

Inelastic Neutron Scattering

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Outline

- ▶ Interaction neutron – matter
- ▶ Collective dynamics: Dispersion
- ▶ Collective dynamics: Intensities
- ▶ More than phonons and spin waves
- ▶ Even on powder

Master equation for neutron scattering

- ▶ weak interaction → **single** scattering process
- ▶ **1st order perturbation - 1st Born approximation - Fermi's golden rule**
- ▶ incoming/scattered **neutron plane wave**
- ▶ energies far away from nuclear resonances

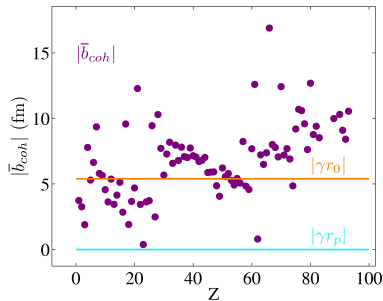
$$\frac{d^2\sigma}{d\Omega dE_f} \Big|_{n_0, \sigma_i \rightarrow n_1, \sigma_f} = \frac{k_f}{k_i} \left(\frac{m}{2\pi\hbar^2} \right)^2 \left| \langle \mathbf{k}_f \sigma_f n_1 | V | \mathbf{k}_i \sigma_i n_0 \rangle \right|^2 \cdot \delta(\epsilon_1 - \epsilon_0 - \underbrace{(E_i - E_f)}_{\hbar\omega})$$

Interactions of neutrons with matter V

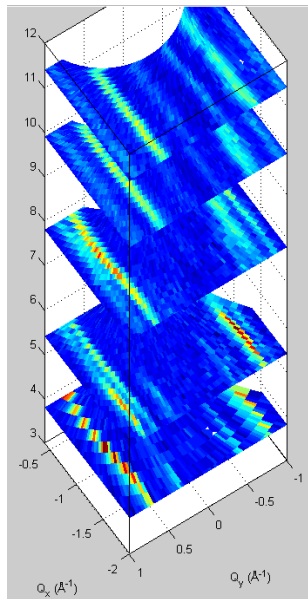
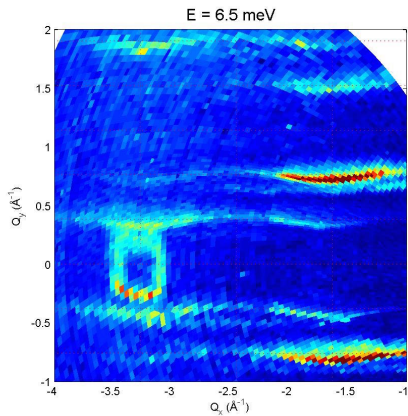
- n – atomic nucleus strong interaction
- n – electronic magn. moment dipole-dipole interaction
- n – electric field spin-orbit + Foldy interaction

average (absolute)
scattering length

nucleus	+6.5	fm	
el. magn. mom.	-5.4	fm	$(\cdot S(J))$
electric field	+1.5	am	



Magnetic and lattice excitations: comparable intensity



Nuclear interaction potential

Fermi pseudopotential V_N for neutron scattering from one nucleus

$$V_N(\mathbf{r}) = \frac{2\pi\hbar^2}{m} \bar{b} \delta(\mathbf{r} - \mathbf{R}_j)$$

Coherent scattering length \bar{b} : average over nuclear spin states and isotopes of an element.

entire sample:
$$V_N(\mathbf{r}) = \frac{2\pi\hbar^2}{m} \sum_{j=1}^{10^{23}} \bar{b}_j \delta(\mathbf{r} - \mathbf{R}_j) = \frac{2\pi\hbar^2}{m} N(\mathbf{r})$$

Magnetic interaction potential

magnetic potential V_M for neutron scattering from one electron

$$V_M(\mathbf{r}) = -\boldsymbol{\mu}_n \cdot \mathbf{B}_e$$

$$V_M(\mathbf{r}) = -\boldsymbol{\mu}_n \cdot \nabla \times \mathbf{A}$$

vector potential \mathbf{A}

$$V_M(\mathbf{r}) = -\boldsymbol{\mu}_n \cdot \nabla \times \left(\underbrace{\nabla \times \frac{\boldsymbol{\mu}_e^S}{r}}_{\text{spin}} + \underbrace{\nabla \times \frac{\boldsymbol{\mu}_e^L}{r}}_{\text{orbital current}} \right)$$

Magnetic matrix element - Fourier transform

one electron

$$\begin{aligned} & \langle \mathbf{k}_i \sigma_i n_0 | -\boldsymbol{\mu}_n \cdot \nabla \times \left(\nabla \times \frac{\boldsymbol{\mu}_e^{tot}}{r} \right) | \mathbf{k}_f \sigma_f n_1 \rangle \\ &= \langle \sigma_i n_0 | -\boldsymbol{\mu}_n \cdot \underbrace{\left(\hat{\mathbf{Q}} \times (\hat{\mathbf{Q}} \times \boldsymbol{\mu}_e^{tot}(\mathbf{Q})) \right)} | \sigma_f n_1 \rangle \\ &= \langle \sigma_i n_0 | -\boldsymbol{\mu}_n \cdot \boldsymbol{\mu}_{e\perp}^{tot}(\mathbf{Q}) | \sigma_f n_1 \rangle \end{aligned}$$

entire sample

$$\sum \tilde{\boldsymbol{\mu}}_{e\perp}^{tot}(\mathbf{Q}) = \mathbf{M}_{\perp}(\mathbf{Q})$$

Coherent and incoherent scattering

Coherent scattering

average scattering amplitude

equal objects periodically
arranged

interference
of different (identical) objects

Pair correlation

Incoherent scattering

standard deviation of the amplitude

unequal objects (periodically arranged)
– isotopes
– nuclear spin directions
– electronic spin directions

