

Soft Matter Studies with X-rays

Theyengeri Narayanan

ESRF – The European Synchrotron

M. Mitov, *Sensitive Matter - Foams, Gels, Liquid Crystals, and Other Miracles* (Harvard University Press, 2012)

R. Piazza, *Soft Matter: The Stuff that Dreams are Made of* (Springer, 2011)

M. Doi, *Soft Matter Physics* (OUP Oxford, 2013)

R.A.L. Jones, *Soft Condensed Matter* (OUP Oxford, 2004)

LS Hirst, *Fundamentals of soft matter science* (CRC press, 2020)

W. de Jeu, *Basic X-ray Scattering for Soft Matter* (OUP Oxford 2016)

T. Narayanan and O. Konovalov, *Materials*, **13**, 752 (2020);

<https://doi.org/10.3390/ma13030752>

Outline

- What is Soft Matter?
- Some general features
- Different X-ray techniques employed
- Self-assembly & complexity
- Out-of-equilibrium phenomena
- Summary and outlook

What is Soft Matter?

Soft matter is a subfield of condensed matter physics (CMP) comprising a variety of physical states that are easily deformed by thermal stresses or thermal fluctuations. They include liquids, colloids, polymers, foams, gels, granular materials, and a number of biological materials. These materials share an important common feature in that predominant physical behaviors occur at an energy scale comparable with room temperature thermal energy. At these temperatures, quantum aspects are generally unimportant. Pierre-Gilles de Gennes, who has been called the "founding father of soft matter," received the Nobel Prize in physics in 1991 for discovering that the order parameter from simple thermodynamic systems can be applied to the more complex cases found in soft matter, in particular, to the behaviors of liquid crystals and polymers.

Matière molle » Madeleine Veyssié

Today soft matter science is an interdisciplinary field of research where traditional borders between physics and its neighboring sciences such as chemistry, biology, chemical engineering and materials science have disappeared. It is one of the frontiers of CMP along with strongly correlated electron systems and nanoscience.

Soft Matter: Encounter in everyday life

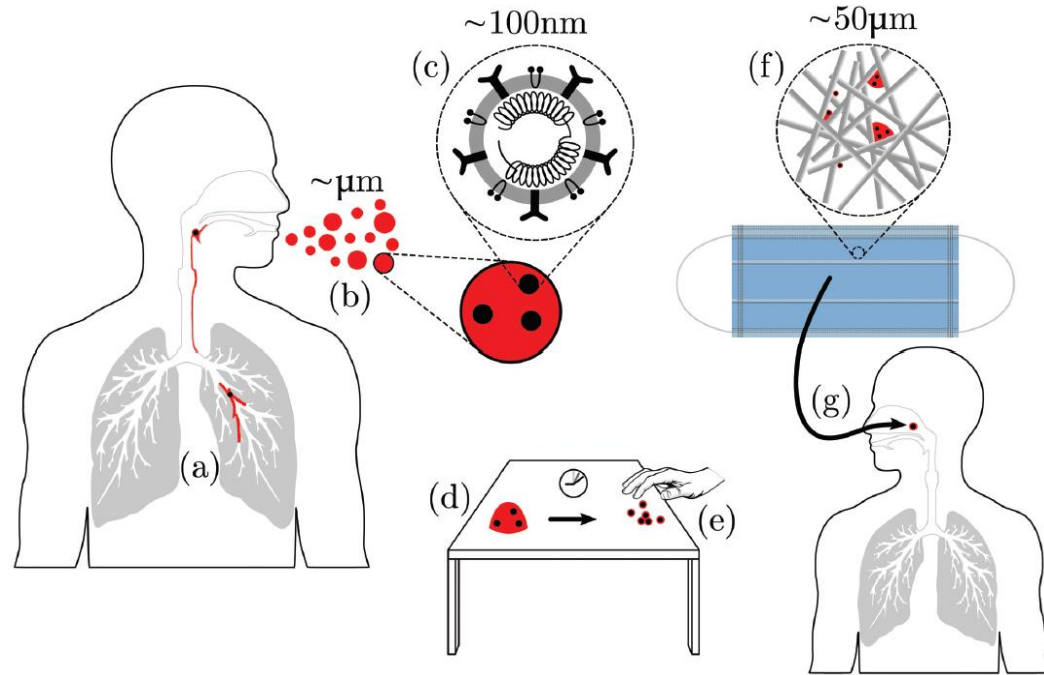


Sustainable development through more rational design of consumer products

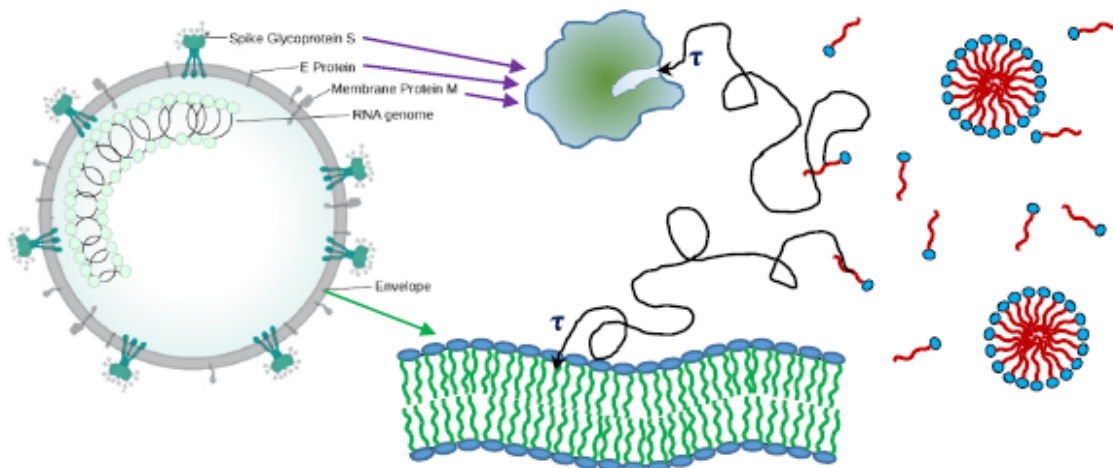
Soft Matter: COVID-19

COVID-19 pandemic exposed the knowledge-gap

Interaction of detergents with SARS CoV-2

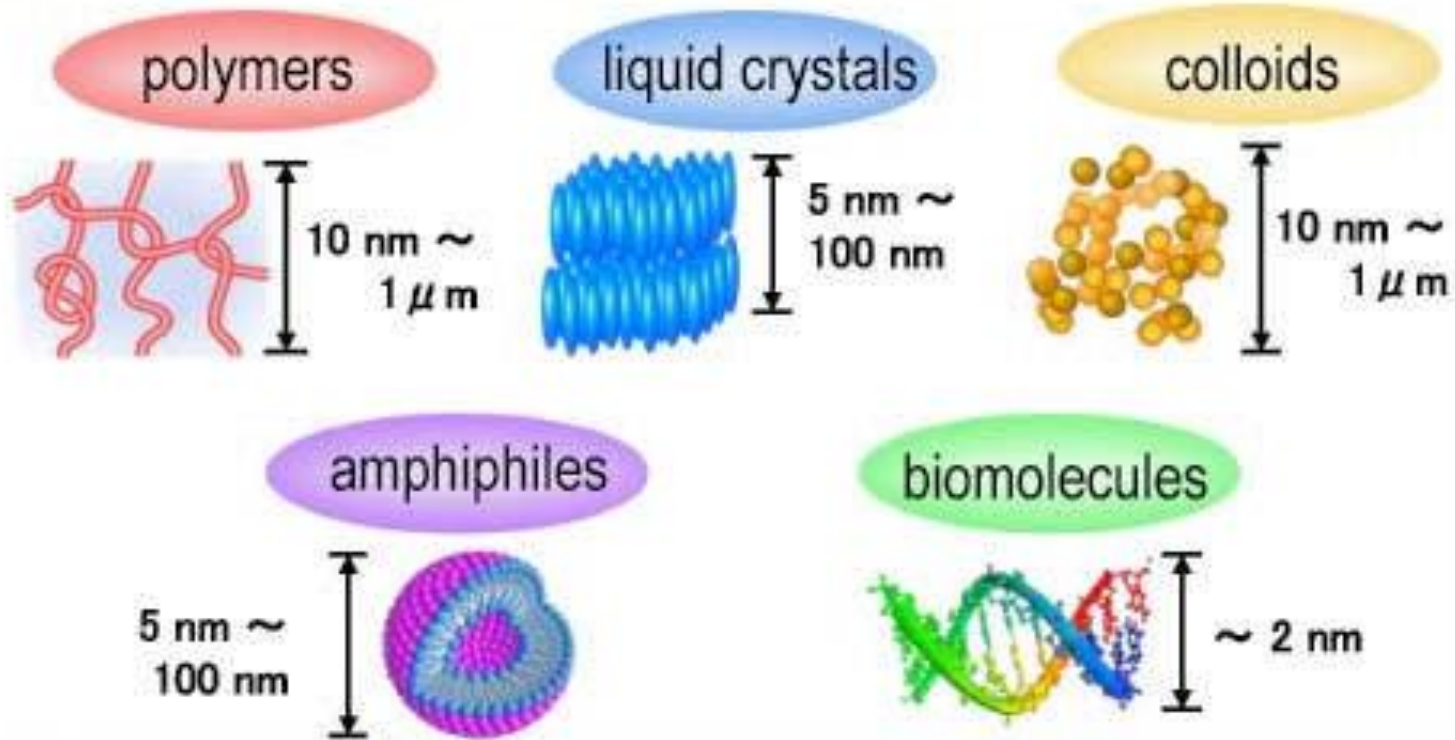


W.C.K. Poon *et al.*, *Soft Matter* (2020)



Formulation of efficient detergents, vaccines, drugs, etc.

Soft Matter Systems



Meso-scale structures determine material properties

SAXS, WAXS, USAXS, GISAXS
(SANS, USANS, GISANS, etc.)

Soft Matter Features

Materials which are soft to touch – characterized by a small elastic modulus (energy/characteristic volume), typically $10^9 - 10^{12}$ times lower than an atomic solid like aluminum.

Dominance of entropy

Strong influence of thermal fluctuations ($\sim k_B T$)

Characteristic size scale or microstructure $\sim 100 - 1000$ nm

Shear modulus, $G \sim \text{Energy/Free volume} \gg 10^9 - 10^{12}$ smaller

Low shear modulus (G) \gg soft and viscoelastic

Soft Matter studies seek to address the link between microscopic structure/interactions and macroscopic properties.

Soft Matter constitutes a significant fraction of modern day Nanoscience/Nanotechnology.

Self-Assembled Soft Matter Systems

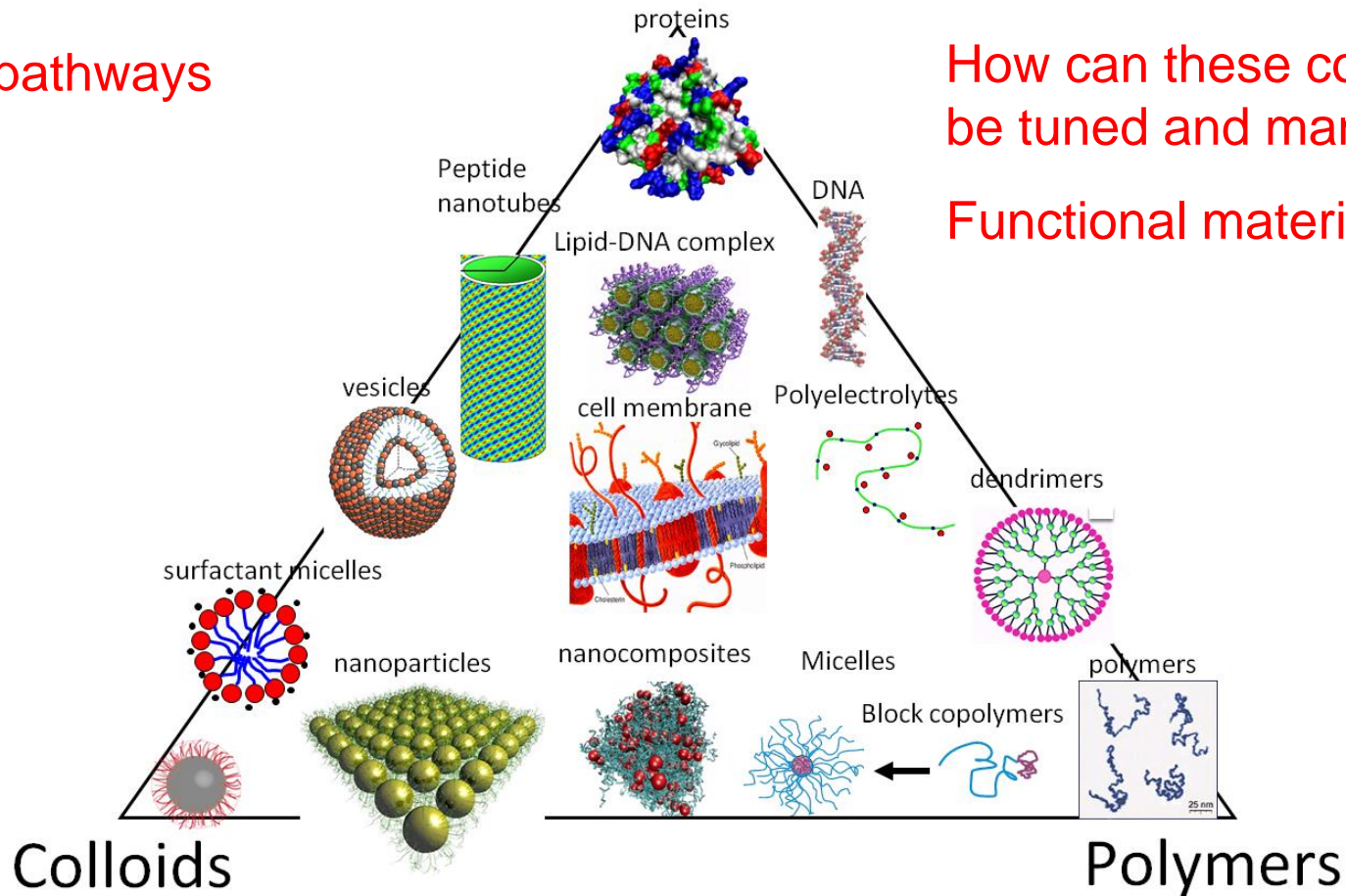
How are these complexes formed?

Kinetic pathways

Biomolecules

How can these complexes be tuned and manipulated?

Functional materials



T. Narayanan et al., Crystallogr. Rev. (2017)

Synchrotron Techniques used in Soft Matter

Synchrotron Radiation Studies of Soft Matter

- **High spectral brilliance or brightness**

Real time studies in the millisecond range, micro/nano focusing and high q resolution

Time-resolved SAXS, WAXS, micro-SAXS, USAXS, etc.

- **Partial coherence**

Equilibrium dynamics using the coherent photon flux (for concentrated systems)

Photon correlation spectroscopy (XPCS)

- **Continuous variation of incident energy**

Contrast variation of certain heavier elements, e.g. Fe, Cu, Se, Br, Rb, Sr, etc.

Anomalous Scattering – contrast variation

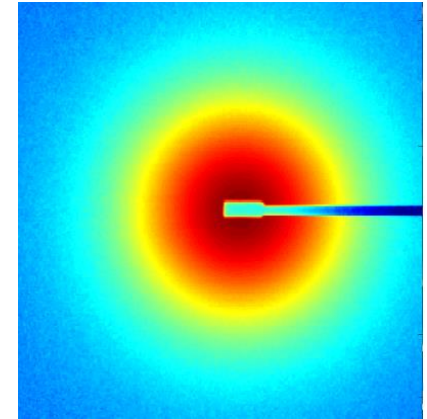
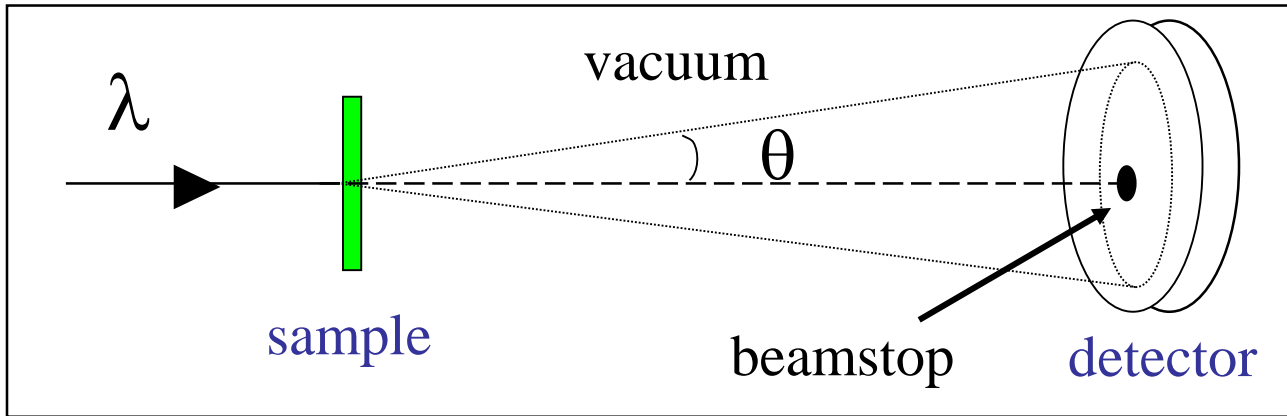
- **Complementary imaging techniques**

X-ray microscopy, micro and nano tomography, etc.

