF-ILL Summer school 2021 I Vincent Favre-Nicolin

#### PHASE CONTRAST IMAGING: HOLOTOMOGRAPHY

#### **PS FOAM**





D = 0.51 m

D = 0.21 m

Page 35

# Phase retrieval $\Delta \phi = 2\pi \delta t/\lambda$

t: thickness

#### N projections

tomographic reconstruction



Reconstruction of  $\boldsymbol{\delta} \ (r)$ 



Cloetens et al, Applied Physics Letters 75, 2912 (1999)

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#### **IMAGING: FIELD-OF VIEW VS RESOLUTION**



# **COHERENT DIFFRACTION IMAGING**




# WHY COHERENT DIFFRACTION IMAGING

Why use a method :

- Which is complex (experimentally : coherence)
- Where more than half the information (phase) is lost
- Where algorithms are not always robust

When there are simpler methods :

- Absorption imaging
- Phase contrast imaging
- Scanning microscopy

# RESOLUTION

For scanning microscopy :

• Resolution = beam size

For phase contrast/absorption imaging :

- Resolution = pixel size
- With focusing optics (projection microscopy), down to a few 10's of nm



# WHY COHERENT DIFFRACTION IMAGING

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When there are simpler methods :

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# For CDI

The smaller the object, the wider its Fourier Transform !

 $\rightarrow$  The resolution is inversely proportionnal to the extent of the measured scattering in reciprocal space

 $\rightarrow$  lower current limit : 5-10 nm for CDI at 8-15 keV

The resolution is smaller than the beam size  $\rightarrow$  " super-resolution "  $\rightarrow$  High resolution studies and/or nano-objects

Page 40 Coherent X-rays and Applications I ESRF-ILL Summer school 2021 I Vincent Favre-Nicolin



# **MORPHOLOGY OF COCCOLITHS USING CDI**

#### T. Beuvier<sup>a,b</sup>, I. Probert<sup>c</sup>, L. Beaufort<sup>d</sup>, B. Suchéras-Marx<sup>d</sup>, <u>Y. Chushkin<sup>b</sup></u>, F. Zontone<sup>b</sup> and A. Gibaud<sup>a</sup>

- <sup>a</sup> LUNAM, IMMM, UMR 6283 CNRS, Faculté des Sciences 72085 Le MANS Cedex 09, France,
- <sup>b</sup> EuropeanSynchrotron Radiation Facility, 71, avenue des Martyrs, 38000 Grenoble, France,
- <sup>c</sup> CNRS, Sorbonne Uni-versité Pierre et Marie Curie (UPMC) Paris 06, FR2424, Roscoff Culture Collection, Station Biologiquede Roscoff, Place Georges Teissier, 29680 Roscoff, France,
- <sup>d</sup> Aix Marseille Univ, CNRS, IRD, CollFrance, CEREGE, Aix-en-Provence, France.



Emiliania Huxleyi bloom south of cornwall (UK)

single-celled phytoplankton covered with calcite disks (coccoliths)

Landsat image from 24th July 1999, courtesy of Steve Groom, Plymouth Marine Laboratories.



Page 41 Coherent X-rays and Applications I ESRF-ILL Summer school 2021 I Vincent Favre-Nicolin

# **MARINE ALGAE - COCCOLITHOPHORES**

#### Emiliania huxleyi



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# **COCCOLITHOPHORE CARBON CHEMISTRY**



Transfer of CO<sub>2</sub> from atmosphere to limestone

Last 200 years absorbed 50% of  $CO_2$  emitted by human activities (>500 Gt  $CO_2$ )

Pre-industrial atmospheric CO<sub>2</sub> 280 ppm

Today atmospheric CO<sub>2</sub> 380 ppm

pH decreased of 0.1 units since pre-industrial times pH of sea water today 8.2±0.3

Calculating mass fluxes is major endeavour



D. A. Hutchins Nature **476**, 41, (2011)

Page 43 Coherent X-rays and Applications I ESRF-ILL Summer school 2021 I Vincent Favre-Nicolin