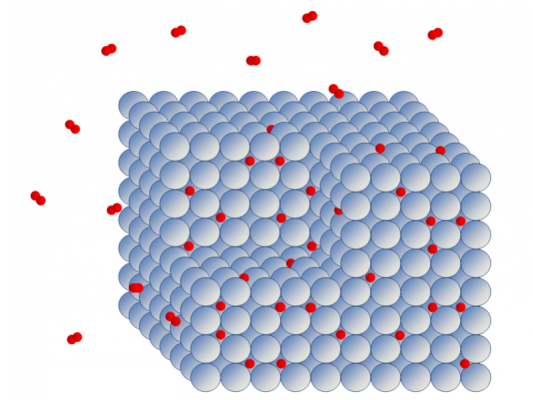
interference
of 1 object with itself

Autocorrelation

Diffuse motion in crystals

Disordered phenomena in crystals

- ▶ hydrogen diffusion
- ▶ spin diffusion, e.g. critical scattering near a phase transition



Signature of diffuse motion: Quasielastic scattering

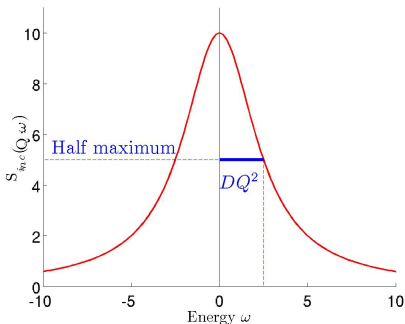
$$\left. \frac{d^2\sigma}{d\omega d\Omega} \right|_{\text{inc}} = \frac{\sigma_{\text{inc}}}{4\pi} \frac{k_f}{k_i} N S_{\text{inc}}(\mathbf{Q}, \omega)$$

$$S_{\text{inc}}(\mathbf{Q}, \omega) = \frac{1}{2\pi\hbar} \int dt d\mathbf{r} e^{i(\mathbf{Q}\mathbf{r} - \omega t)} G_{\text{self}}(\mathbf{r}, t)$$

$$G_{\text{self}}(\mathbf{r}, t) = \frac{1}{N} \sum_j \int d\mathbf{r}' \langle \delta(\mathbf{r}' - \mathbf{R}_j(0)) \delta(\mathbf{r}' + \mathbf{r} - \mathbf{R}_j(t)) \rangle_T$$

Incoherent cross section \sim
autocorrelation

correlation of a particle/spin
at $\mathbf{r} = 0, t = 0$
with the same particle/spin
at \mathbf{r}, t



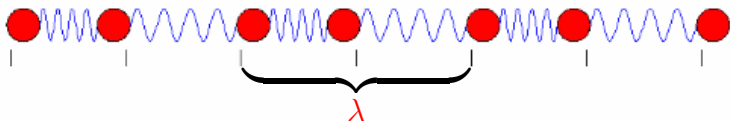
Instruments for Quasielastic scattering

Slow dynamics \Rightarrow high energy resolution

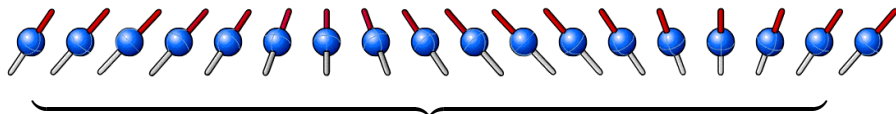
- ▶ cold Time Of Flight
- ▶ backscattering
- ▶ spin echo spectroscopy

Collective motion – coherent dynamics – "ballet"

phonons



magnons



wavelength λ

wave vector $Q = \frac{2\pi}{\lambda}$

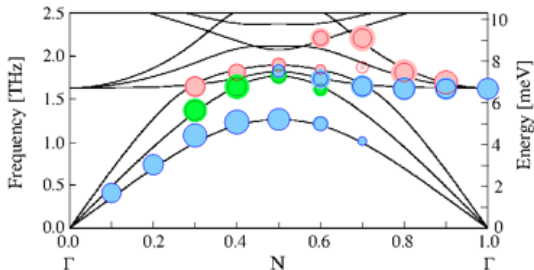
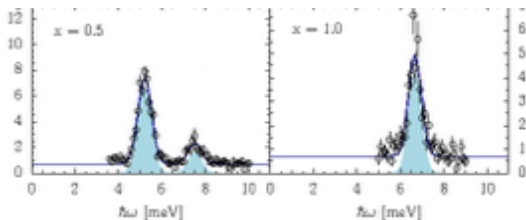
Collective dynamics: Signature dispersion

phonons (IN8)

- ▶ in periodic arrays/
crystals
- ▶ in liquids
(sound wave)

Dispersion:

discrete $\hbar\omega$
at each Q



M.M. Koza *et al.* PRB **91** 014305 (2015)

Collective motion – wave – interference pattern

Coherent cross section

$$\begin{aligned} \left. \frac{d^2\sigma}{d\Omega dE_f} \right|_{\text{coh}} &= \frac{k_f}{k_i} \left(\frac{m}{2\pi\hbar^2} \right)^2 \sum_{n_0, n_1} p(n_0) \left| \langle n_1 | V(\mathbf{Q}) | n_0 \rangle \right|^2 \delta(\varepsilon_1 - \varepsilon_0 - \hbar\omega) \\ &= \frac{k_f}{k_i} \left(\frac{m}{2\pi\hbar^2} \right)^2 \sum_{n_0} p(n_0) \underbrace{\frac{1}{2\pi\hbar} \int_{-\infty}^{\infty} dt e^{-i\omega t} \langle n_0 | V^*(\mathbf{Q}, 0) V(\mathbf{Q}, t) | n_0 \rangle}_{S(\mathbf{Q}, \omega)} \\ &= \frac{k_f}{k_i} S(\mathbf{Q}, \omega) \quad \text{coherent dynamic scattering function} \end{aligned}$$

Coherent dynamic scattering function

$$\begin{aligned} S_N(\mathbf{Q}, \omega) &= \sum_{n_0} p(n_0) \frac{1}{2\pi\hbar} \int dt e^{-i\omega t} \langle n_0 | N^*(\mathbf{Q}, 0) N(\mathbf{Q}, t) | n_0 \rangle \\ &= \frac{1}{2\pi\hbar} \int d\mathbf{r} dt e^{i(\mathbf{Q}\mathbf{r} - \omega t)} \langle N(\mathbf{0}, 0) N(\mathbf{r}, t) \rangle_T \end{aligned}$$

$$\begin{aligned} S_M(\mathbf{Q}, \omega) &= \sum_{n_0} p(n_0) \frac{(\gamma r_0)^2}{2\pi\hbar} \int dt e^{-i\omega t} \langle n_0 | \mathbf{M}_\perp^*(\mathbf{Q}, 0) \mathbf{M}_\perp(\mathbf{Q}, t) | n_0 \rangle \\ &= \frac{(\gamma r_0)^2}{2\pi\hbar} \int d\mathbf{r} dt e^{i(\mathbf{Q}\mathbf{r} - \omega t)} \langle \mathbf{M}_\perp(\mathbf{0}, 0) \cdot \mathbf{M}_\perp(\mathbf{r}, t) \rangle_T \end{aligned}$$