Radiation damage

Small-Angle X-ray Scattering (SAXS)

Scattering originates from the spatial fluctuations of electron density



$$q = \frac{4\pi}{\lambda} \sin(\theta / 2)$$

Measured Intensity: $I_S = i_0 T_r \varepsilon \Delta\Omega \left(\frac{d\sigma}{d\Omega} \right)$ Differential scattering cross-section

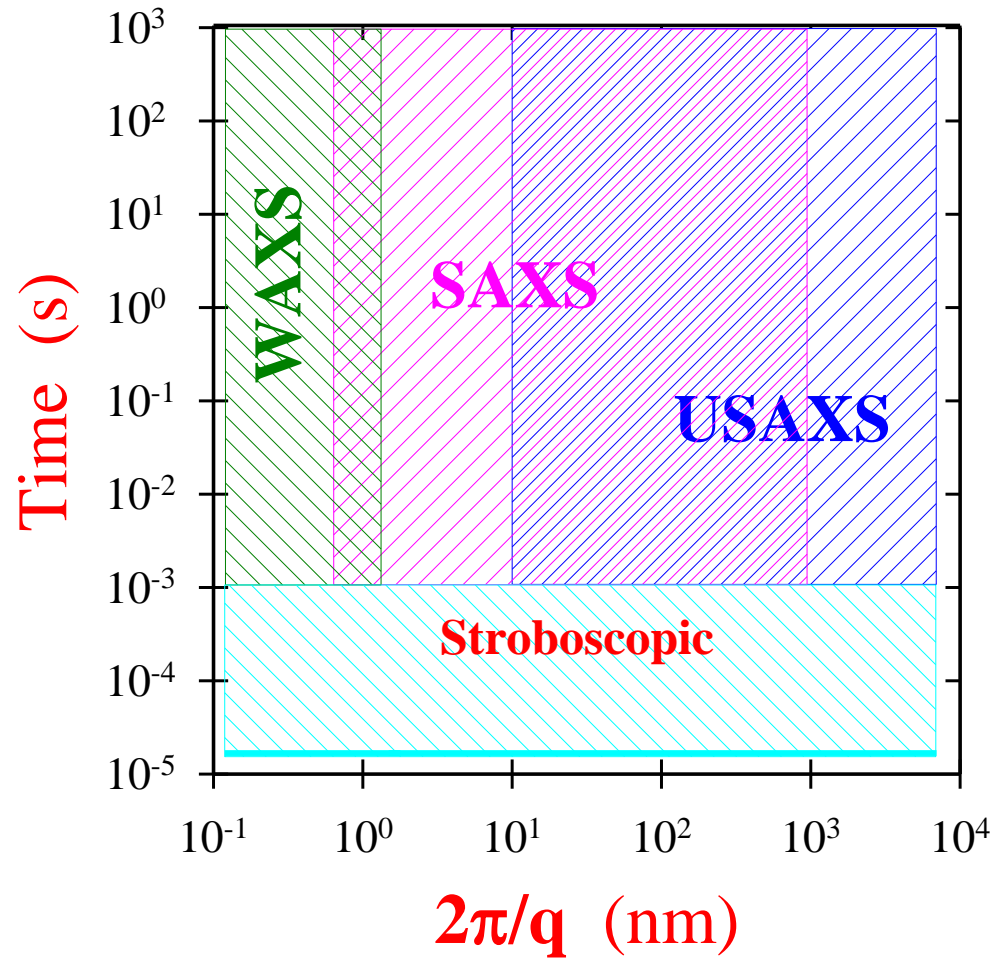
i_0 - incident flux
 T_r - transmission
 ε - efficiency
 $\Delta\Omega$ - solid angle

$$I(q) = \frac{d\Sigma}{d\Omega} = \frac{1}{V_{Scat}} \frac{d\sigma}{d\Omega}$$

Ultra SAXS/SAXS/WAXS

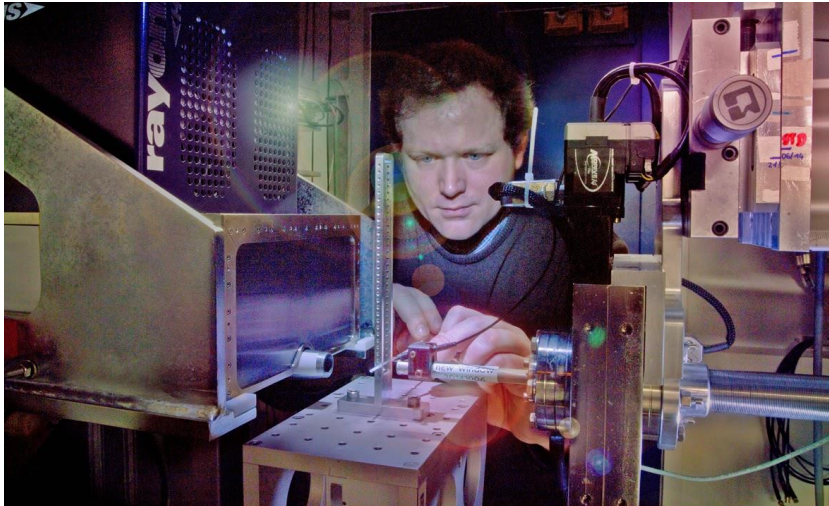
Beamline ID02

34 m

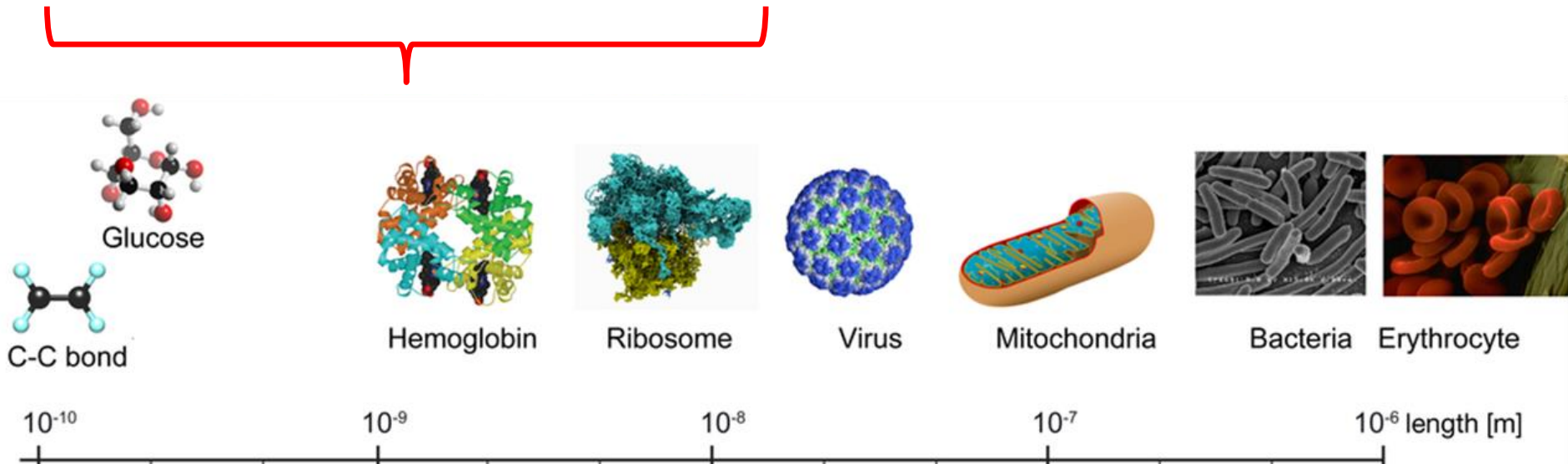
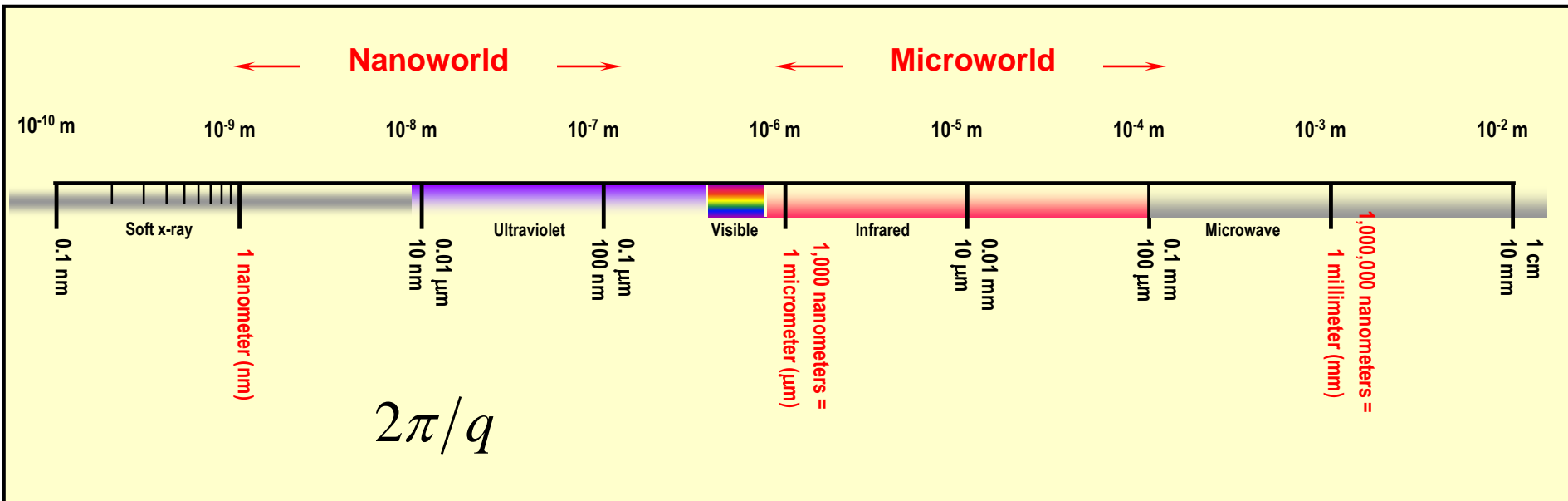


Δq SATO III (100000)

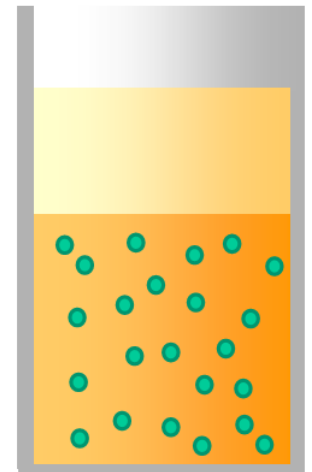
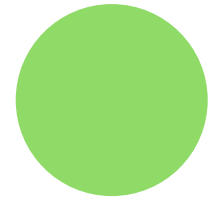
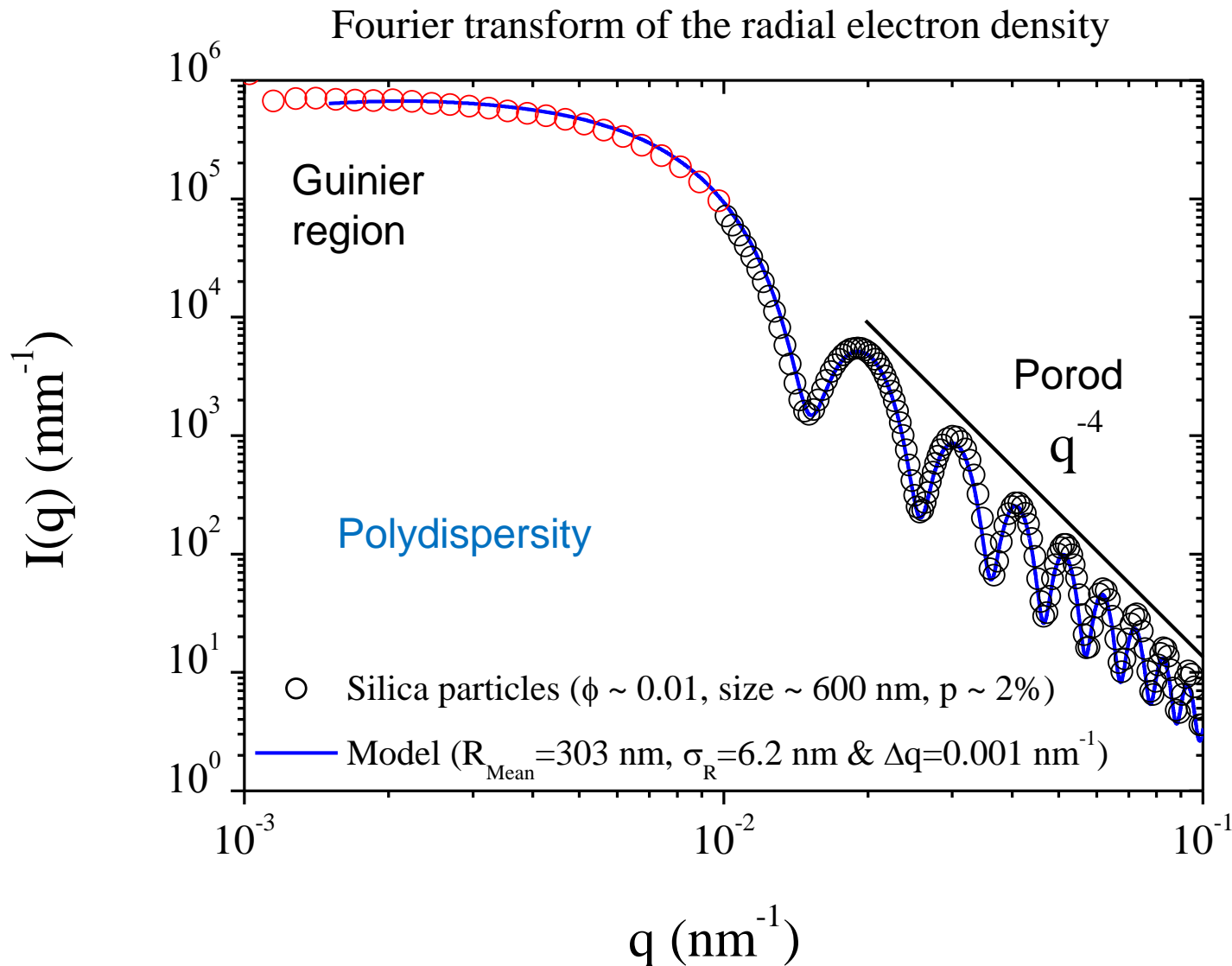
Time resolution: $< 100 \mu\text{s}$



Size scales probed by SAXS & related techniques



SAXS from dilute spherical particles



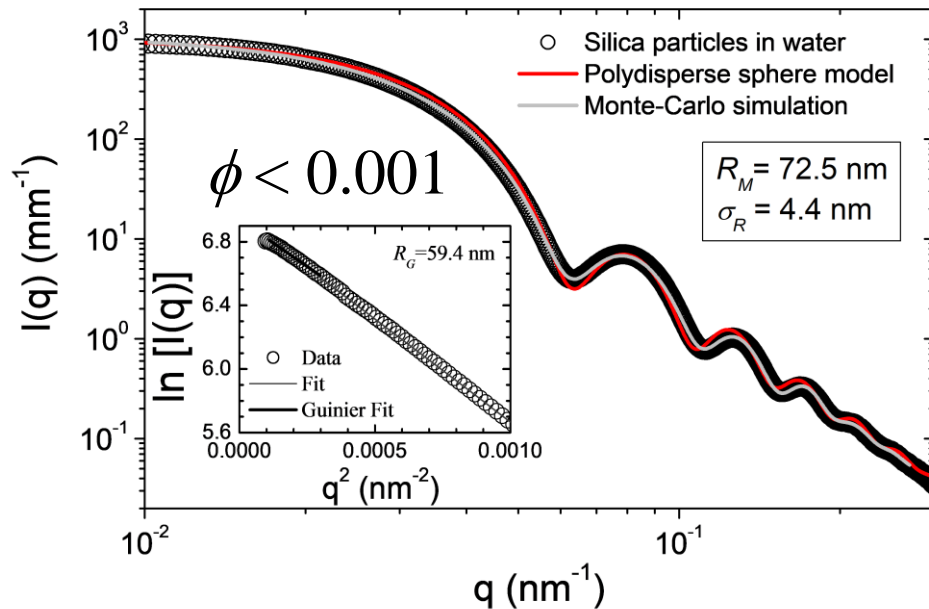
Modeling or simulation required to extract quantitative information

Form & Structure Factors

Differential scattering cross-section per unit volume

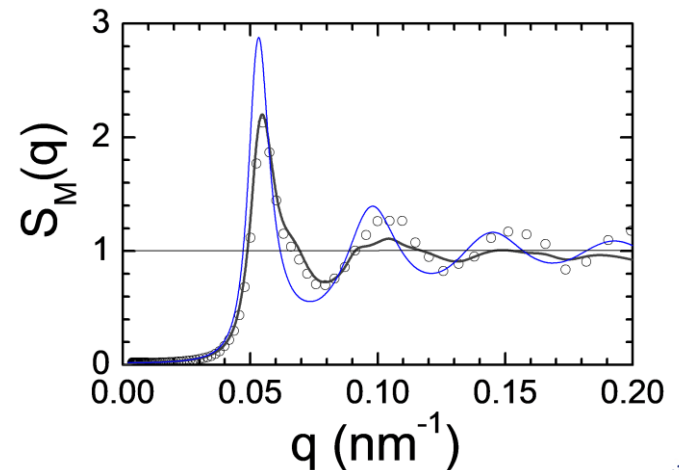
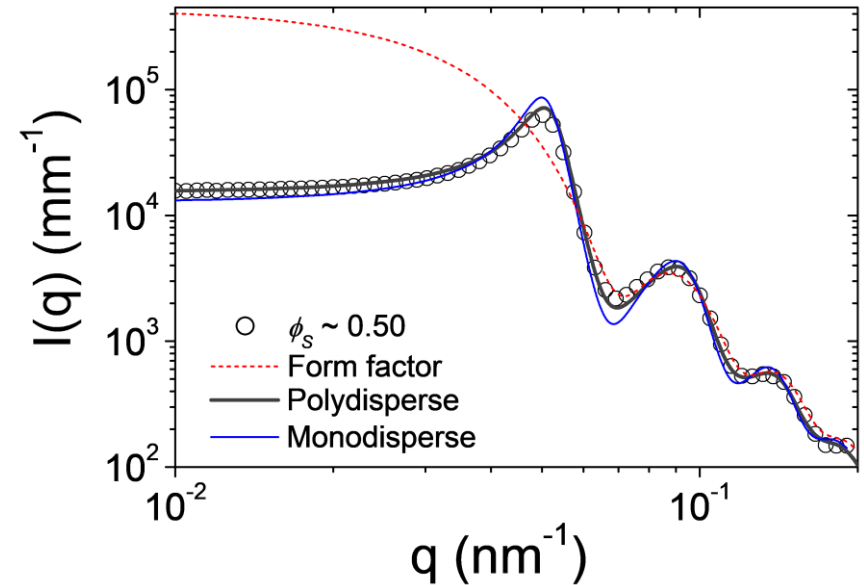
$$I(q) = N(\Delta\rho^* V)^2 P(q) S_M(q)$$