# **COCCOLITHS MASS DETERMINATION – OPTICAL METHOD**



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Slide: Y. Chushkin

#### **CXDI – ID10 BEAMLINE**

Isolated sample <7 µm is illuminated with coherent plane wave Voxel size < 32nm

**Detector** *p*,*N* 





# **3D-CXDI**





Page 46 Coherent X-rays and Applications I ESRF-ILL Summer school 2021 I Vincent Favre-Nicolin

Slide: Y. Chushkin

# **3D-CXDI**







# RESOLUTION



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Slide: Y. Chushkin



#### E. Huxleyi RCC1216





Page 49 Coherent X-rays and Applications I ESRF-ILL Summer school 2021 I Vincent Favre-Nicolin

#### E. Huxleyi RCC1216





Page 50 Coherent X-rays and Applications I ESRF-ILL Summer school 2021 I Vincent Favre-Nicolin

# COCCOLITHS



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# **COCCOLITHS - MASS**





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Slide: Y. Chushkin

## **COCCOLITHS DEFORMATION**

#### R. parvula





# CDI: CHROMOSOME





Y. Nishino et al, Physical Review Letters 102, (2009).

#### **CDI: CHROMOSOME**



Reconstructed 3D structure :

- 2D resolution : 38 nm
- 3D resolution : 120 nm
- Dose : 2x10^10 Gy

Y. Nishino et al, Physical Review Letters 102, (2009).

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# **PTYCHOGRAPHY**

#### Limitations of CDI :

- No imaging of extended objects (limited to the coherent volume of the beam)
- Need oversampled diffraction data
- Convergence of the algorithm can be difficult (support evaluation)
- The probe (amplitude and phase of the incoming beam) is unknown
- Non-unicity of the solution

First experiments from electron microscopy :

Hoppe, Acta Cryst. A25 (1969) 459 Hoppe, Ultramicroscopy 10, 187 (1982)

Nellist, McCallum & Rodenburg Nature A54 (1995) 49

" Resolution beyond the 'information limit' in transmission electron microscopy "





# **X-RAY PTYCHOGRAPHY**



# PTYCHOGRAPHY

ResultsScan0000/Run0000 - # 0







As we are using the sweet stucks sweets API we can actus the parameters exactly as for the command line carint

# **PTYCHOGRAPHY: PHASE & AMPLITUDE**

Object phase [-0.12- 0.08 radians]



Probe amplitude & phase



id16A @17keV Lambda detector 256x256 GaAs 150 nm step, 125 ms/frame, 566 frames With filters (~20x) <sup>®</sup>

Both object and probe, amplitude and phase are recovered at the same time



# **PTYCHO: PROBE PROPAGATION**



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# **RESOLUTION: FOURIER SHELL (RING) CORRELATION**



Resolution from Fourier shell (ring) correlation: ~15nm (comparing two scans from the same area with different positions) van Heel & M. Schatz, J. Struct. Biol. 151(2005), 250



# **PTYCHOGRAPHY-TOMOGRAPHY**



Experiments at cSAXS beamline SLS Dierolf et al Nature, 467, 436-439 (2010)

#### Mouse femur bone, imaged in 3D at 120nm resolution Voxel size : 65 nm



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# **PTYCHOGRAPHY: 3D HIGH RESOLUTION**



Test object : porous SiO<sub>2</sub> structure of 139 nm mean pore size + Ta<sub>2</sub>O<sub>5</sub> coating



3D reconstruction resolution : 16 nm

From :

- 720 angular positions
- For each angle, 180 CDI images
- $\rightarrow$  129600 images



# **HIGH RESOLUTION IMAGING WITH PTYCHO-(TOMO)**

#### Sample: micro-processor:





Select an area from the processor schematics



Socket LGA 1150, 3MB Cache, 22nm

Holler et al, Nature 543, 402–406 (2017)

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# Extraction of a 10 $\mu$ m pillar Mount on a sample holder



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The European Synchrotron Holler et al, Nature 543, 402–406 (2017)



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The European Synchrotron Holler et al, Nature 543, 402–406 (2017)