$S(\mathbf{Q}, \omega)$ is the space-time Fourier transform of the

nuclear-positional
magnetic

density-density pair correlation function

Coherent and incoherent scattering

Coherent cross section

~ **pair** correlation function:

→ **dispersion** relation

→ **structural pattern**

Incoherent cross section

~ **1-particle autocorrelation**:

→ **diffusion coefficient**

no structural information

Collective dynamics

atoms/magnetic moments
move "**correlated**" ("ballet")

Brownian motion

"random walk"
uncorrelated, diffuse motion

Snapshot:

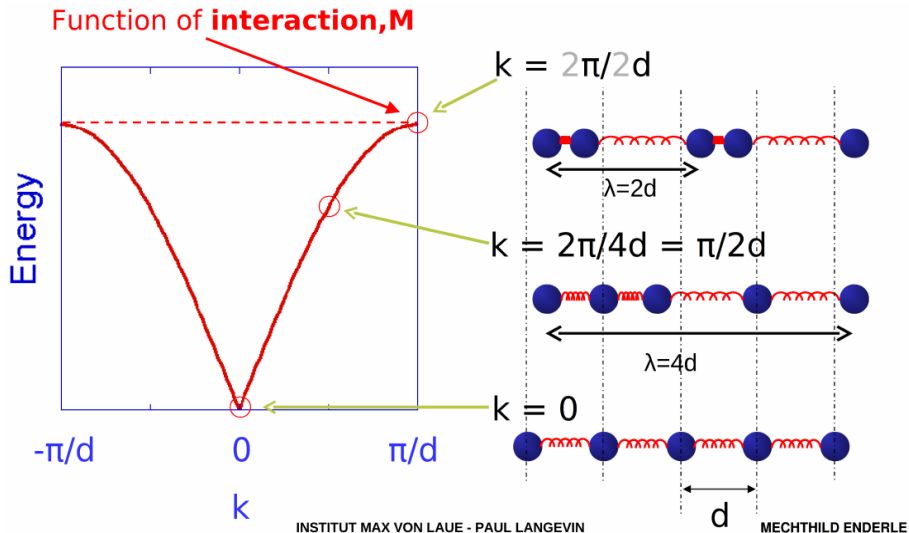
periodic pattern – wave

disordered

Collective dynamics in the **incoherent** cross section:

~ **density of states** $Z(\omega)$ – loss of all structural information

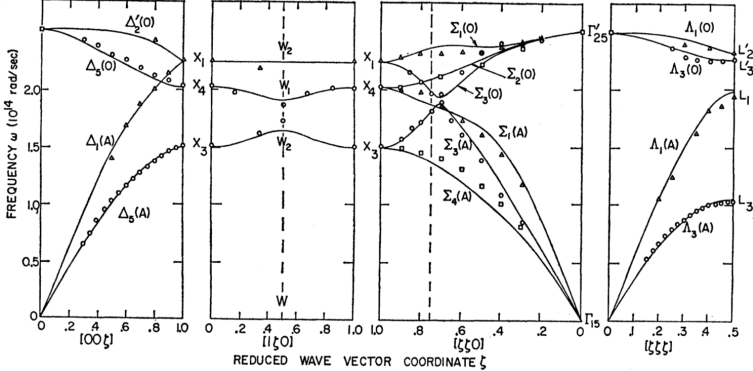
Collective excitations of the lattice: phonons



Phonons in diamond

diamond:  covalent bonds

1000 meV

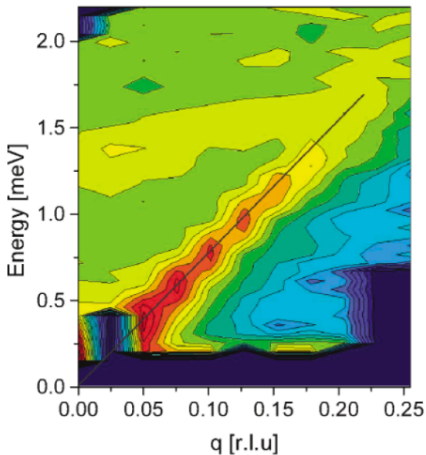


J.L. Warren *et al.* Phys.Rev. **158** 805 (1967)

Phonons in bcc ^4He

bcc ^4He  van der Waals (+quantum effects)

1 meV



$T = 1.6400(1)\text{K}$

IN12

M. Markovich *et al.* PRL **88** 195301 (2002)

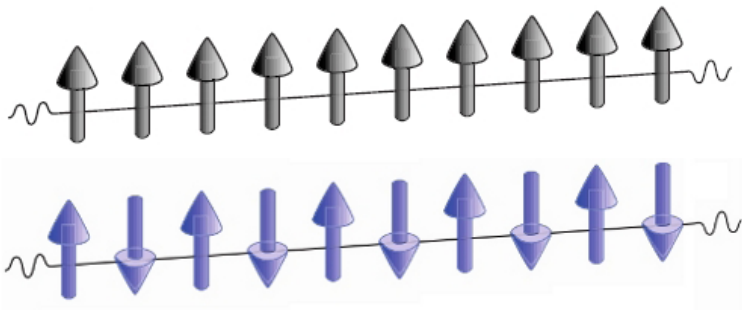
"Magnetic springs" - mostly super-exchange

may favor

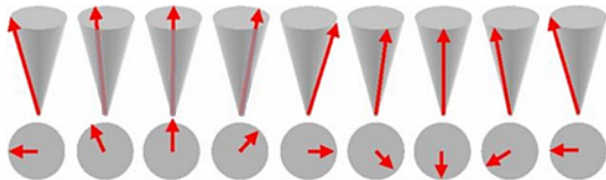
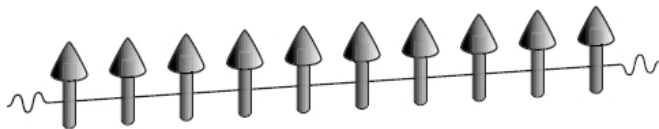
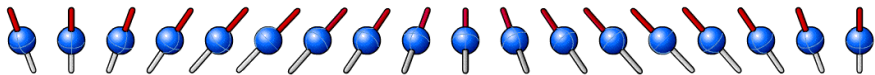
parallel
antiparallel

magnetic moments:

Ferromagnet
Antiferromagnet

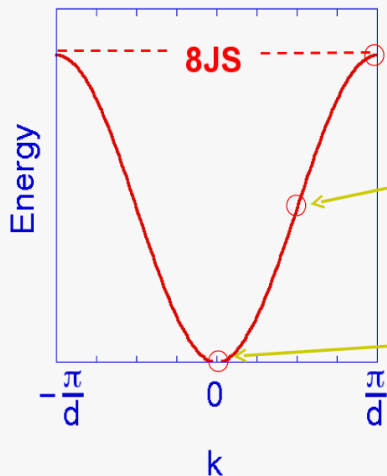


Spin waves in a ferromagnet



Collective excitations of the ferromagnet: magnons

$$\hbar\omega(q) = 4SJ [1 - \cos(qa)]$$



$$k = \pi/d$$



$$k = \pi/2d$$

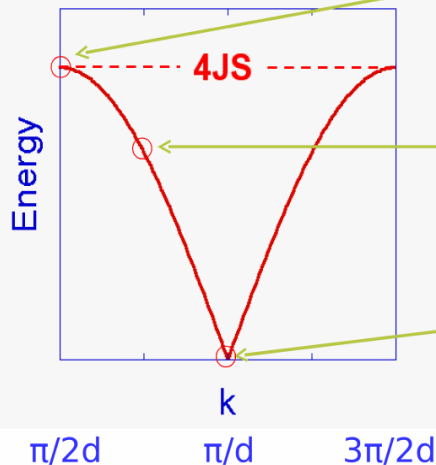


$$k = 0$$



Magnons in the "classical" antiferromagnet

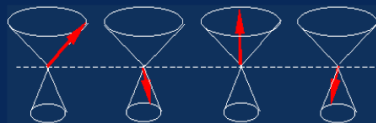
$$\hbar\omega(q) = 4S |J| |\sin(qa)|$$



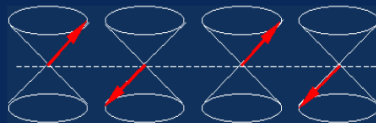
$$k = \pi/2d$$



$$k = 3\pi/4d$$

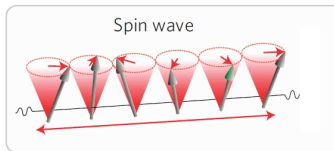
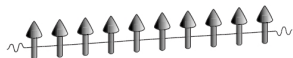


$$k = \pi/d$$

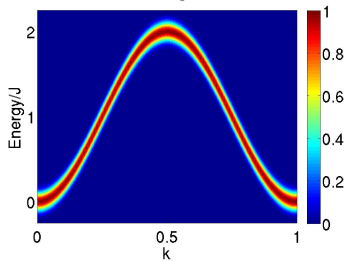


Magnon dispersion reveals microscopic interactions

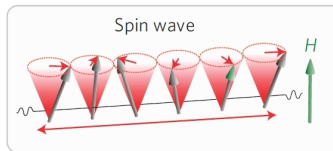
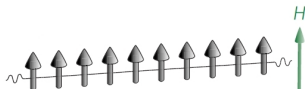
Ferromagnet



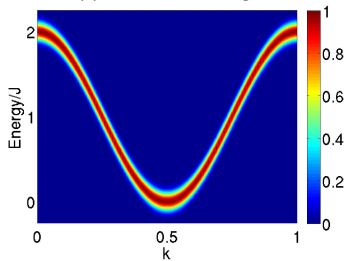
ferromagnet



Saturated antiferromagnet $H > H_{\text{sat}}$



fully polarized antiferromagnet



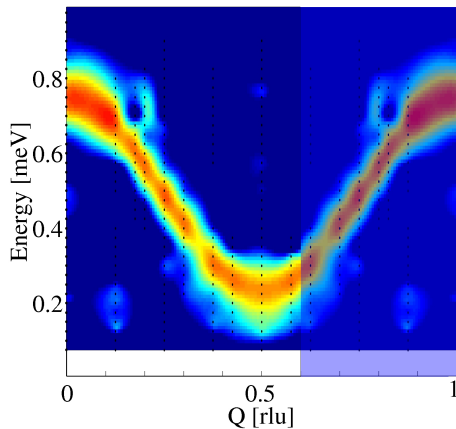
Magnon dispersion reveals microscopic interactions

$\text{CuSO}_4 \cdot 5\text{D}_2\text{O}$



$H > H_{\text{sat}}$

no long range order $> 0.1\text{K}$



↑
antiferromagnetic exchange

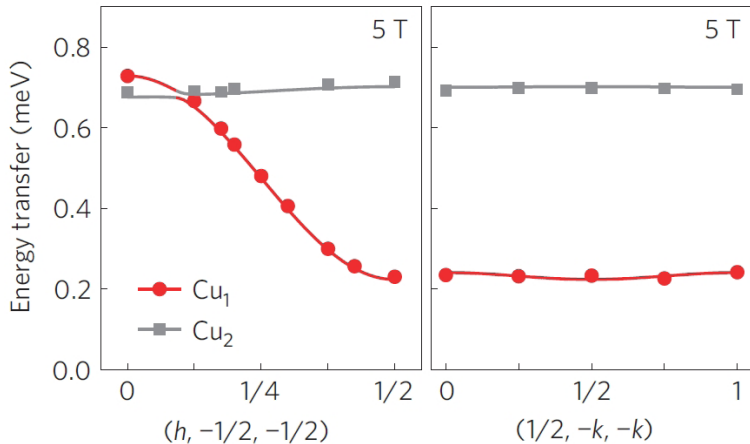
Magnon dispersion reveals microscopic interactions

CuSO₄.5D₂O

fully saturated

$H > H_{\text{sat}}$

magnetic springs only in one direction



magnetically 1D!