FT of radial electron density



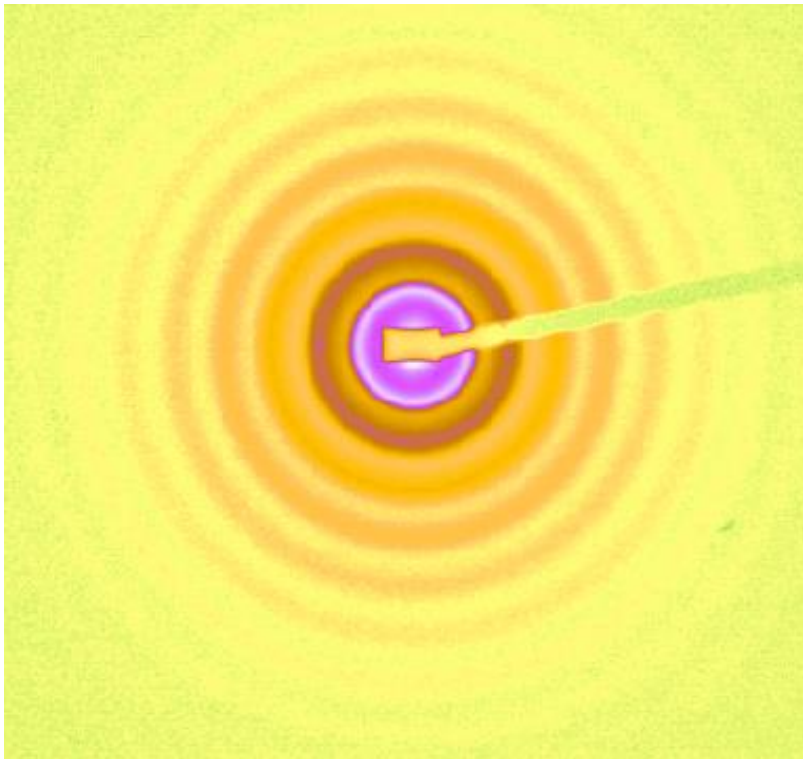
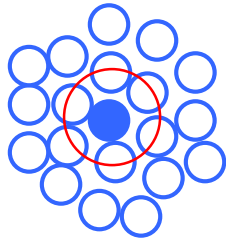
pair correlation function

$S(q)$ from liquid state theories (e.g. Percus-Yevick (PY)) or simulations

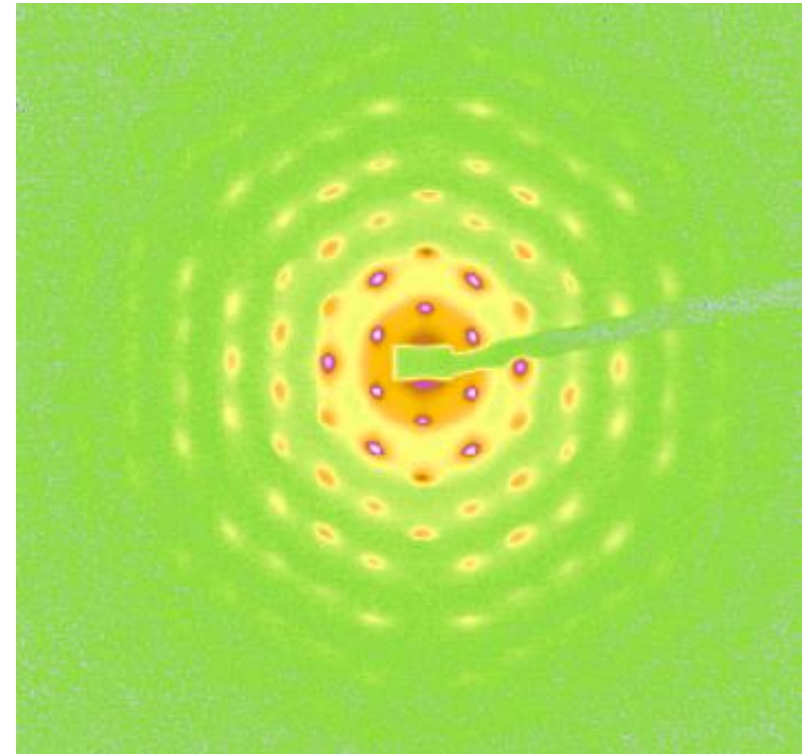


Structure Factors at high packing fractions

E.g. 60%



Glass

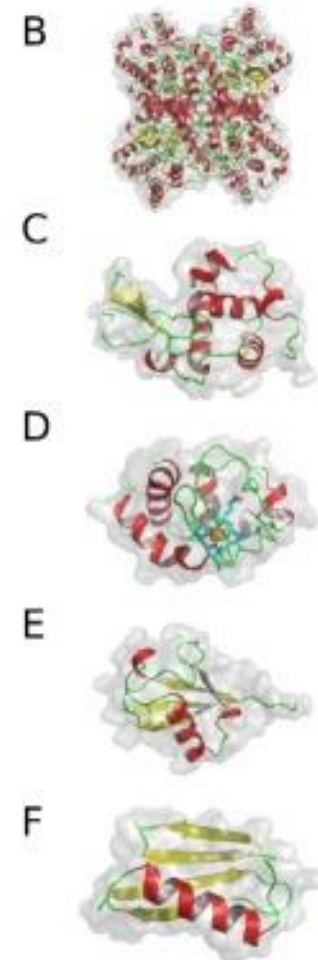
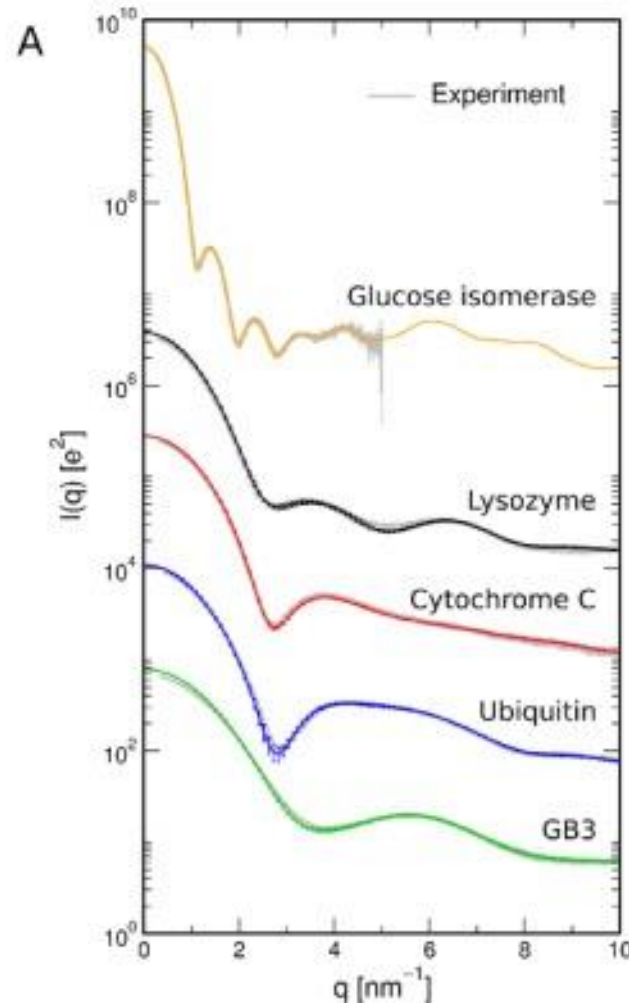
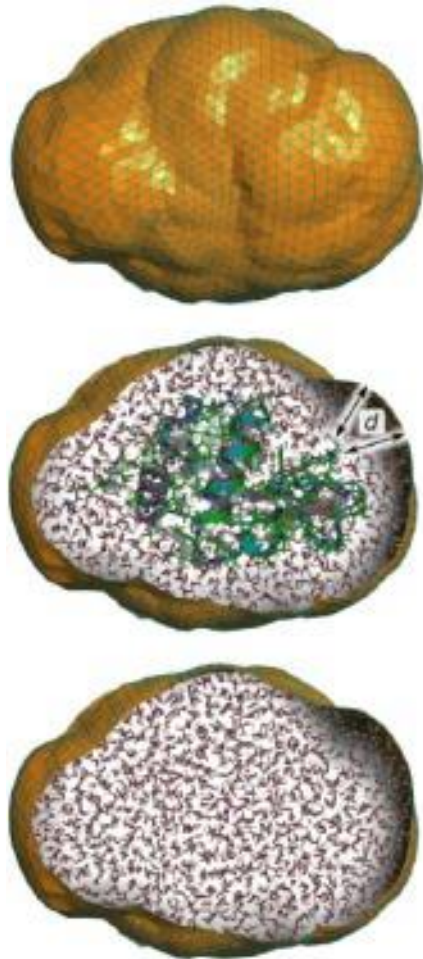


Crystal

Protein Solution Scattering

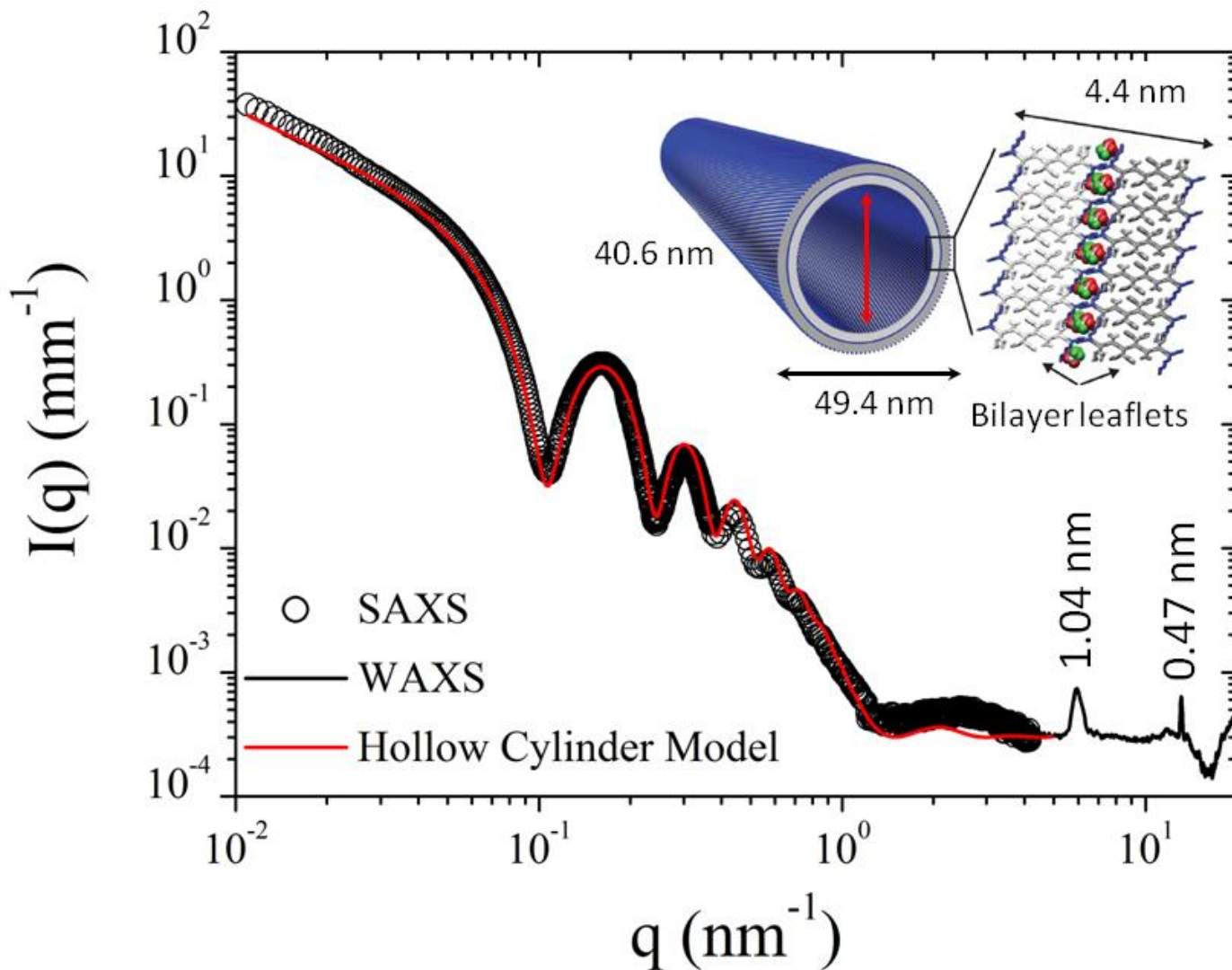
Traditionally a few structural features: size, shape, size or density distribution

Beamline - BM29



Hierarchical Structures

Self-assembled nanotubes formed by an amyloid β peptide

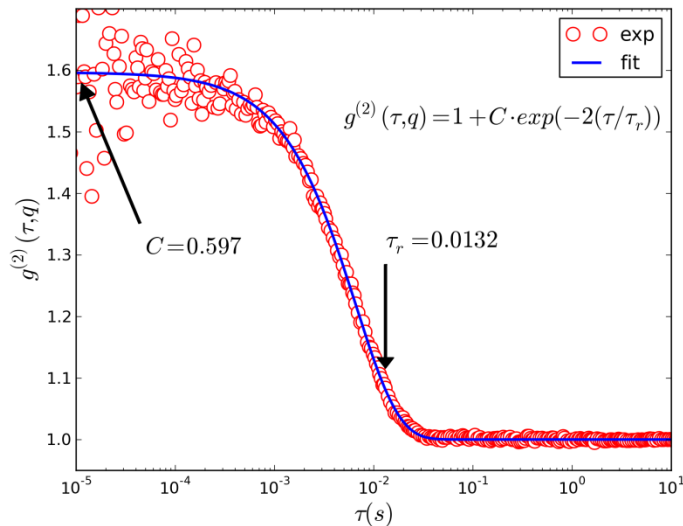


X-ray Photon Correlation Spectroscopy (XPCS)

Coherent beam

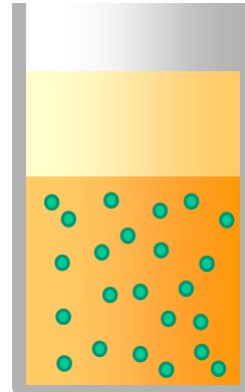
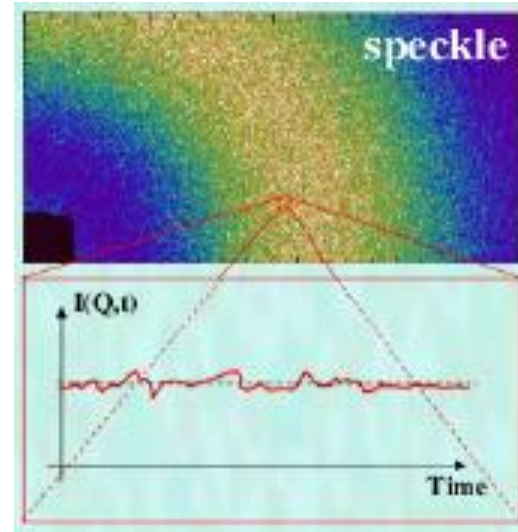
Beamline – ID10

$$g^{(2)}(\tau) = \frac{\langle I(t)I(t + \tau) \rangle}{\langle I(t) \rangle^2}$$



Silica microspheres in water
 $d = 0.49 \pm 0.02 \mu\text{m}$, $q = 0.09 \text{ nm}^{-1}$

$$1/\tau_r = D_0 q^2$$



$$\langle \Delta r^2(\tau) \rangle = 6D_0\tau$$

mean-square displacement

$$D_0 = \frac{k_B T}{6\pi\eta R}$$

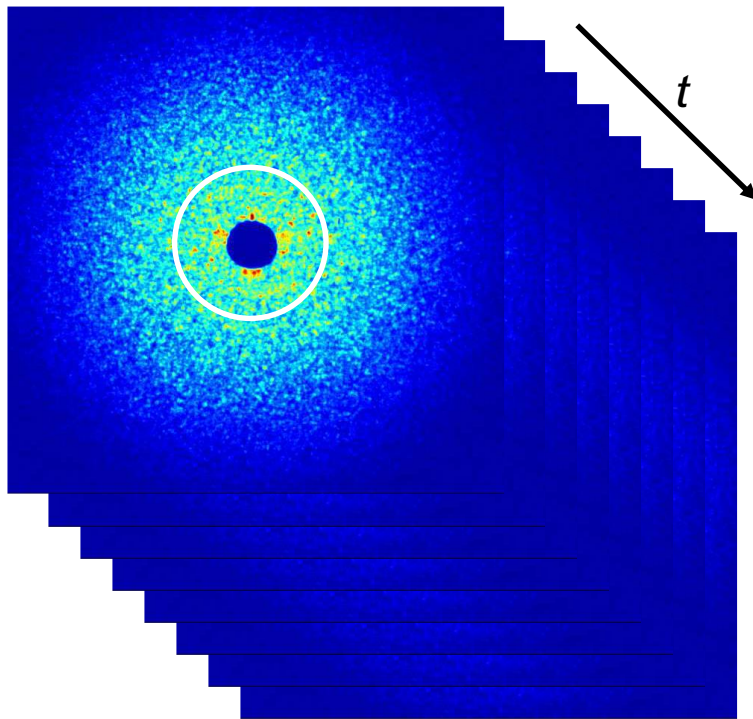
diffusion constant
 (Stokes-Einstein)

Multi-Speckle XPCS

Multi speckle XPCS at small and wide angles: **ID10 beamline** (Y. Chushkin)

At ultra low angles, $10^{-3} \leq q \leq 10^{-1} \text{ nm}^{-1}$: ID02 beamline