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#### **Result:**

- 14.6 nm 3D resolution
- 1200 projections
- 24 hours
- 5850 resolution elements per second



Holler et al, Nature 543, 402-406 (2017)





Page 73 Coherent X-rays and Applications I ESRF-ILL Summer school 2021 I Vincent Favre-Nicolin

The European Synchrotron Holler et al, Nature 543, 402–406 (2017)



Coherent X-rays and Applications I ESRF-ILL Summer school 2021 I Vincent Favre-Nicolin Page 74

Holler et al, Nature 543, 402–406 (2017)



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The European Synchrotron | ] Holler et al, Nature 543, 402–406 (2017)



#### IMAGING MAGNETIC NANO-STRUCTURES WITH PTYCHO-TOMOGRAPHY



Synchrotron X-rays are normally (\*) linearly polarised

A phase plate can be used to transform this into a circularly-polarised X-ray beam

Sensitivity is maximal when magnetic moment is // to X-ray photon wavevector



#### IMAGING MAGNETIC NANO-STRUCTURES WITH PTYCHO-TOMOGRAPHY







#### IMAGING MAGNETIC NANO-STRUCTURES WITH PTYCHO-TOMOGRAPHY



Setup for a ptycho-tomography setup

Using two tilt angles to be sensitive to the 3D orientation of magnetic domain !! Magnetic structure is a <u>3D vector field</u>, not a 3D scalar !!


#### IMAGING MAGNETIC NANO-STRUCTURES WITH PTYCHO-TOMOGRAPHY



Axial tomographic slice of the reconstructed magnetization vector field Note the anti- and clockwise vortices Spatial resolution ~100-200 nm



#### IMAGING MAGNETIC NANO-STRUCTURES WITH PTYCHO-TOMOGRAPHY





3D view of the magnetic reconstruction with two main domains Two vortices Vi and Vd intersect at two Bloch points (m=0)



#### **SMALL ANGLE VS BRAGG CDI**



 $A(\vec{k}) \approx FT[\Omega(\vec{r})e^{2i\pi\vec{s}\vec{u}}]$ 

#### Simulated nanowire w/insertion

• - 2% strain along x



#### **SMALL ANGLE VS BRAGG CDI**



## **BRAGG CDI: STRAIN RECONSTRUCTION**



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## **BRAGG PTYCHOGRAPHY**



Bragg Ptychography : 2D Ptychography at different rotation angles (angle step ~0.04°, ptycho step 300 nm)





## **BRAGG PTYCHOGRAPHY ON MOLLUSC SHELLS**





Pinctada margaritifera shell at different length scales

#### Calcite nano-structures





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#### **BRAGG PTYCHOGRAPHY ON MOLLUSC SHELLS**



#### Diffraction on individual calcite prisms



#### **BRAGG PTYCHOGRAPHY ON MOLLUSC SHELLS**



Page 87 Coherent X-rays and Applications I ESRF-ILL Summer school 2021 I Vincent Favre-Nicolin



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### **BRAGG PROJECTION PTYCHOGRAPHY**

Page 88



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#### **BRAGG PROJECTION PTYCHOGRAPHY**



Single-angle Bragg ptychography

- Allows reconstructing an extended object with limited data:
  - Faster data collection
  - Less radiation damage
  - Only sensitive to deformation in the detector plane



### **XFEL LATTICE VIBRATION IMAGING USING BRAGG CDI**





## **XFEL LATTICE VIBRATION IMAGING USING BRAGG CDI**



Experimentally recorded coherent diffraction patterns from a single nanocrystal for delay times of –10 and +60 ps.

## Bragg peak angular shift as a function of delay time for two different nanocrystals





# Orthogonal cut planes through the center of the nanocrystal showing the projected displacement as a function of delay time



## **XFEL LATTICE VIBRATION IMAGING USING BRAGG CDI**



#### Displacement

Orthogonal slices taken either side of the center (top) of the nanocrystal compare the projected displacement obtained from the experiment (middle) with a simulated (1, 1) mode for a cylinder (bottom).



#### **THANK YOU FOR YOUR ATTENTION !**