M. Mourigal, M.E. *et al.* Nat. Phys. **9** 435 (2013)

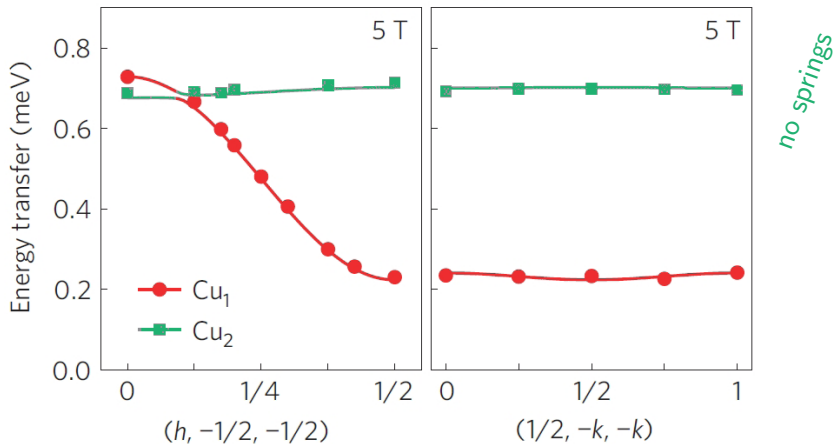
Magnon dispersion reveals microscopic interactions

CuSO₄.5D₂O

fully saturated

$H > H_{\text{sat}}$

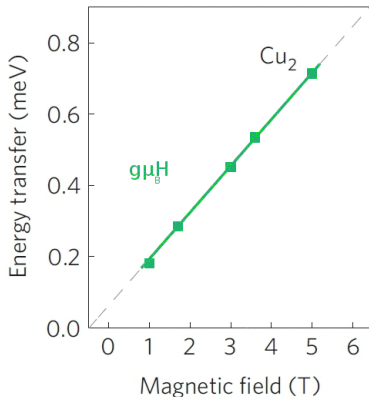
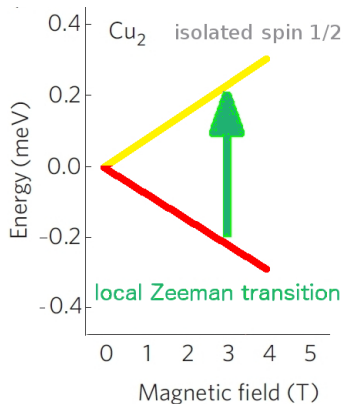
no springs/ no interaction: local transition



Energy independent of Q for all directions of Q

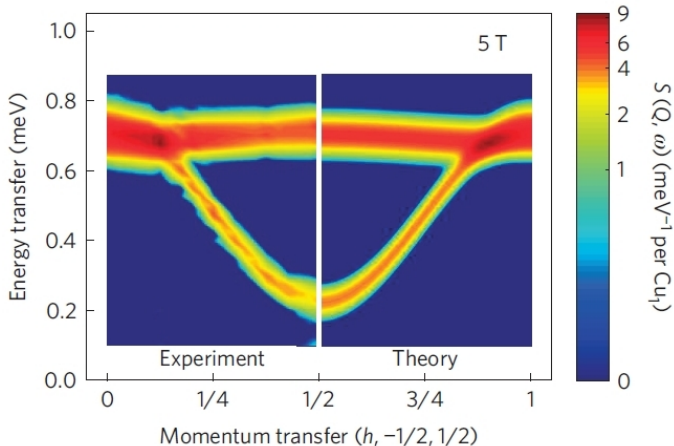
Local spin flip between Zeeman-split states

$\text{CuSO}_4 \cdot 5\text{D}_2\text{O}$



M. Mourigal, M.E. *et al.* Nat. Phys. **9** 435 (2013).

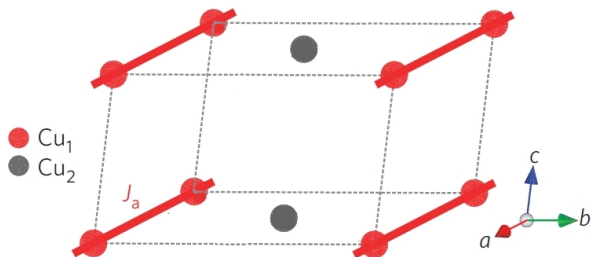
Fully saturated $\text{CuSO}_4 \cdot 5\text{D}_2\text{O}$



M. Mourigal, M.E. *et al.* Nat. Phys. **9** 435 (2013).

Spin waves in fully saturated $\text{CuSO}_4 \cdot 5\text{D}_2\text{O}$

→ microscopic scheme of magnetic interactions



Cu_1 : one-dimensional arrays with antiferromagnetic interaction

Cu_2 : not coupled by any interaction

M. Mourigal, M.E. *et al.* Nat. Phys. **9** 435 (2013).

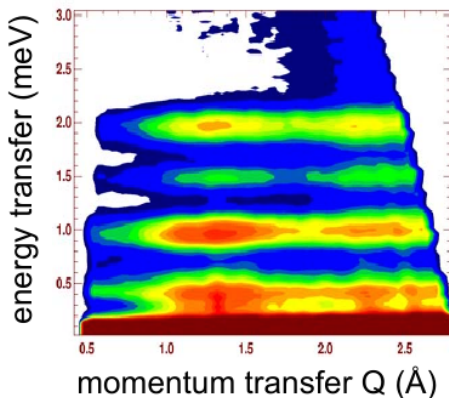
Local excitations: infinitely weak "springs"

Signature: flat dispersion

- ▶ Molecular magnets
- ▶ Crystal field excitations (Rare Earth)