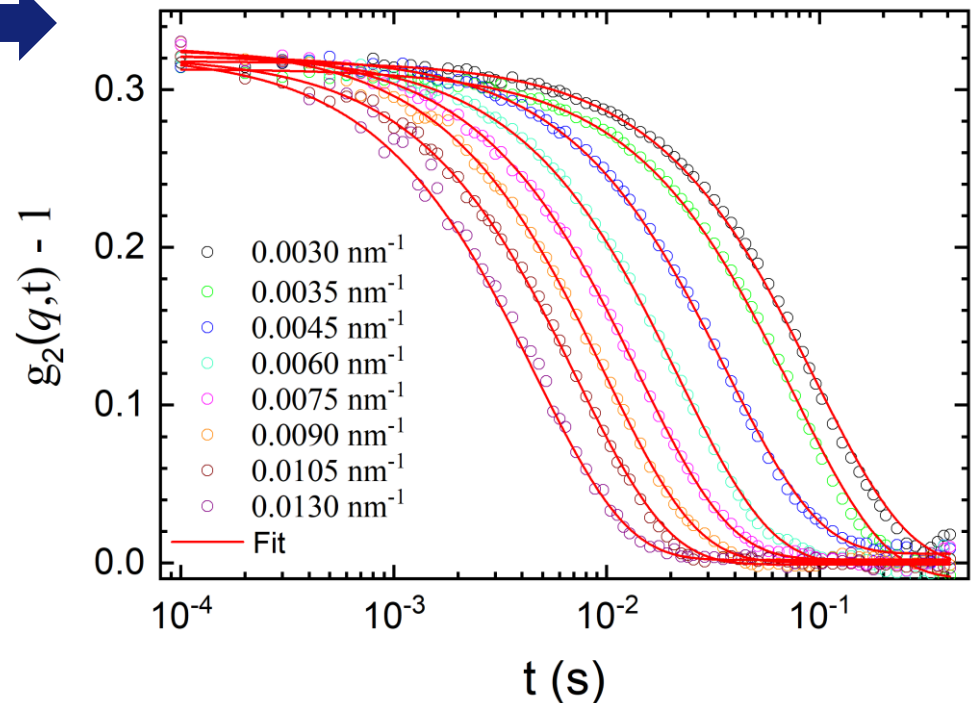
Suitable for optically opaque systems



Dilute silica colloids of 430 nm in size

Intensity autocorrelation function

$$g_2(\mathbf{q}, t) = \frac{\langle I(\mathbf{q}, \tau) I(\mathbf{q}, \tau + t) \rangle}{\langle I(\mathbf{q}) \rangle^2}$$

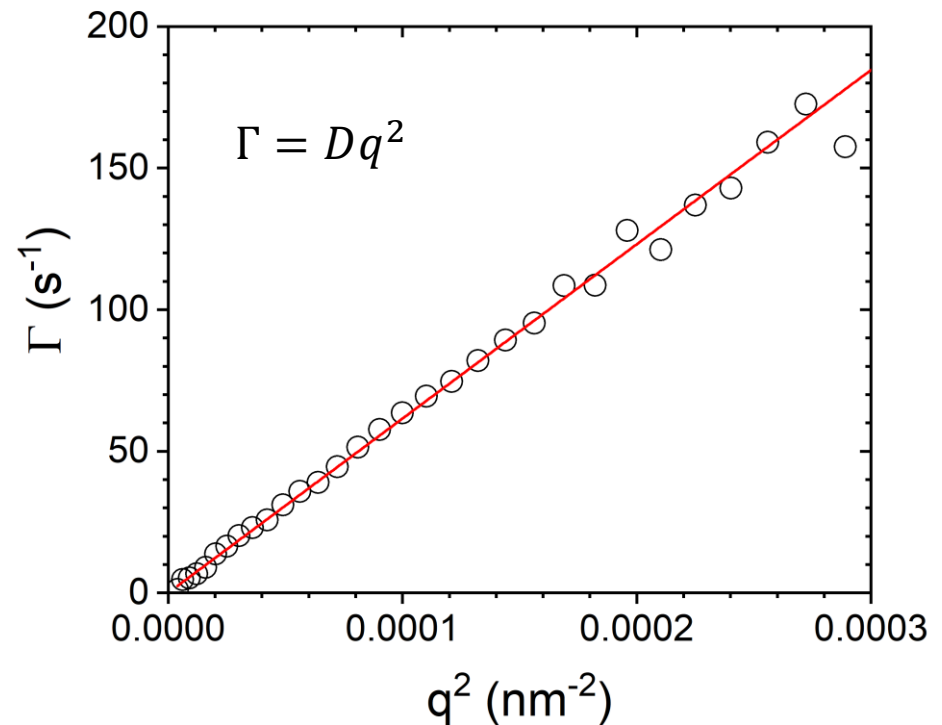
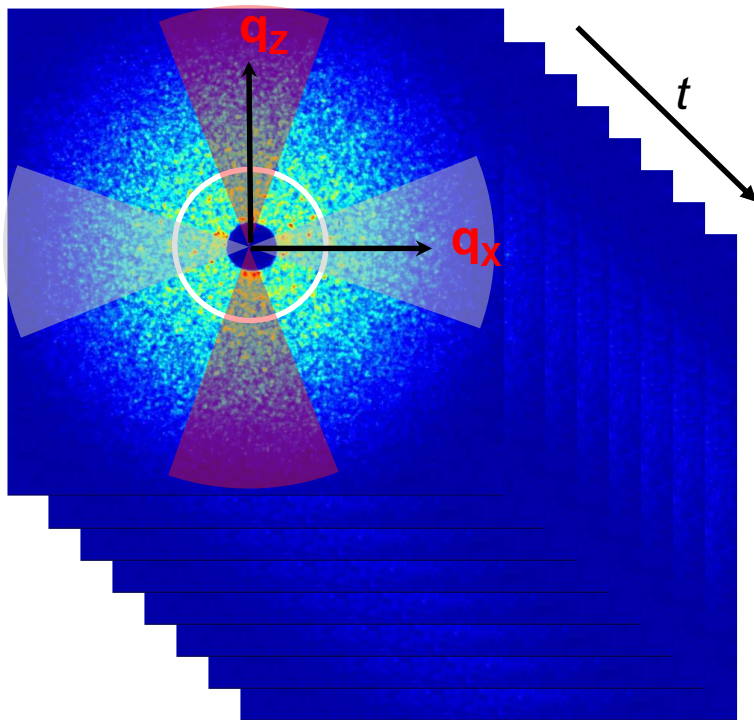


Multi-Speckle XPCS

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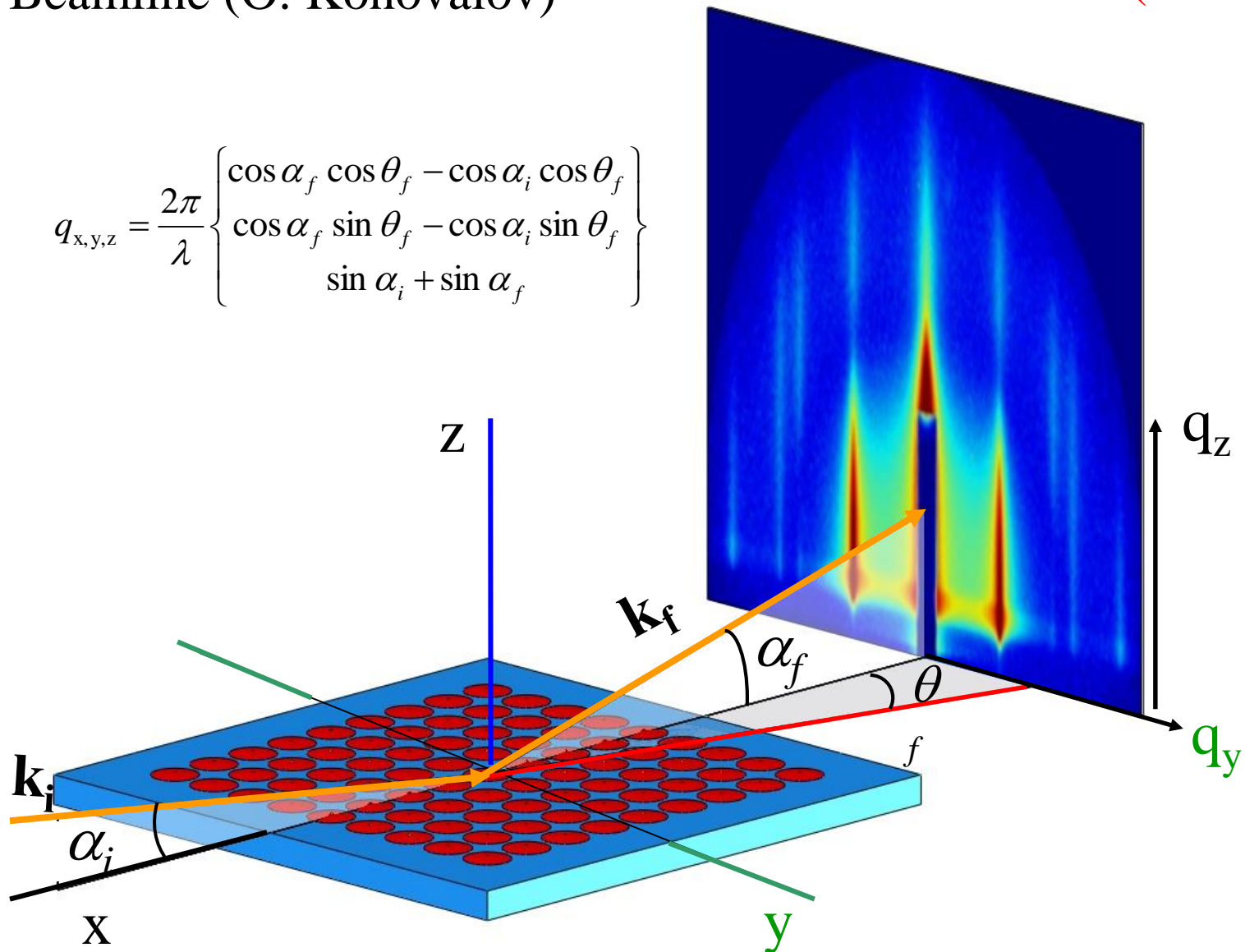
Dilute silica colloids of 430 nm in size

Grazing Incidence Small-Angle X-ray Scattering

ID10 Beamline (O. Kononov)

(GISAXS)

$$q_{x,y,z} = \frac{2\pi}{\lambda} \begin{cases} \cos \alpha_f \cos \theta_f - \cos \alpha_i \cos \theta_i \\ \cos \alpha_f \sin \theta_f - \cos \alpha_i \sin \theta_i \\ \sin \alpha_i + \sin \alpha_f \end{cases}$$



ID10 Surface & Interface Scattering Beamline

GISAXS, GID, XRR, GIXF

(O. Konovalov)

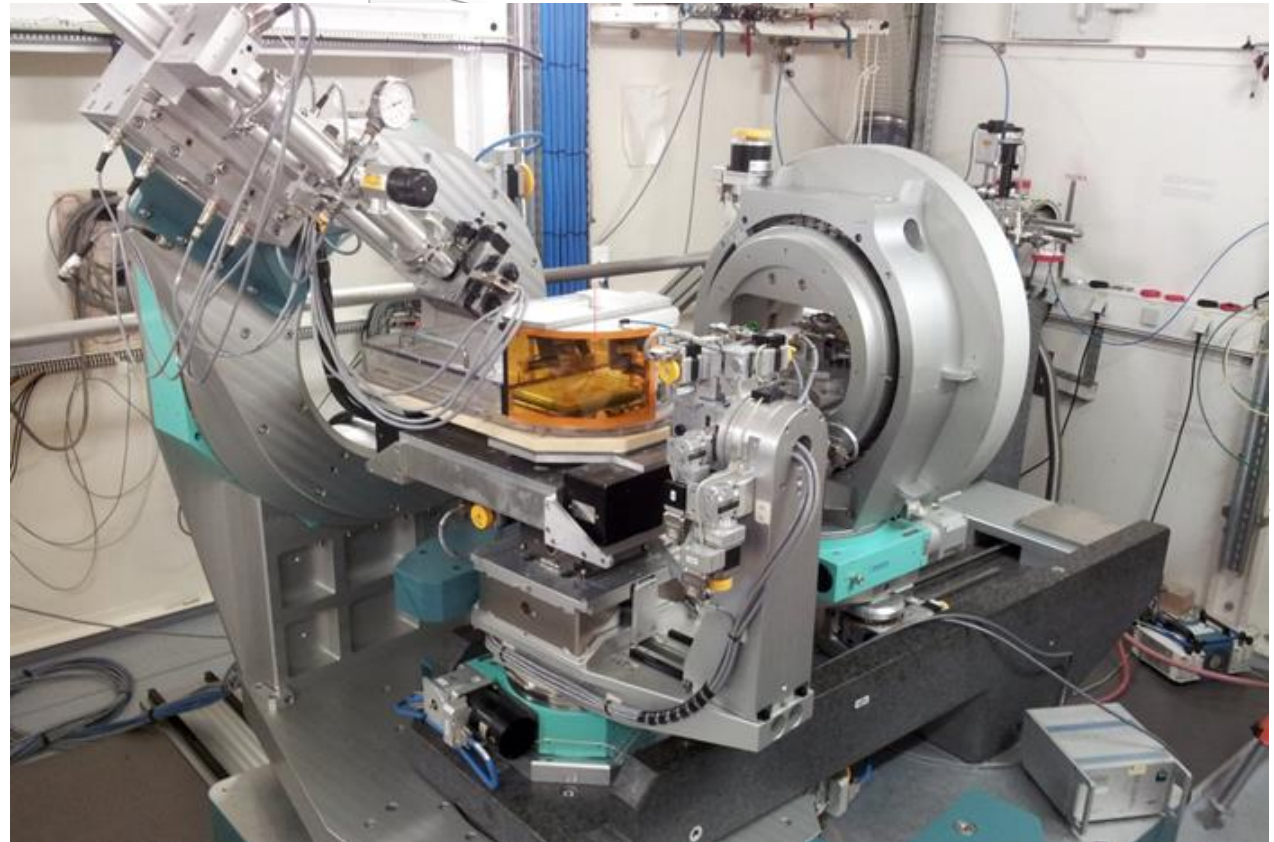
Multipurpose instrument for surface/interface studies

4 circle diffractometer

Beam deflector stage for liquid surfaces

The two-crystal
deflector stage rotates
the X-ray beam around
a fixed point on the
liquid surface

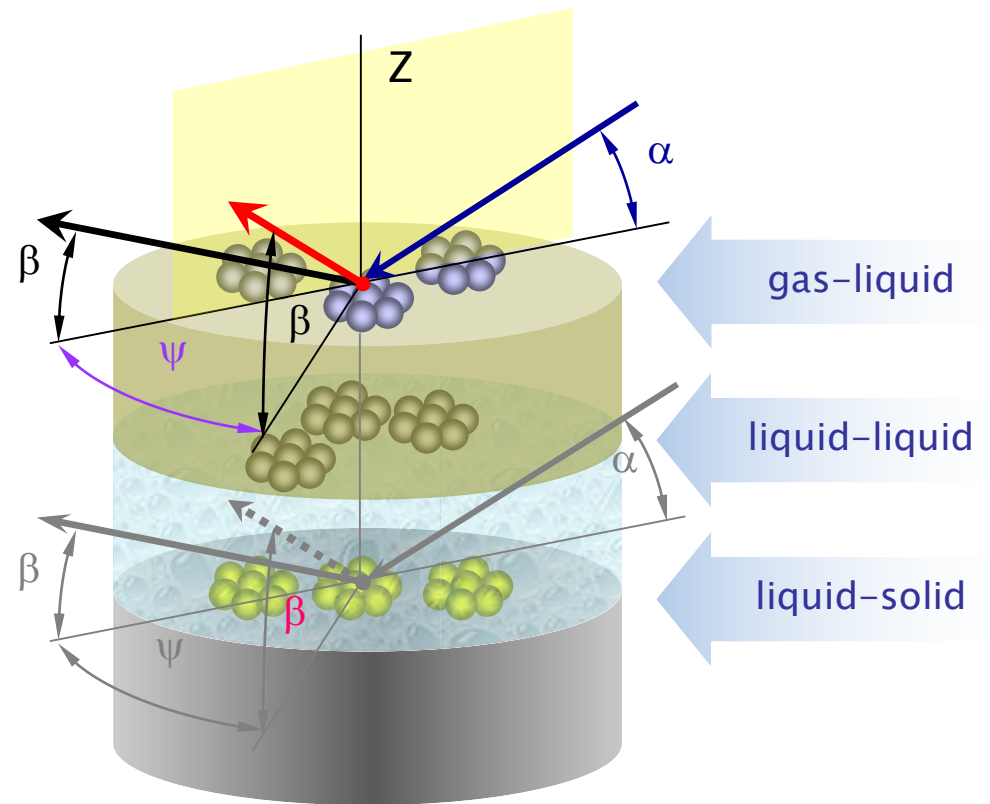
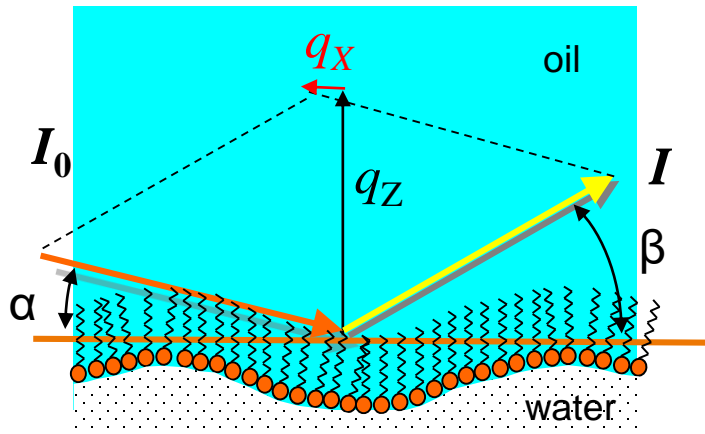
$\left\{ \begin{array}{l} q_x \\ q_y \\ q_z \end{array} \right.$



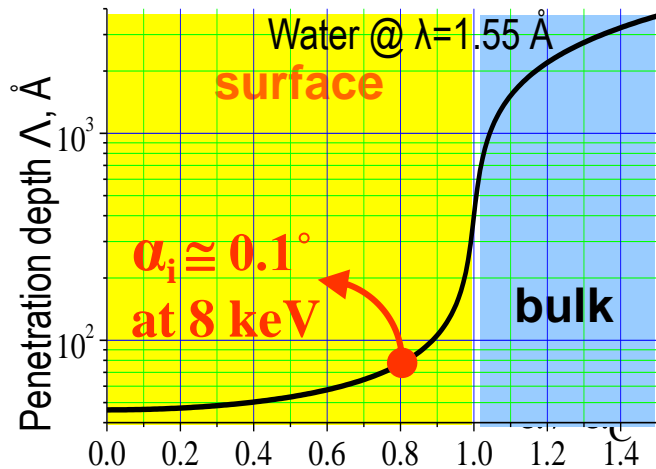
Soft Interfaces Scattering

Beamline ID10

Using higher energy X-rays
(> 30 keV)

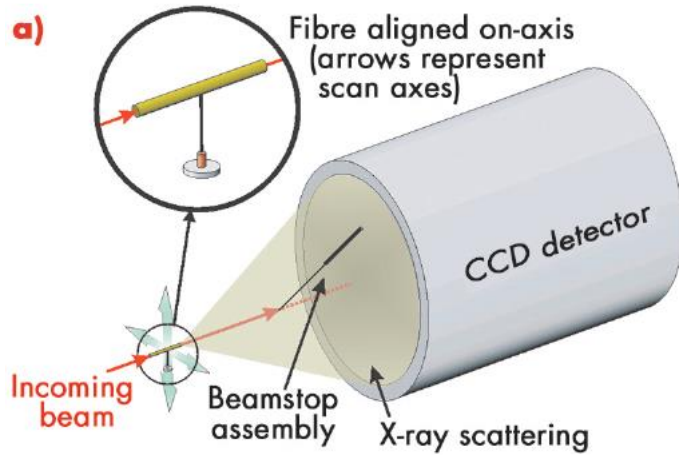


Varying the penetration depth



Scanning Micro-diffraction

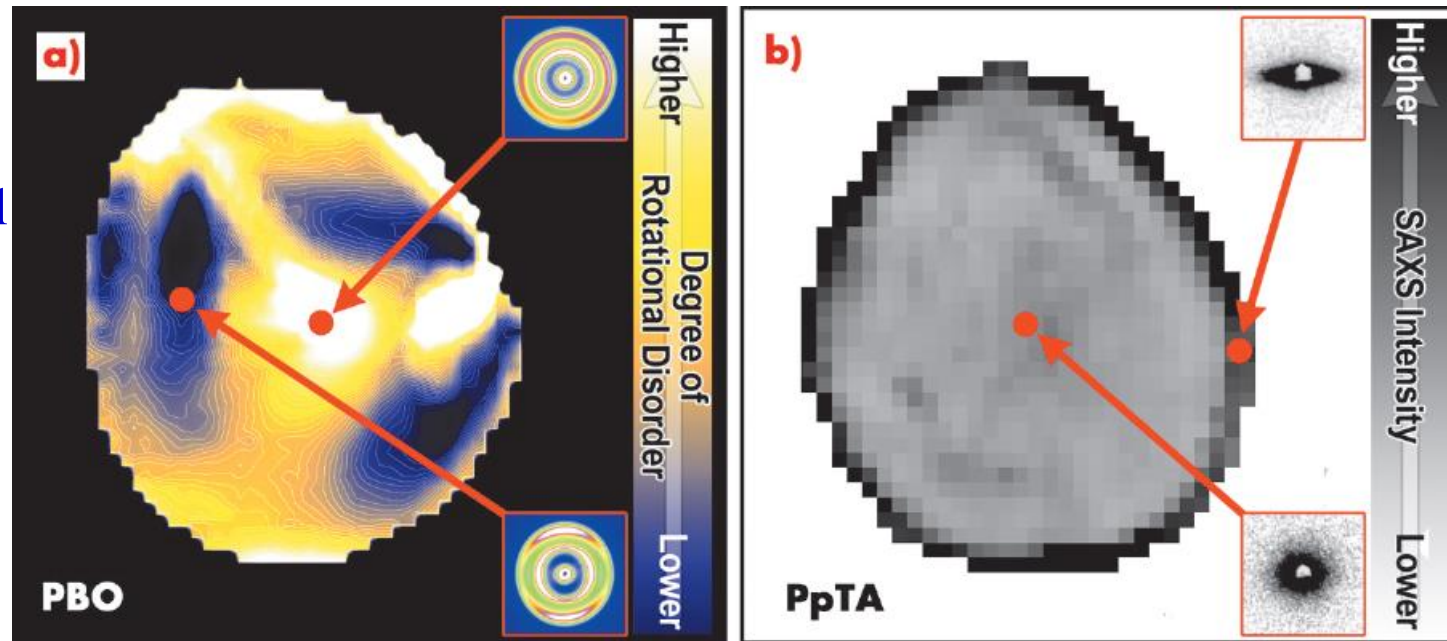
Beamline (ID13)



Combining the real space resolution provided by the beam and reciprocal space information from diffraction/scattering

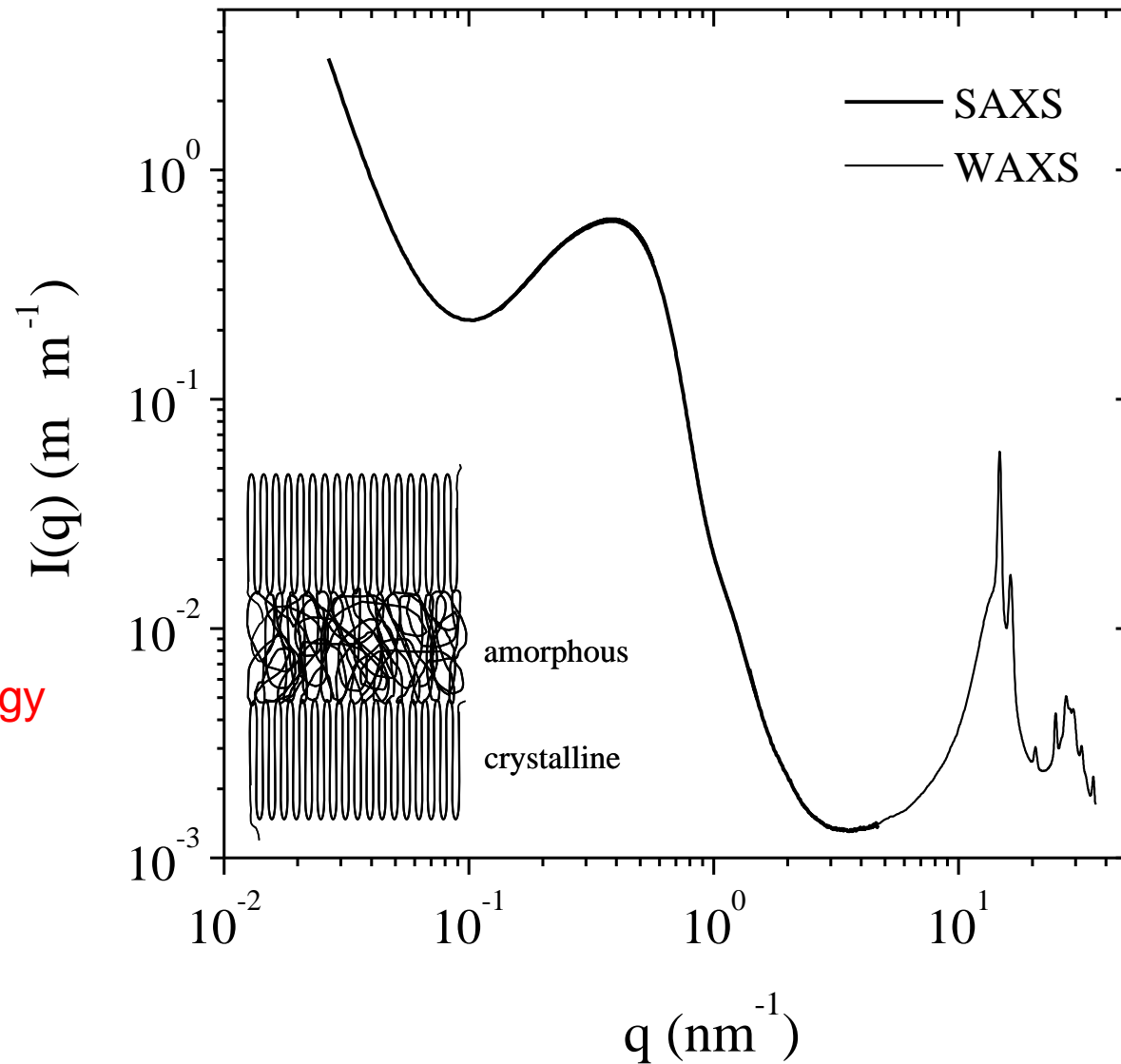
Correlate the local nanostructure to the fiber mechanical properties.

Elucidating the local nanostructure

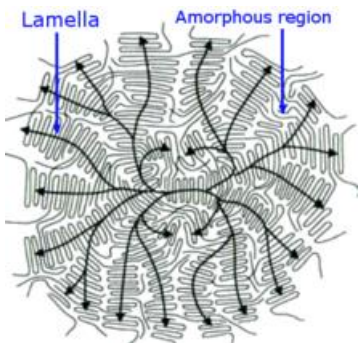


R. Davies *et al.*, *APL* (2008)

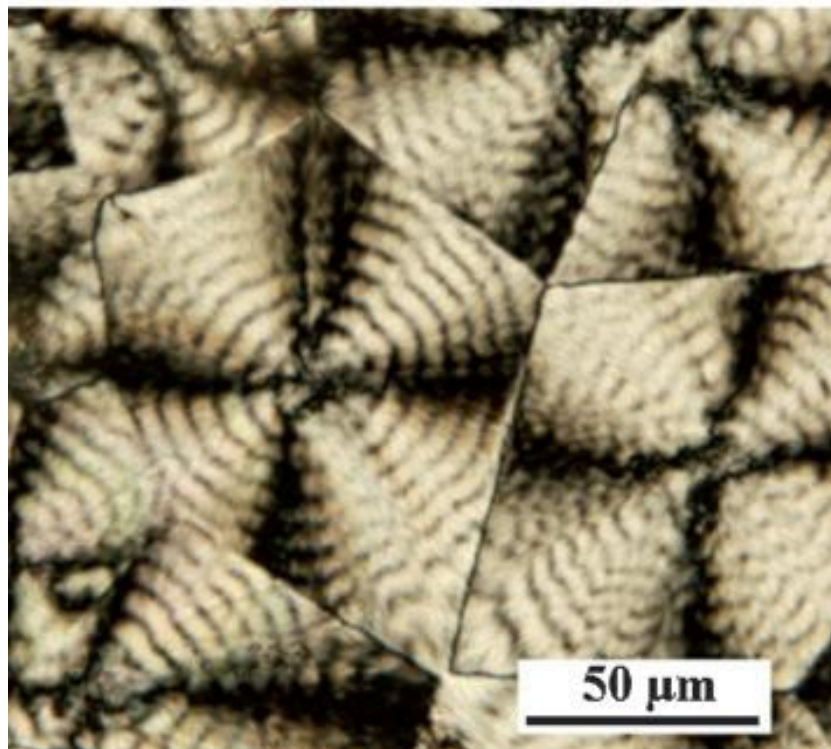
SAXS/WAXS from Semi-crystalline Polymers



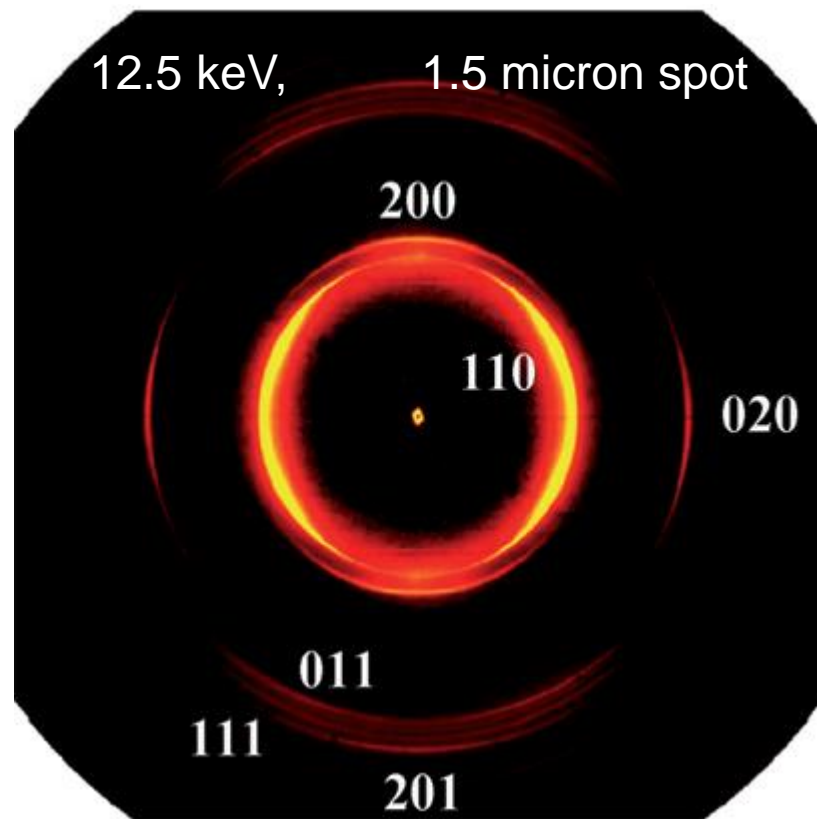
Spherulite morphology



Scanning Micro-diffraction on HDPE spherulites



- **high density poly-ethylene**
- spherulites under polarized light banded structures indicating long range order

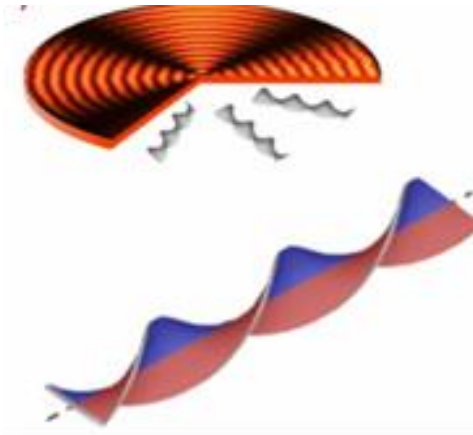
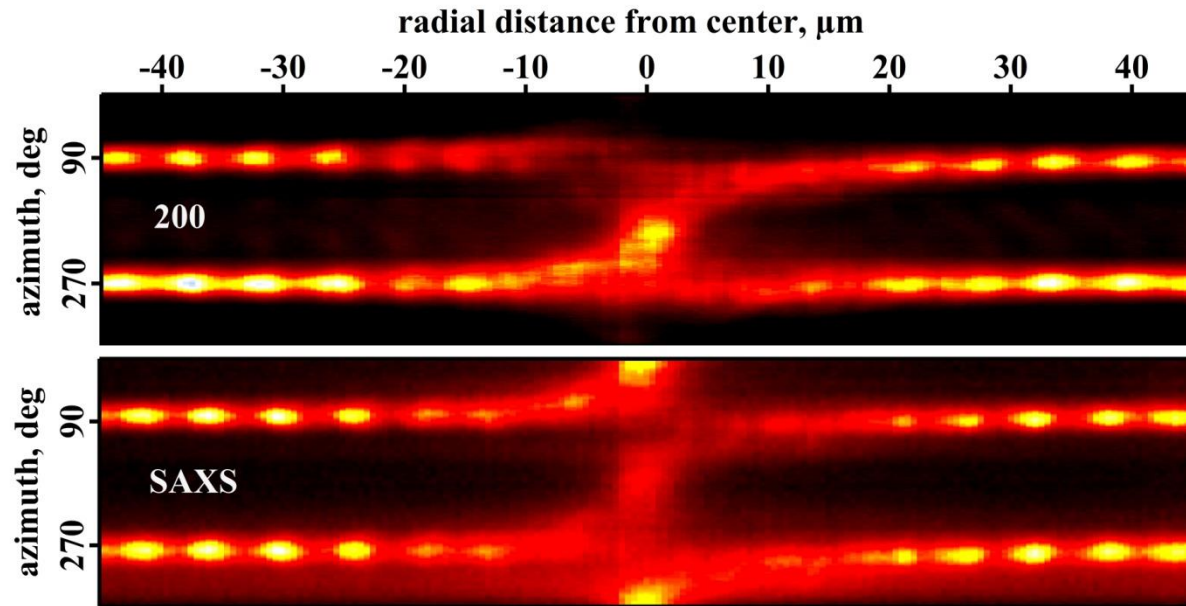
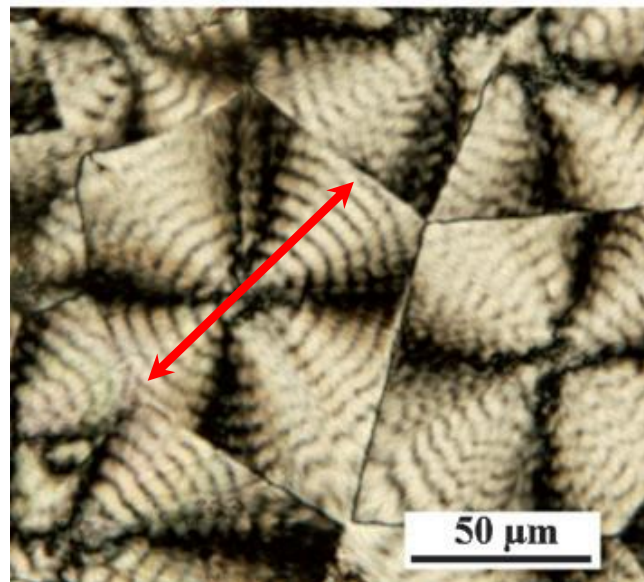


- **SAXS/WAXS** patterns
- line scans across the center reveal information on crystallite orientation

M. Rosenthal et al., Angewandte Chemie, 123, 9043-9047 (2011)

Chirality of twisted polymer crystals

Azimuth/Intensity vs Distance from the center in μm



- 35° tilt between c-axis and the normal of the base plane of crystalline lamellas
- orientation of b-axis aligned with growth direction
- chirality can be determined