CsFe₈

IN5



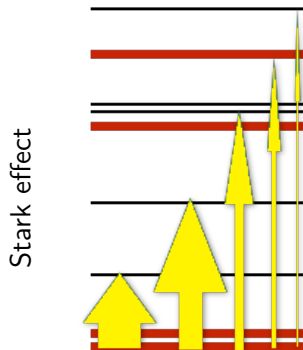
O. Waldmann, APS lecture 2006

Local transitions: Crystal Electric Field Splitting

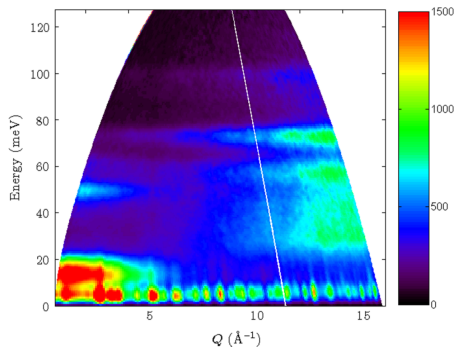
$\text{Tb}_2\text{Ti}_2\text{O}_7$

Tb^{3+} :

$${}^7F_6 \left\{ \begin{array}{l} S = 3 \\ L = 3 \end{array} \right\} J = 6$$



Merlin $E_i = 150\text{meV}$
powder, $T = 7\text{K}$



CF

phonons

A. J. Princep *et al.* PRB **91** 224430 (2015).

Collective dynamics

atoms/magnetic moments move "correlated" ("ballet")

Snapshot: periodic pattern – wave

Positions of the **nuclei**

Direction/Length of the **magnetic moment**

Local:

vibrational scattering
rattling modes

Local:

C(rystal)F(ield)-excitations
transitions in molecular magnets

**Propagating:
phonons**

**Propagating:
spin waves (magnons)**

triplons

spinons

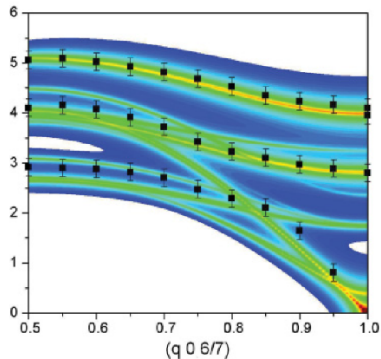
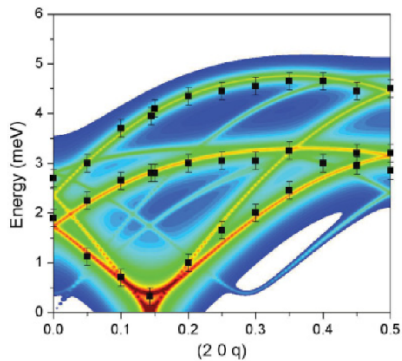
phasons

multi-magnon/-spinon states

[... and hybrid states ...]

Reality is not always so simple . . .

J. Jensen (2011) PRB 84, 104405



Quantitative info from intensities: Coherent dynamic scattering function

$$S_N(\mathbf{Q}, \omega) = \frac{1}{2\pi\hbar} \int d\mathbf{r} dt e^{i(\mathbf{Q}\mathbf{r} - \omega t)} \langle N(\mathbf{0}, 0) N(\mathbf{r}, t) \rangle_T$$

$$S_M(\mathbf{Q}, \omega) = \frac{(\gamma r_0)^2}{2\pi\hbar} \int d\mathbf{r} dt e^{i(\mathbf{Q}\mathbf{r} - \omega t)} \langle \mathbf{M}_\perp(\mathbf{0}, 0) \cdot \mathbf{M}_\perp(\mathbf{r}, t) \rangle_T$$

$S(\mathbf{Q}, \omega)$: space-time Fourier transform of the
nuclear-positional density-density pair correlation function
magnetic

- ▶ **quantitative** info from intensity
- ▶ phonon and magnetic scattering (often) well separated

Intensities - phonons

$$S_N(\mathbf{Q}, \omega) = \sum_{n_0} p(n_0) \frac{1}{2\pi\hbar} \int_{-\infty}^{\infty} dt e^{-i\omega t} \langle n_0 | N^*(\mathbf{Q}, 0) N(\mathbf{Q}, t) | n_0 \rangle$$

$$S_N^{1ph}(\mathbf{Q}, \omega) = \sum_{s=1}^{3r} |I_{N,s}(\mathbf{Q})|^2 [\langle n_s + 1 \rangle_T \delta(\omega - \omega_s) + \langle n_s \rangle_T \delta(\omega + \omega_s)]$$

$$\langle n_s + 1 \rangle_T = \frac{1}{1 - e^{-\frac{\hbar\omega_s}{k_B T}}}$$

$$\langle n_s \rangle_T = \frac{e^{-\frac{\hbar\omega_s}{k_B T}}}{1 - e^{-\frac{\hbar\omega_s}{k_B T}}}$$

Intensities - phonons

$$S_N(\mathbf{Q}, \omega) = \sum_{n_0} p(n_0) \frac{1}{2\pi\hbar} \int_{-\infty}^{\infty} dt e^{-i\omega t} \langle n_0 | N^*(\mathbf{Q}, 0) N(\mathbf{Q}, t) | n_0 \rangle$$

$$S_N^{1ph}(\mathbf{Q}, \omega) = \sum_{s=1}^{3r} |I_{N,s}(\mathbf{Q})|^2 [\langle n_s + 1 \rangle_T \delta(\omega - \omega_s) + \langle n_s \rangle_T \delta(\omega + \omega_s)]$$

$$|I_{N,s}(\mathbf{Q})|^2 = \frac{1}{\omega_s} \left| \sum_{j=1}^r \frac{\bar{b}_j}{\sqrt{M_j}} e^{-W_j} e^{i\mathbf{Q}d_j} \underbrace{(\mathbf{Q} \cdot \mathbf{e}_{js})}_{\text{increases with } Q^2} \right|^2$$

FT of points d_j
increases with Q^2

Intensity periodic if d_j special position e_{js} : amplitude atom j , phonon s

Intensities - magnons, $T \ll T_N$

$$S_M(\mathbf{Q}, \omega) = (\gamma r_0)^2 \sum_{n_0} p(n_0) \frac{1}{2\pi\hbar} \int_{-\infty}^{\infty} dt e^{-i\omega t} \langle n_0 | \mathbf{M}_{\perp}^*(\mathbf{Q}, 0) \mathbf{M}_{\perp}(\mathbf{Q}, t) | n_0 \rangle$$

$$S_M^{1m}(\mathbf{Q}, \omega) = \sum_{s=1}^r |I_{M,s}(\mathbf{Q})|^2 [\langle n_s + 1 \rangle_T \delta(\omega - \omega_s) + \langle n_s \rangle_T \delta(\omega + \omega_s)]$$

$$\langle n_s + 1 \rangle_T = \frac{1}{1 - e^{-\frac{\hbar\omega_s}{k_B T}}}$$

$$\langle n_s \rangle_T = \frac{e^{-\frac{\hbar\omega_s}{k_B T}}}{1 - e^{-\frac{\hbar\omega_s}{k_B T}}}$$