Soft Matter Self-Assembly

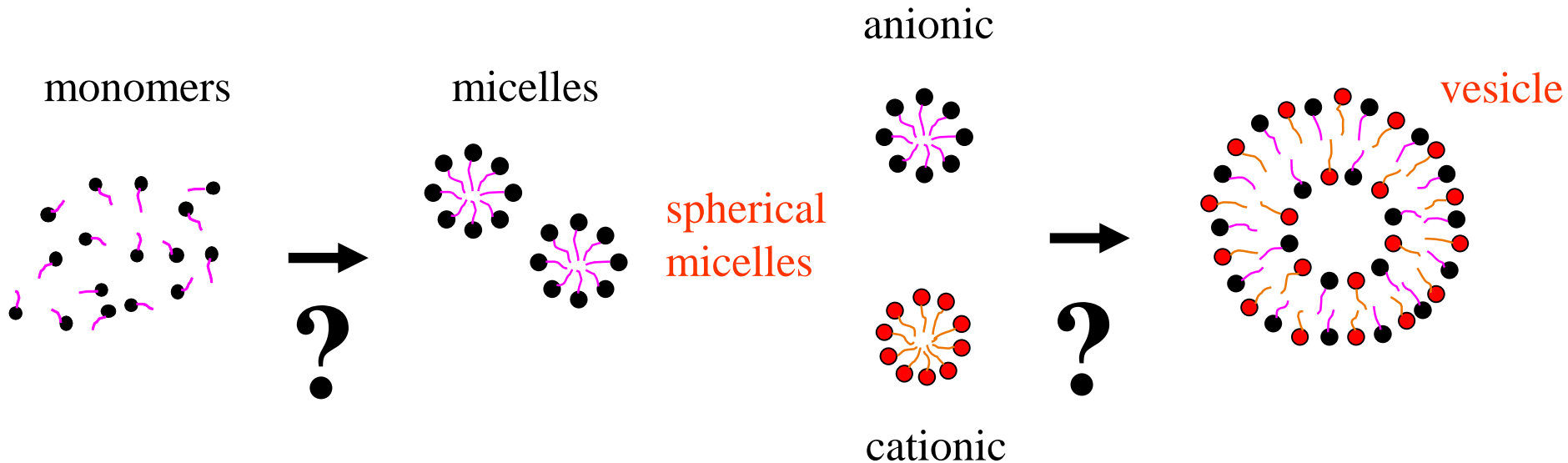
Spontaneous self-assembly of micelles and vesicles

E.g. surfactants, lipids or block copolymers

Large variety of equilibrium structures

Dynamics of formation is very little explored

Self-assembly of micelles and vesicles



Rate-limiting steps » predictive capability

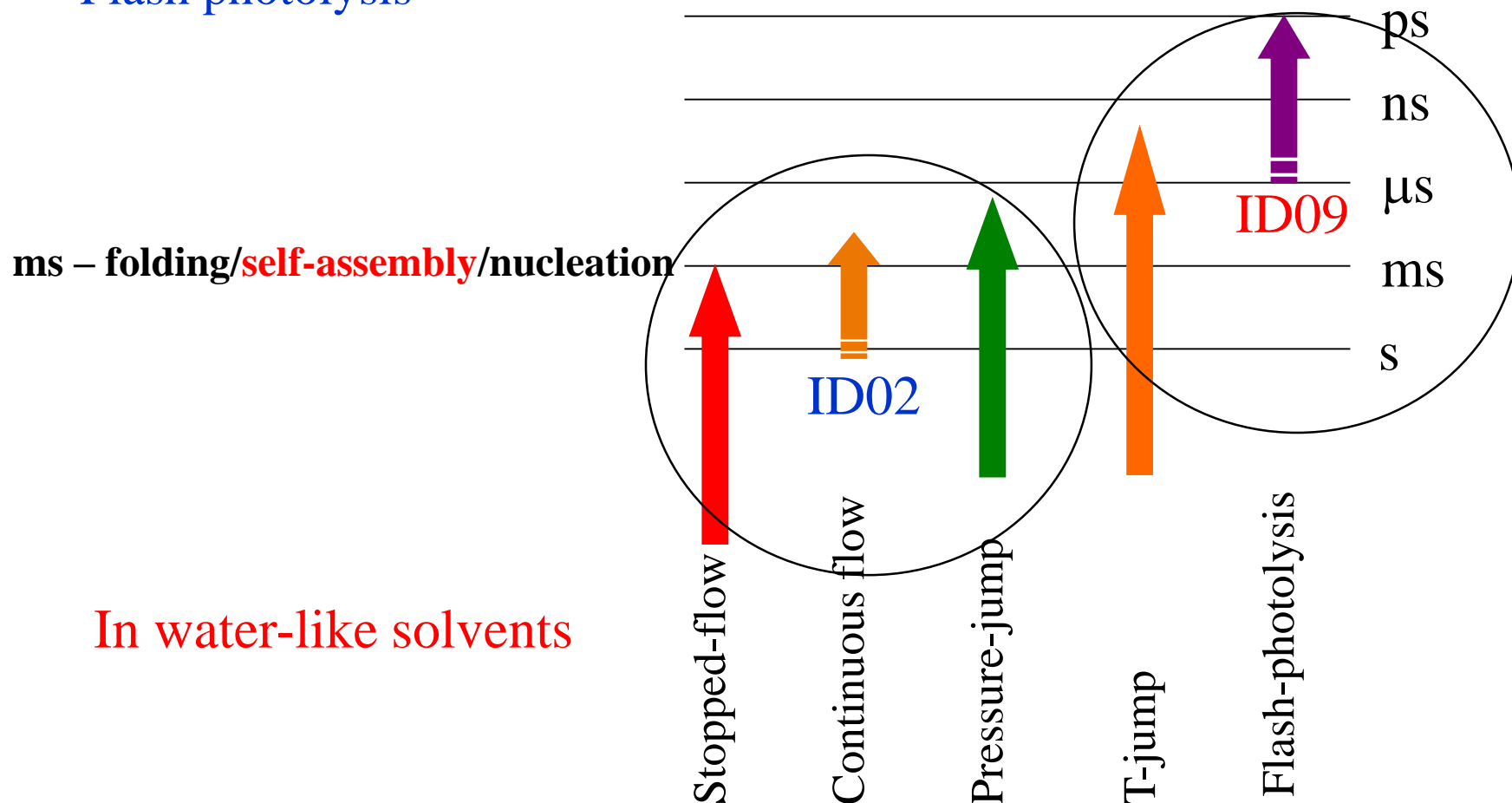
Kinetic pathway: stopped-flow rapid mixing & time-resolved SAXS

Triggering & Synchronization of Dynamic Processes

E.g. concentration/pH jump (rapid mixing)

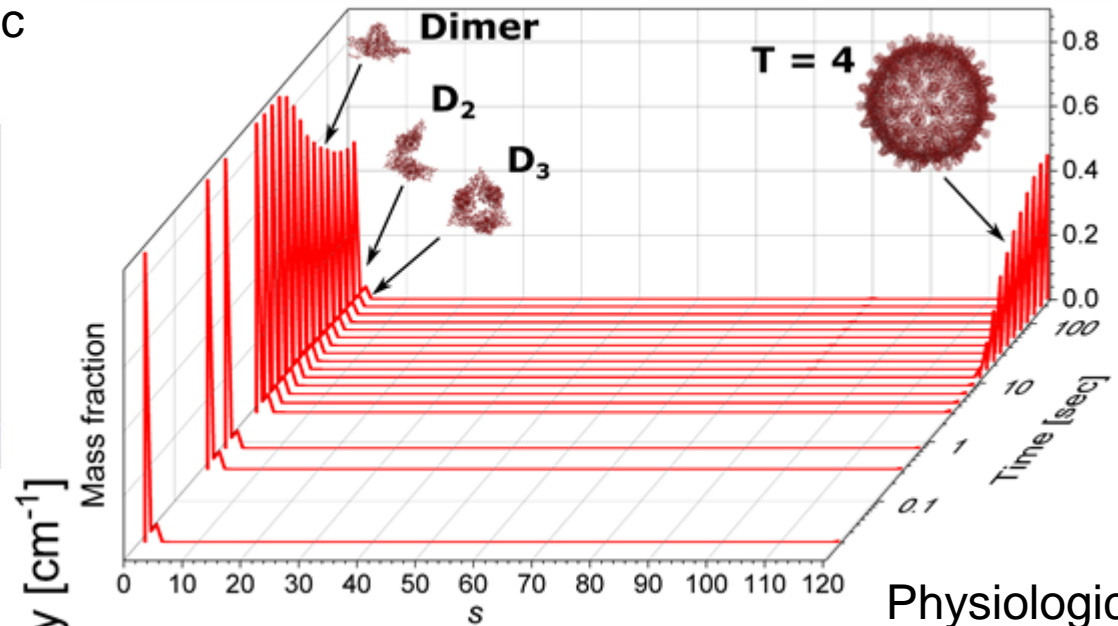
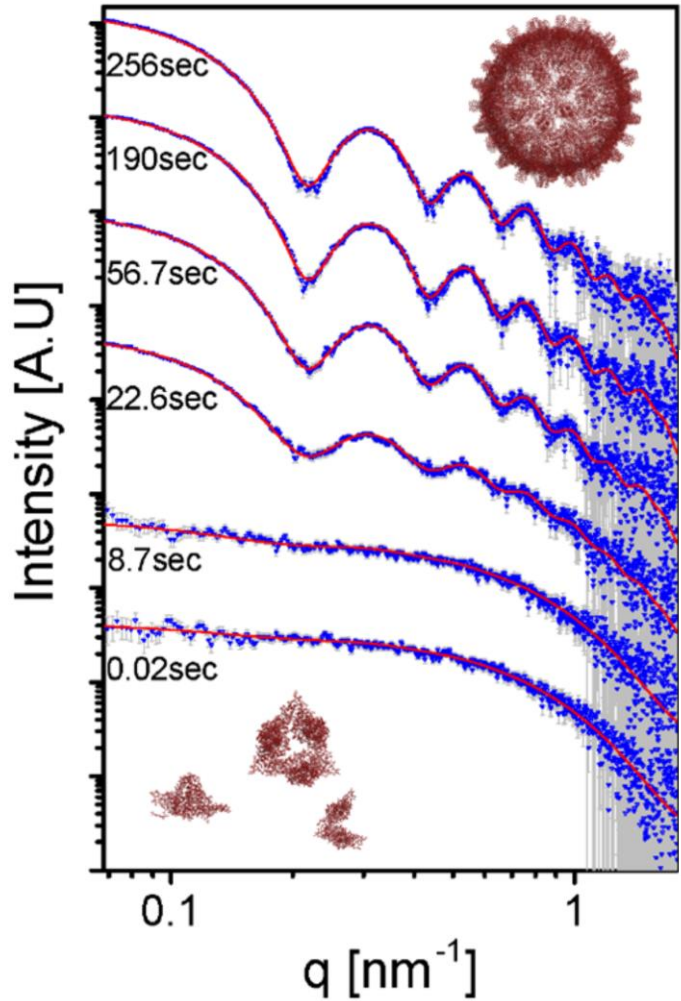
Rapid temperature or pressure change

Flash photolysis

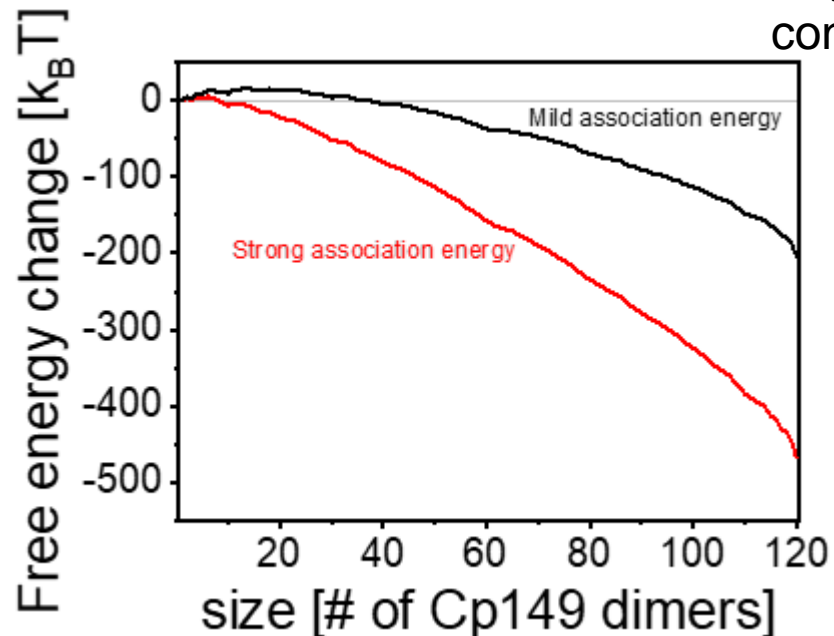


Pathways of Hepatitis B Virus Capsid Assembly

Simultaneous change of ionic strength and temperature



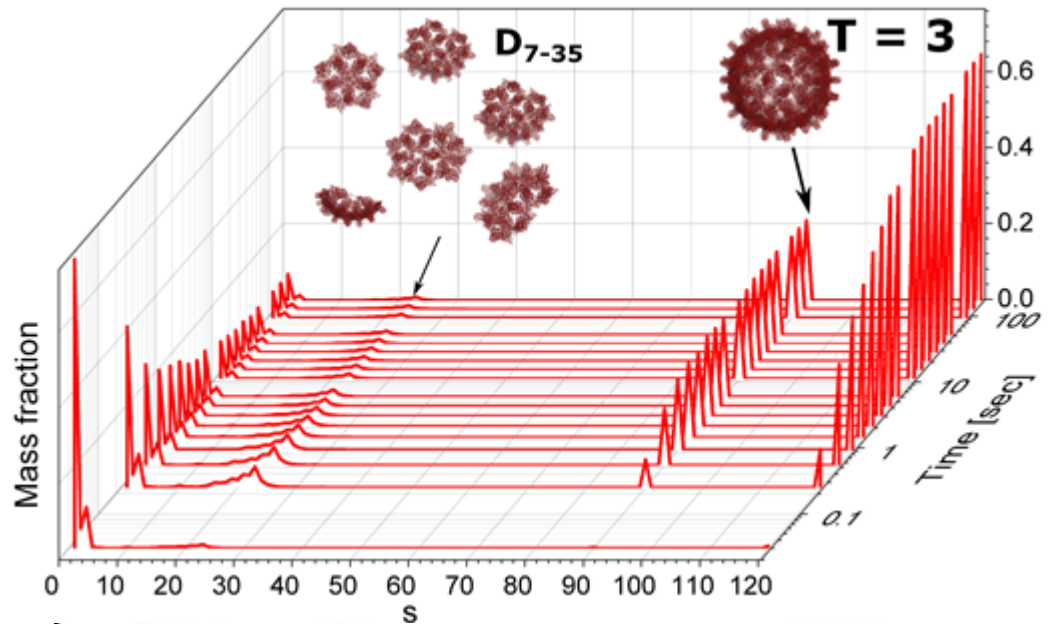
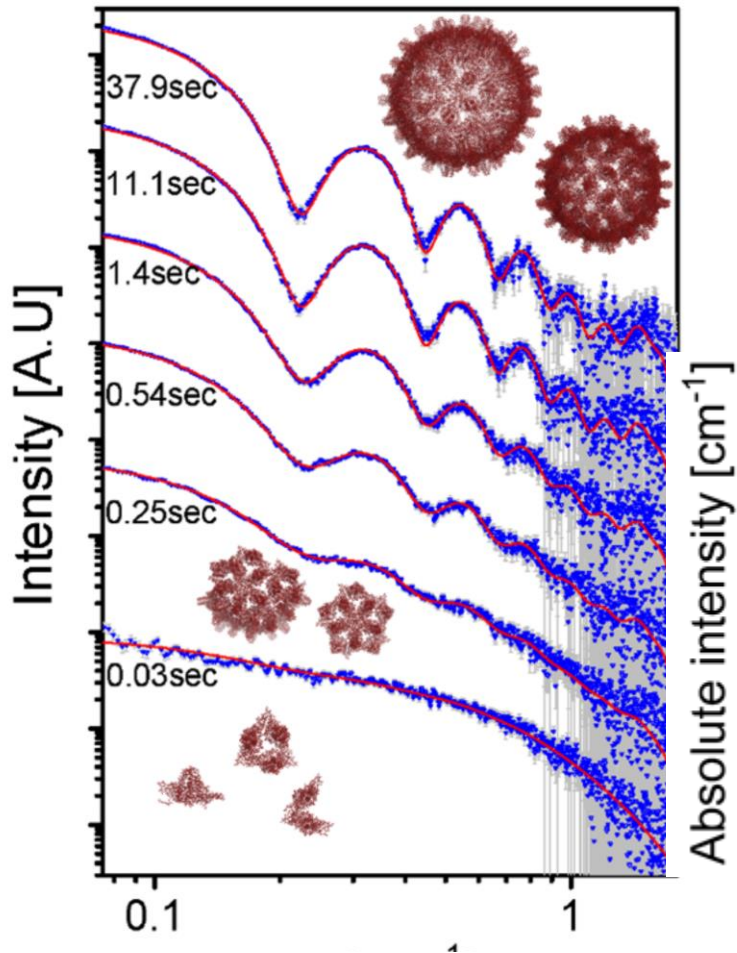
Physiological conditions



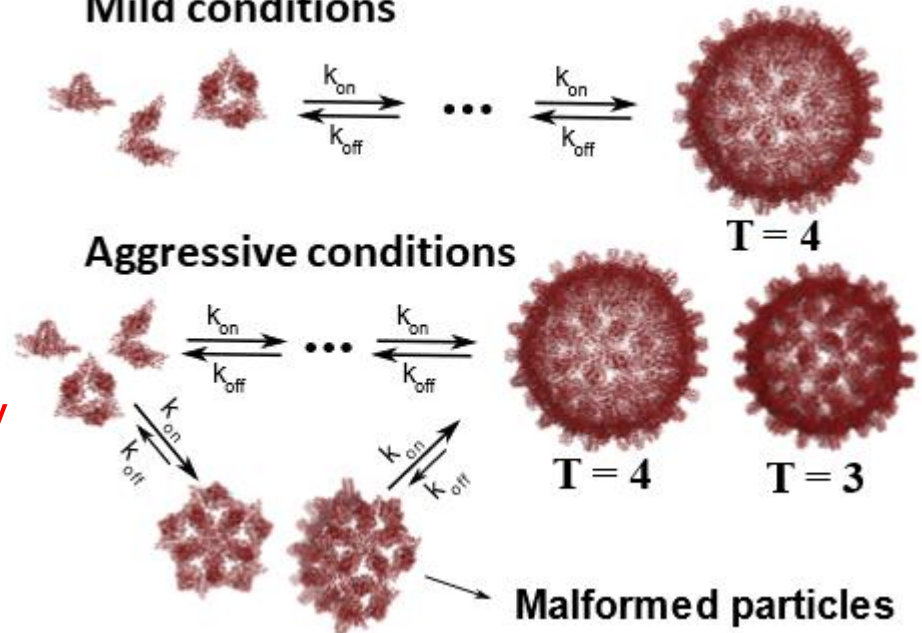
R. Asor *et al.*, JACS, 142, 7868 (2020)

Pathways of Hepatitis B Virus Capsid Assembly

Aggressive conditions

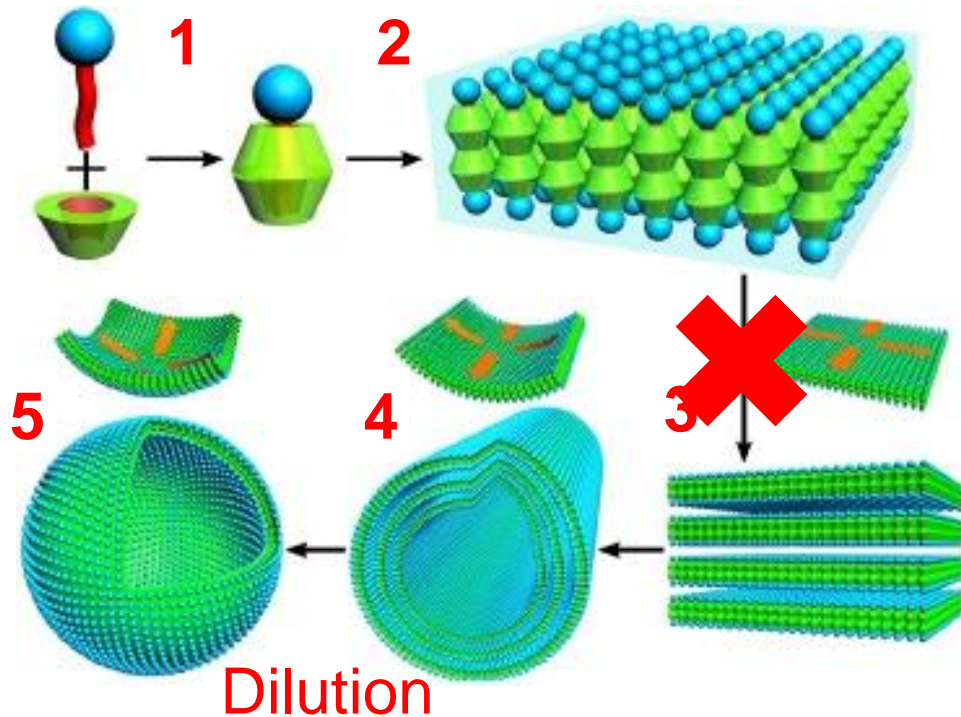


Mild conditions



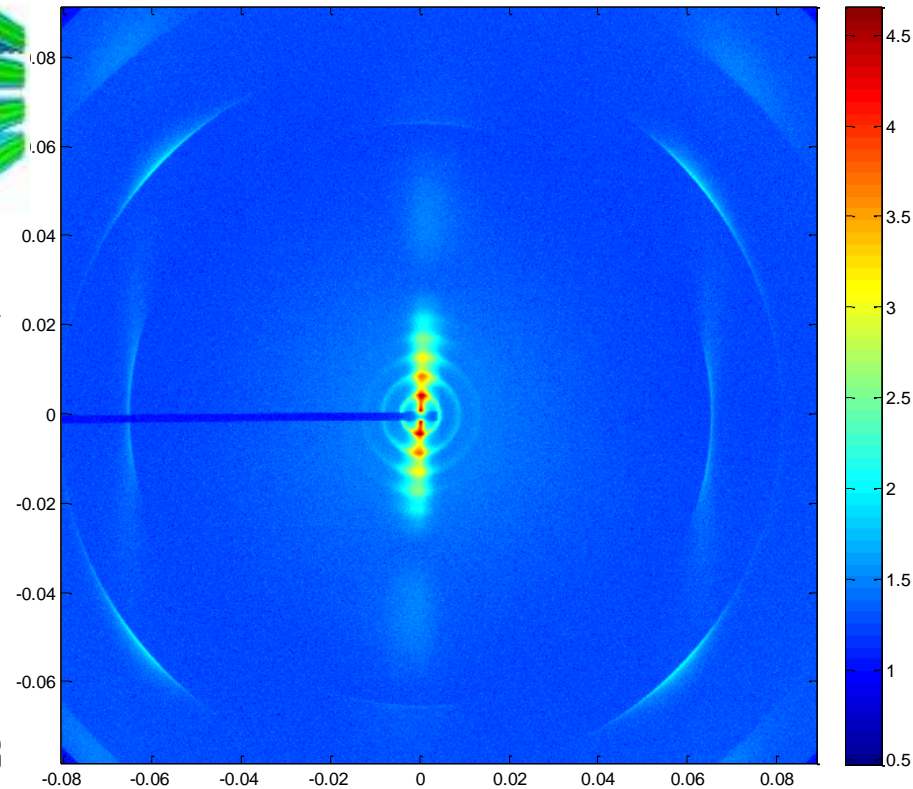
Dimer-dimer association free energy controls the earliest steps of the reaction, which dictates the subsequent assembly pathway

Multi-step hierarchical self-assembly of microtubules



Simple ingredients, a prototypical surfactant (SDS) and a naturally abundant polysaccharide (β -cyclodextrin) in water forming complex hierarchical structures.

$2\beta\text{-CD} + \text{SDS} @ 75\text{ }^\circ\text{C} \rightarrow 25\text{ }^\circ\text{C}$



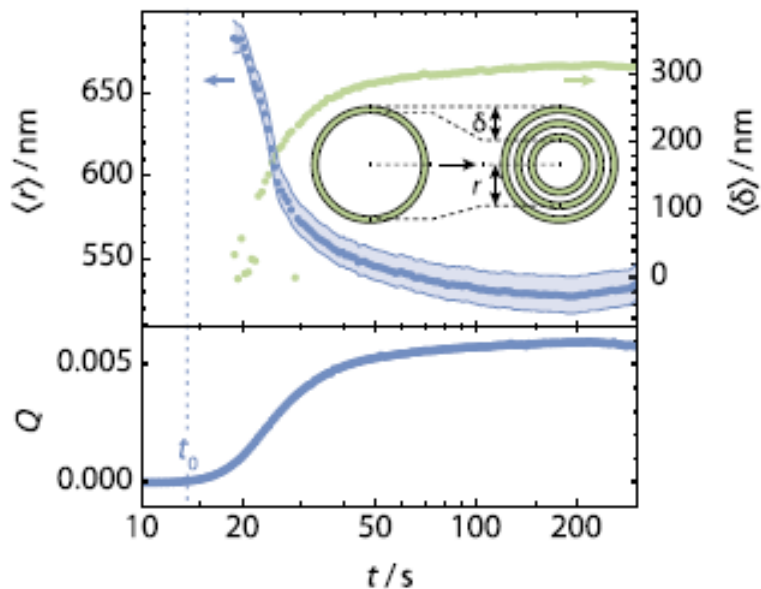
L. Jiang et al., *Soft Matter* (2011)

Spectacular self-assembly spanning size scales of 3 orders leading to formation of microtubules with a diameter of about $1.2\text{ }\mu\text{m}$

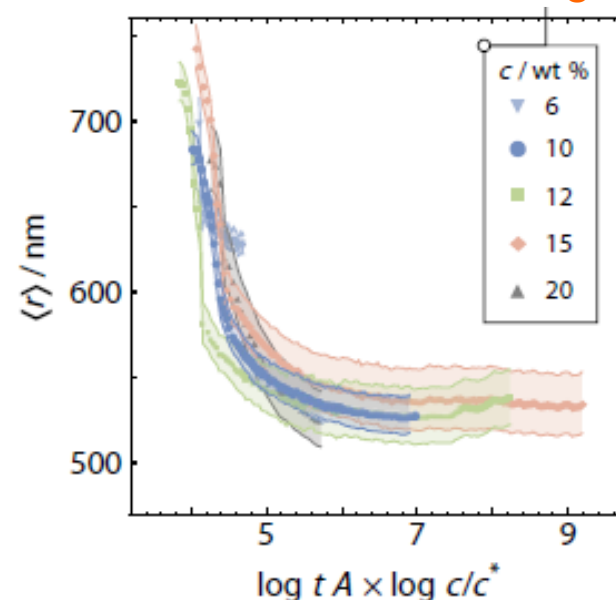
J. Landman *et al.*, *Science Advances* (2011)

Nucleation and Growth Mechanism

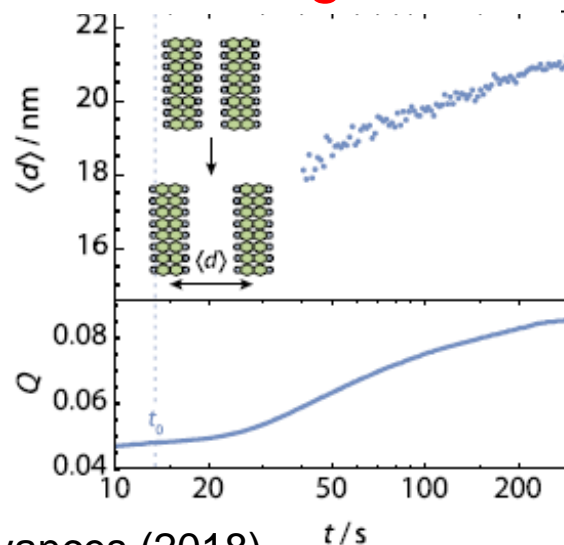
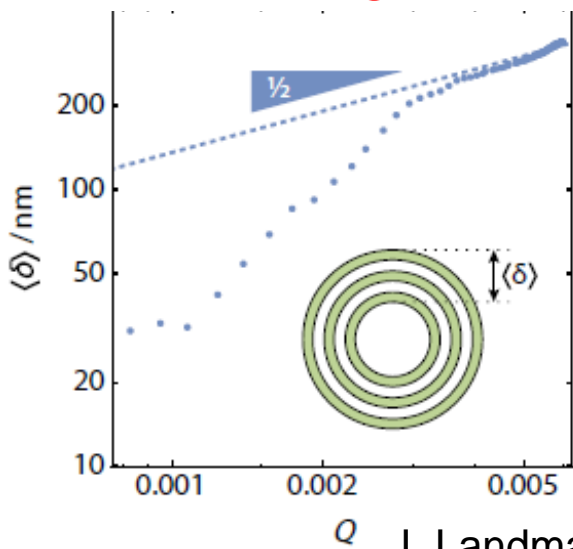
Central radius & wall thickness



Concentration scaling

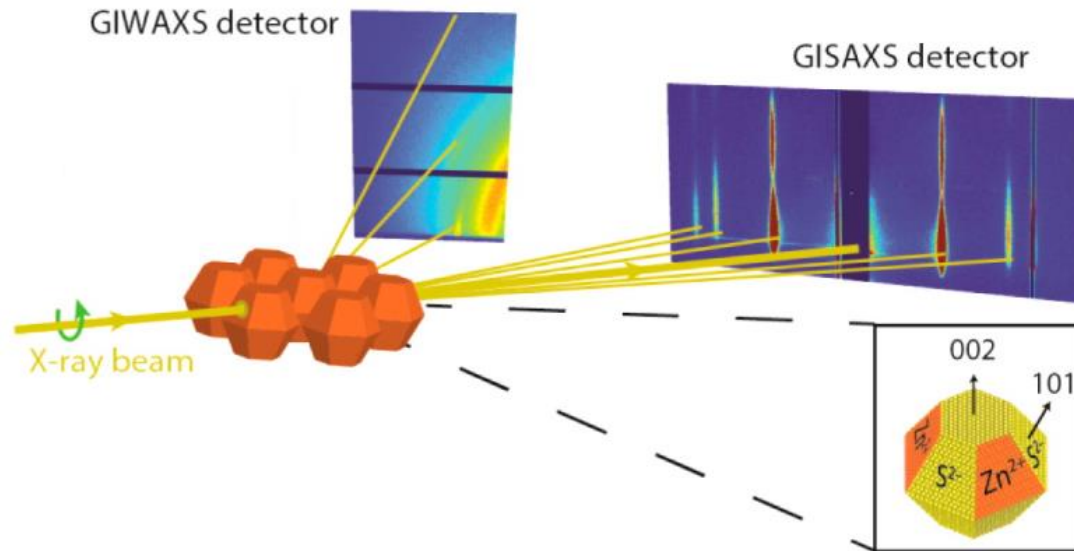


Inward growth of tubes by nucleation & growth

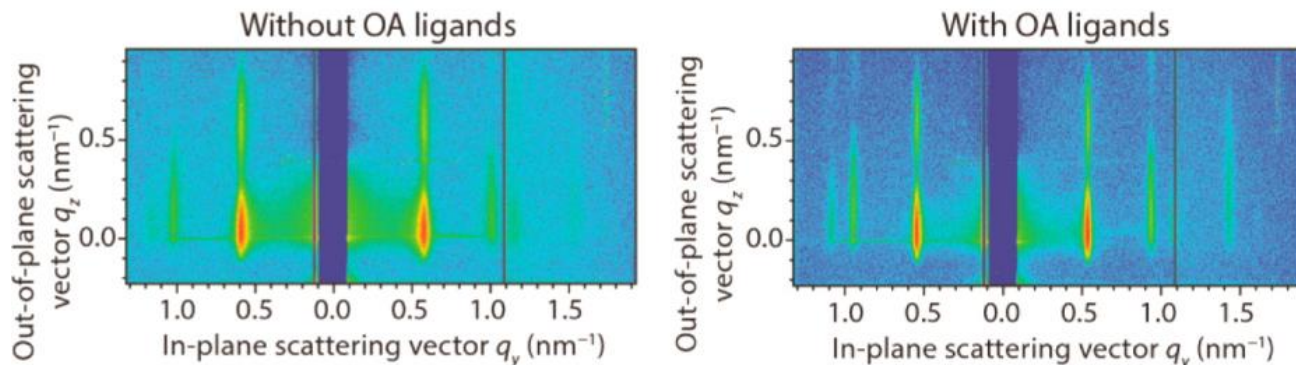


Soft matter self-assembly at interfaces

2D ZnS nanocrystal superlattice structure development at the vapour-liquid interface



W. van der Stam, Nano Lett. 16, 2608 (2016)



Oleic Acid (OA) ligands which induce atomic scale alignment of nanocrystals and promote superlattice formation

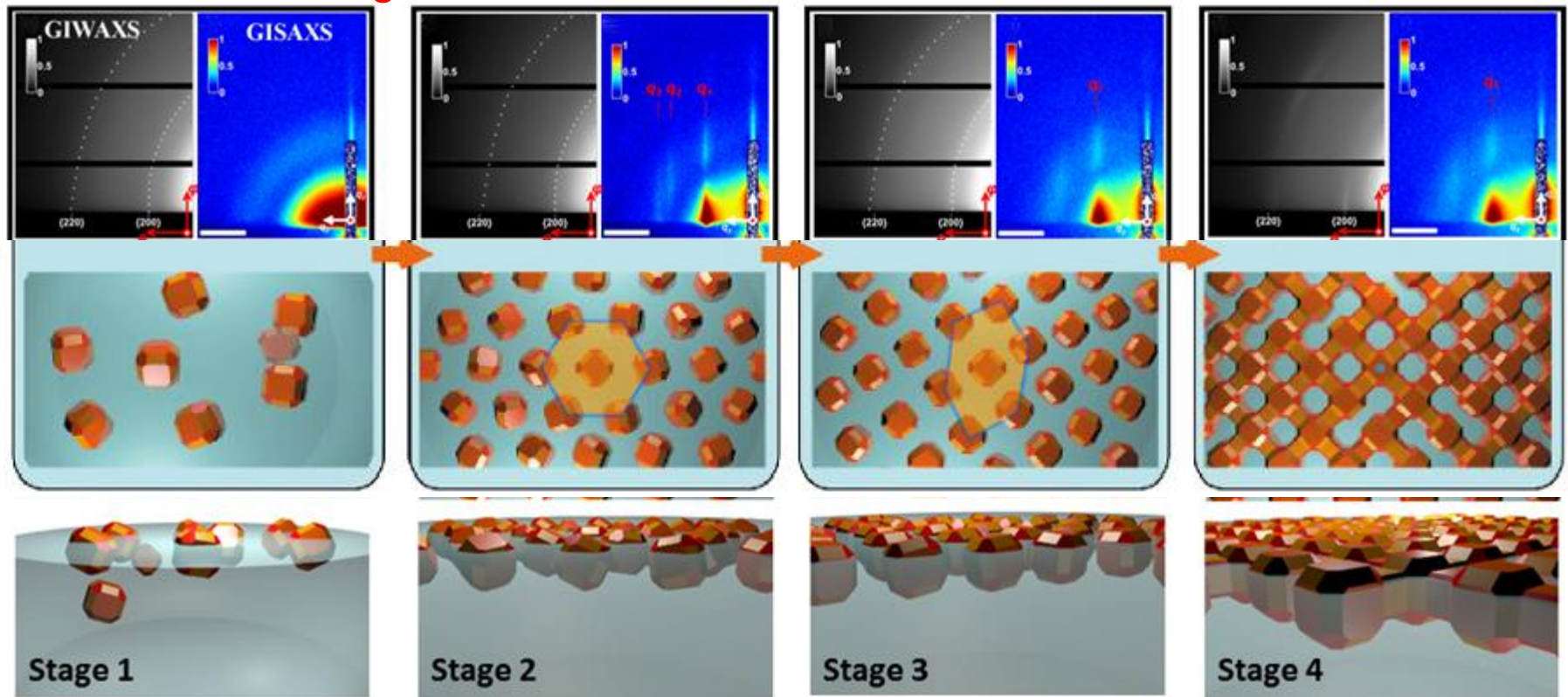
Self-Assembly of 2D Superlattices

Formation mechanism of two-dimensional superlattices from PbSe nanocrystals at vapour/liquid interface

WAXS: Orientation/domain size

J.J. Geuchies, *et al.*, Nature Materials (2016)