Intensities - magnons, $T \ll T_N$

$$S_M(\mathbf{Q}, \omega) = (\gamma r_0)^2 \sum_{n_0} p(n_0) \frac{1}{2\pi\hbar} \int_{-\infty}^{\infty} dt e^{-i\omega t} \langle n_0 | \mathbf{M}_{\perp}^*(\mathbf{Q}, 0) \mathbf{M}_{\perp}(\mathbf{Q}, t) | n_0 \rangle$$

$$S_M^{1m}(\mathbf{Q}, \omega) = \sum_{s=1}^r |I_{M,s}(\mathbf{Q})|^2 [\langle n_s + 1 \rangle_T \delta(\omega - \omega_s) + \langle n_s \rangle_T \delta(\omega + \omega_s)]$$

$$|I_{M,s}(\mathbf{Q})|^2 = (\gamma r_0)^2 \left| \sum_{j=1}^r \underbrace{f_j(\mathbf{Q})}_{\text{form factor}} e^{-W_j} e^{i\mathbf{Q}\mathbf{d}_j} \underbrace{e_{\perp,j,s}}_{\text{mag. amp. ion } j, \text{ magnon } s} \right|^2$$

Intensity periodic if \mathbf{d}_j special position

Magnon intensities

... often essential to assign a spin wave branch to a peak !

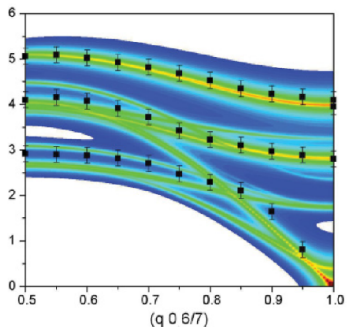
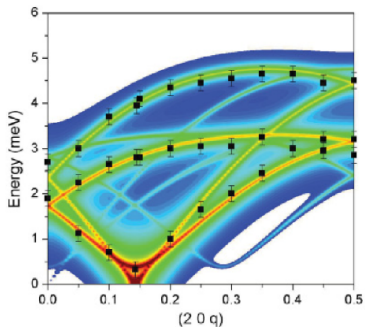
Long-range ordered structures

length of ordered moment identical at equivalent sites

transverse excitations

"Classical" Spin Wave Theory

J. Jensen (2011) PRB 84, 104405



Magnetic excitations: more than spin waves

So far:

Ground state: periodically ordered atoms or magnetic moments

Collective excitations:

phonons small oscillations around the structural order
spin waves magnetic

Now:

periodically ordered magnetic sites with a local magnetic moment

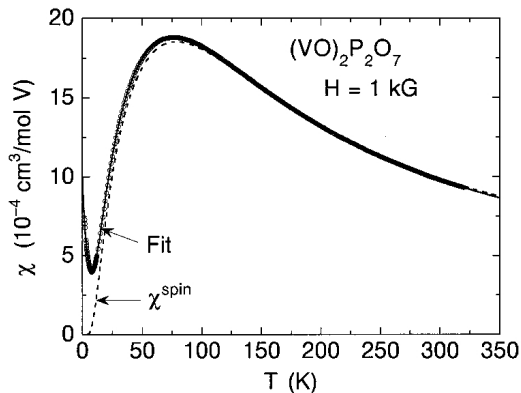
interaction between the spins (e.g. visible in $\chi(T)$)

no long-range ordered magnetic moment

Collective excitations ?

Collective phenomena without magnetic long-range order

χ displays interactions – but no phase transition



Two spins $\frac{1}{2}$ and an antiferromagnetic spring

$S = \frac{1}{2}$ at each site

strong antiferromagnetic

no

coupling between

coupling between

next-neighbours

pairs



Dimer: Pair spin 0

$$\frac{1}{\sqrt{2}} [|\uparrow\downarrow\rangle - |\downarrow\uparrow\rangle]$$

Local singlet-triplet excitations

$S = \frac{1}{2}$ at each site

strong antiferromagnetic

no

coupling between

coupling between

next-neighbours

pairs



Triplon: Pair spin 1

$$\left\{ \frac{1}{\sqrt{2}} \left[\begin{array}{c} | \uparrow \uparrow \rangle \\ | \uparrow \downarrow \rangle + | \downarrow \uparrow \rangle \\ | \downarrow \downarrow \rangle \end{array} \right] \right\}$$

Triplons – Signature Zeeman splitting

$S = \frac{1}{2}$ at each site

strong antiferromagnetic

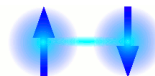
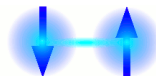
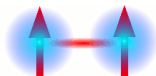
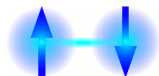
coupling between

next-neighbours

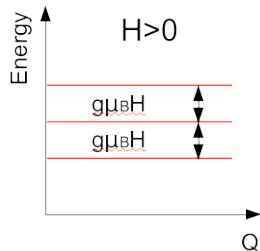
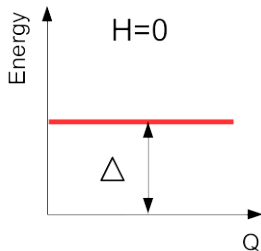
no

coupling between

pairs



$$\frac{1}{\sqrt{2}} \left[\begin{array}{c} |\uparrow\uparrow\rangle \\ |\uparrow\downarrow\rangle + |\downarrow\uparrow\rangle \\ |\downarrow\downarrow\rangle \end{array} \right]$$