SAXS: Lateral organization



Hexagonal array

Deformed array

Square lattice

Crystalline bridges between the nanocrystals

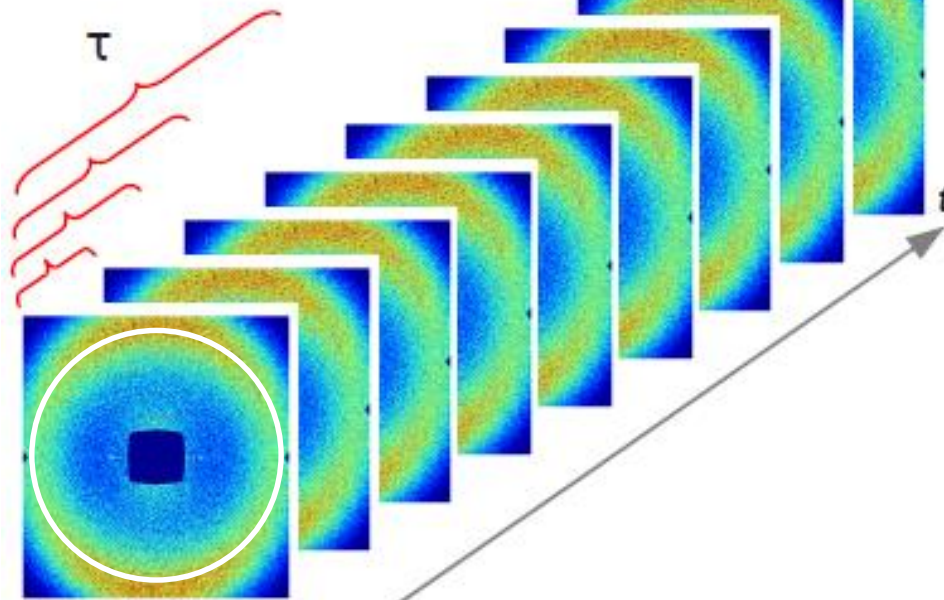
Out-of-equilibrium dynamics

Soft Matter: Out-of-equilibrium Dynamics

Out-of-equilibrium dynamics of systems far away from equilibrium

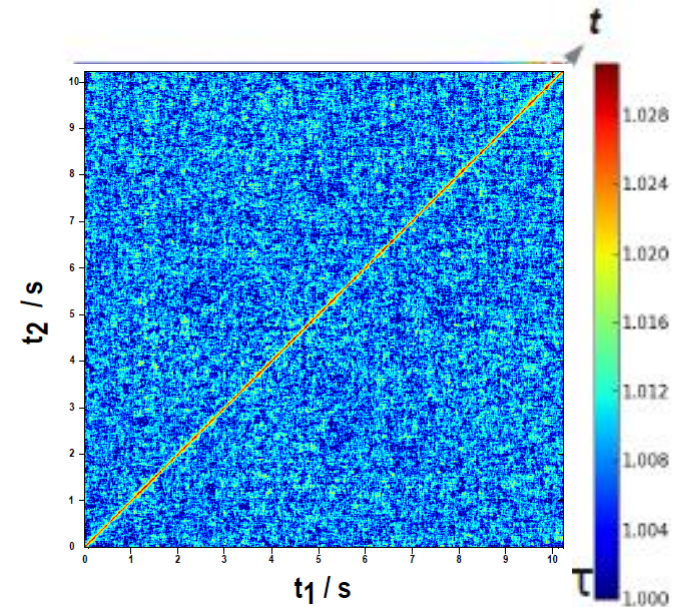
Multi-speckle XPCS

Series of scattering patterns

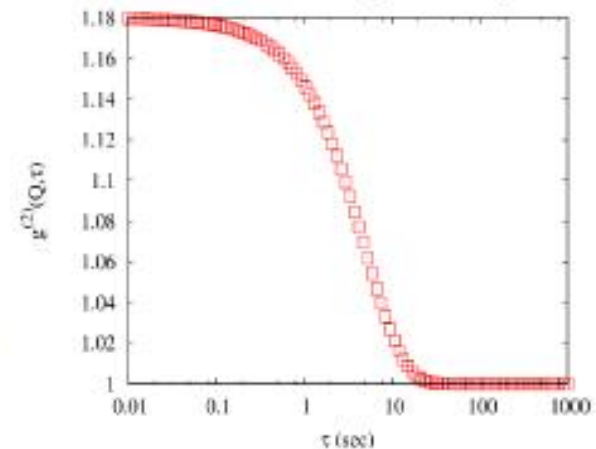


$$c_I(t, \tau) = \frac{\langle I_p(t) I_p(t + \tau) \rangle_p}{\langle I_p(t) \rangle_p \langle I_p(t + \tau) \rangle_p}$$

Time resolved correlation function



$$g^{(2)}(Q, \tau) = \langle c_I(t, \tau) \rangle_t$$



Complex Systems

Swarming

Self-replication

Cellular function

Emergence of complexity

Collective behavior

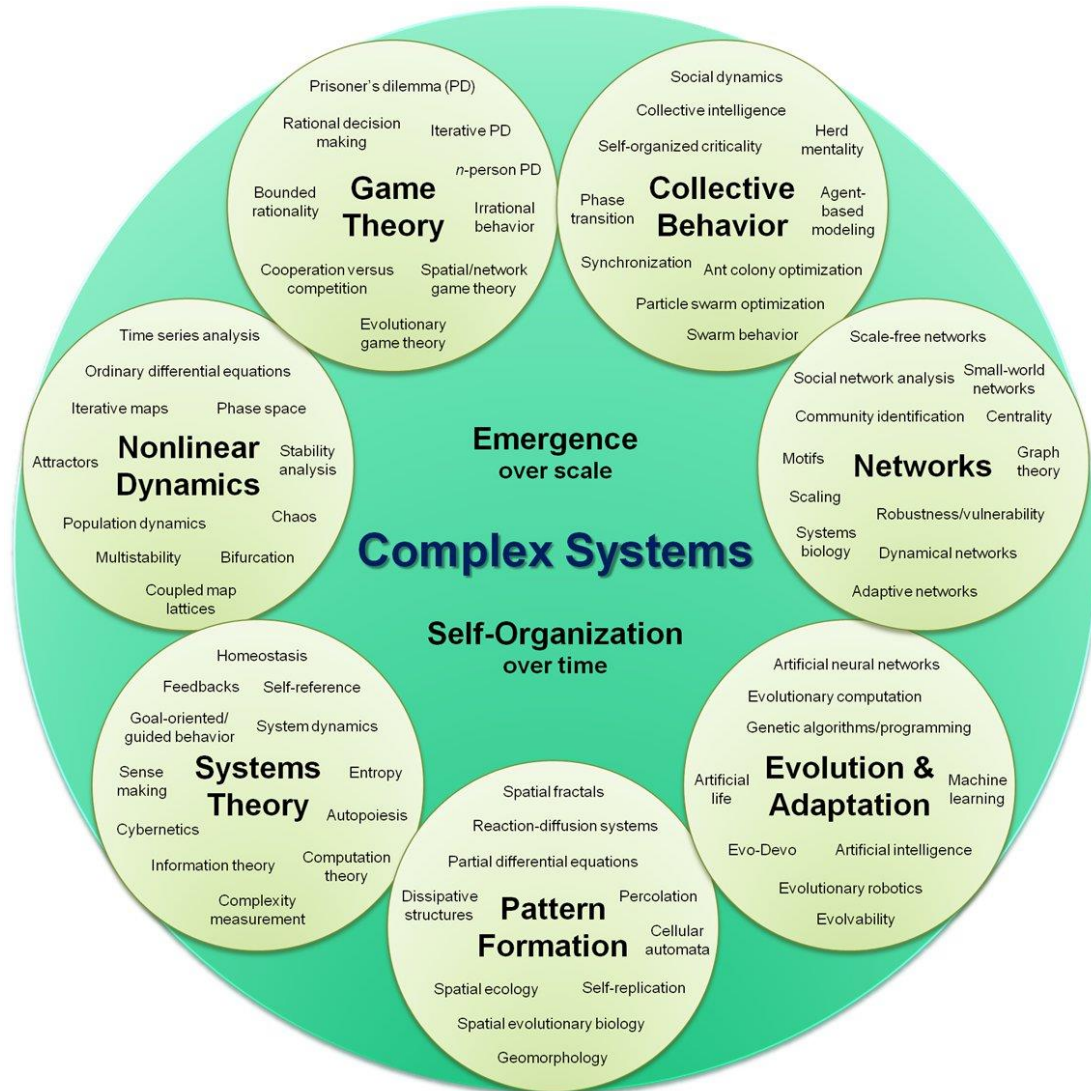
Self-organization

Active matter:

Physics of life

E.g. statistical mechanics

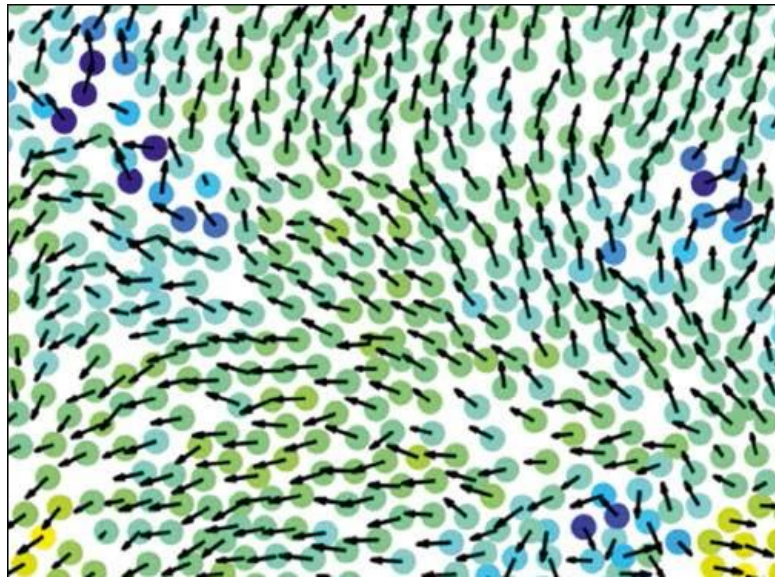
of virus capsid assembly



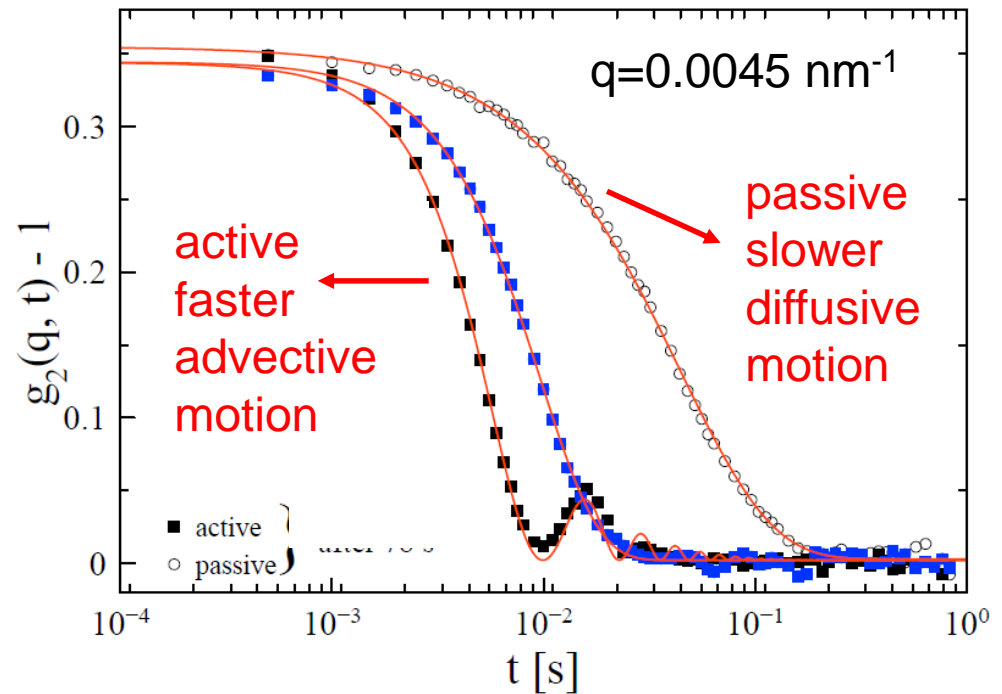
Soft Matter: Towards Macroscopic World

Connecting molecular world to macroscopic world – Active Matter

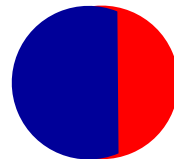
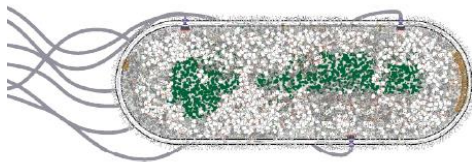
Self-propelled systems



Passive and active dynamics



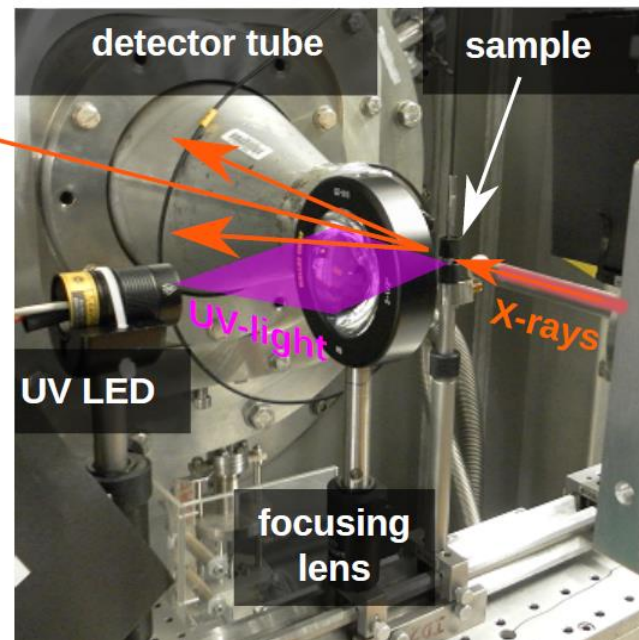
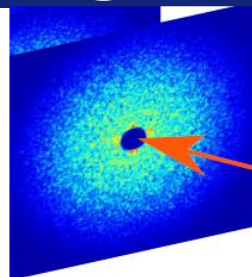
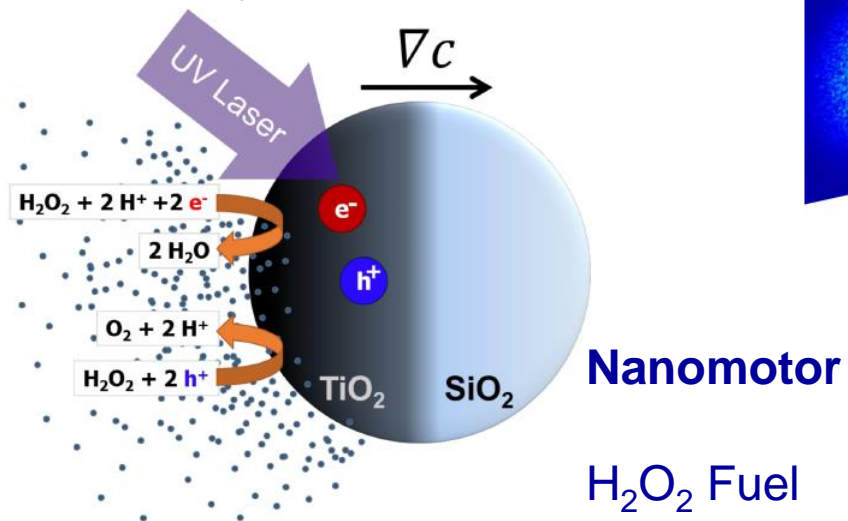
Micro-swimmers (microorganisms & Janus particles)



Super diffusive dynamics at large length scales

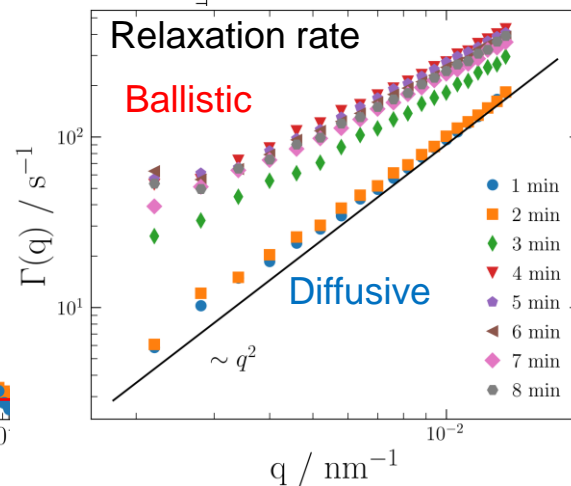
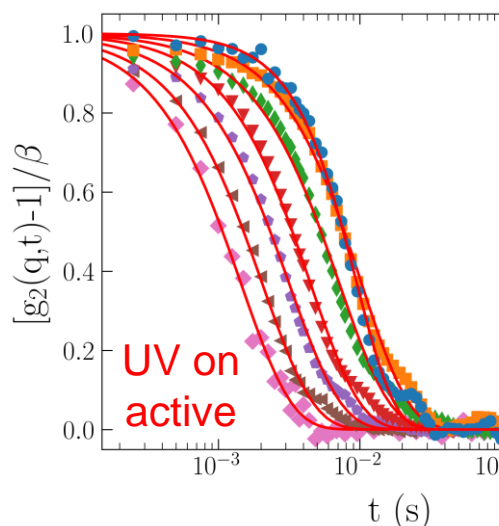
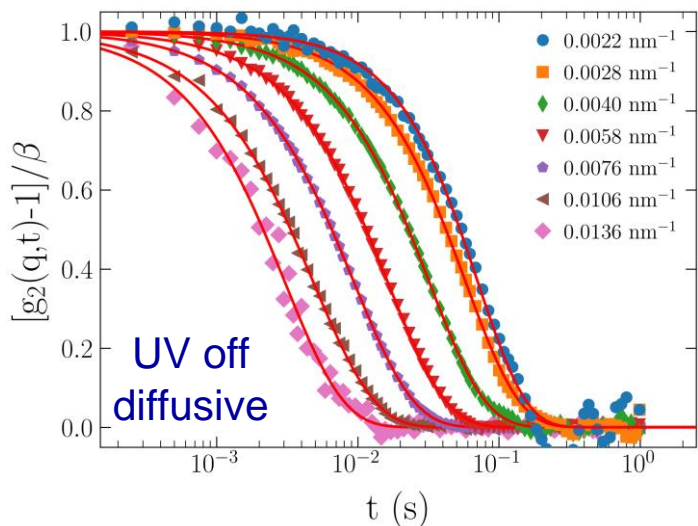
XPCS Study of Emergent Active Dynamics

Photo-catalytic Janus particles



Self-propulsion & associated dynamics

Evolution of the dynamics



Summary & Outlook

- High brilliance X-ray scattering is a powerful method to elucidate the non-equilibrium structure & dynamics of soft matter.
- Time-resolved scattering experiments in the sub-millisecond range can be performed even with dilute samples.
- **Combination of nanoscale spatial and millisecond time resolution makes synchrotron techniques unique in these studies.**
- Experiments can be performed in the functional state of the system.
- Challenges lie in the ability to investigate multicomponent systems and radiation sensitive specimen.
- The emphasis has become on quantitative studies of highly complex systems by exploiting the coherence properties of extremely bright synchrotron sources. In particular to problems related to the Physics of Life.