Triplons – Signature Zeeman splitting

$$S = \frac{1}{2} \text{ at each site}$$

strong antiferromagnetic

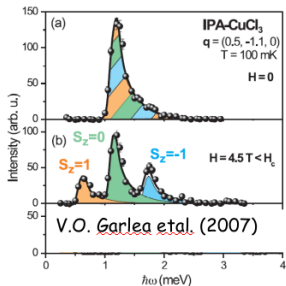
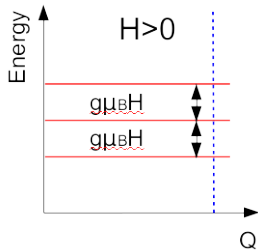
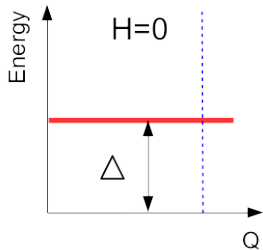
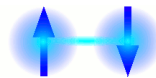
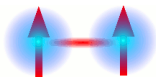
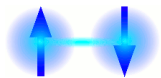
coupling between

next-neighbours

no

coupling between

pairs



Non-Interacting triplons – intensity signature

$$S = \frac{1}{2} \text{ at each site}$$

strong antiferromagnetic

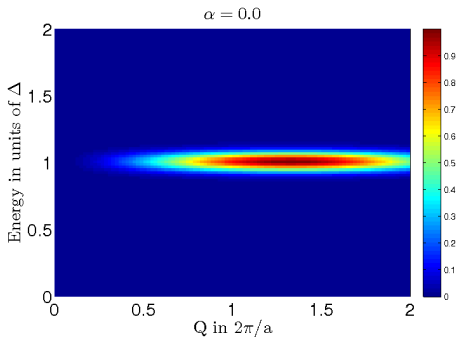
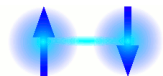
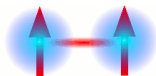
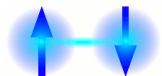
no

coupling between

coupling between

next-neighbours

pairs



Interacting triplons – propagation – dispersion

$$S = \frac{1}{2} \text{ at each site}$$

strong antiferromagnetic

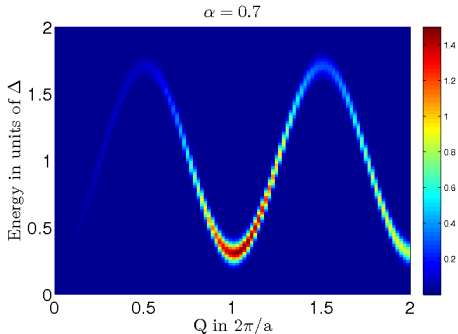
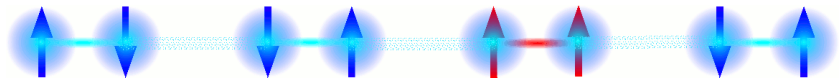
increasing

coupling between

coupling between

next-neighbours

pairs



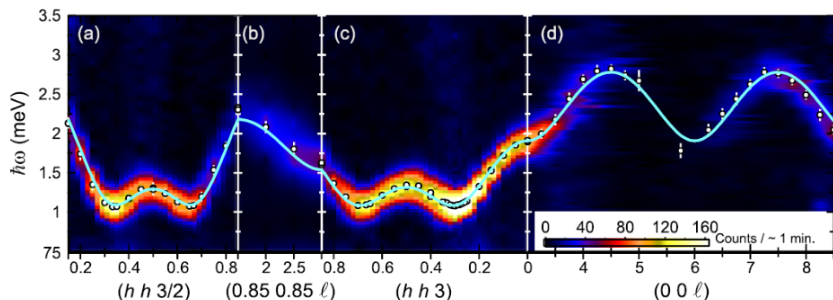
Interacting triplons – propagation – dispersion

$$S = \frac{1}{2} \text{ at each site}$$

strong antiferromagnetic
increasing

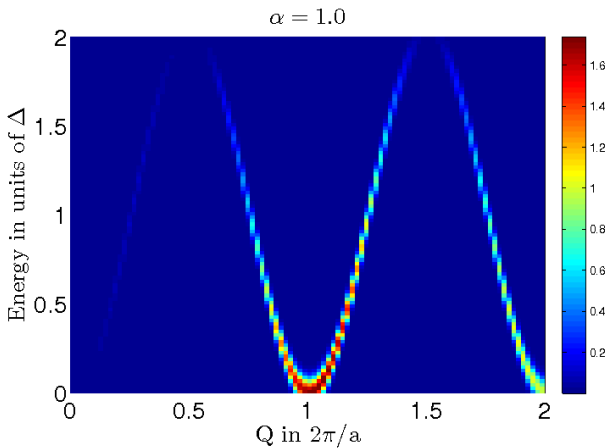
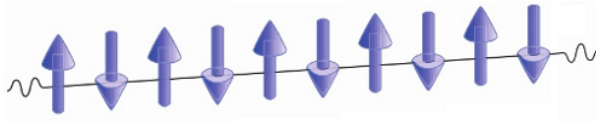
coupling between
coupling between

next-neighbours
pairs

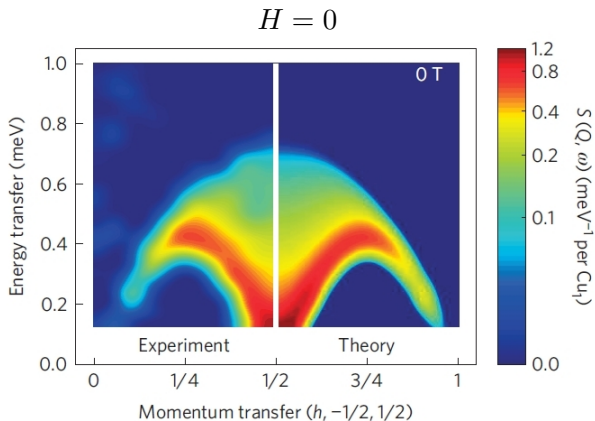


M.B. Stone *et al.* PRL **100** 237201 (2008)

1D array – Limit of uniform coupling between $S = \frac{1}{2}$



1D array – Limit of uniform coupling between $S = \frac{1}{2}$



M. Mourigal, M.E. *et al.* Nat.Phys. **9** 435 (2013)

Weakly coupled dimer array

Ground state



Triplon



Stronger coupled dimer array

Ground state



Triplon

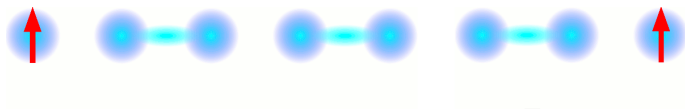


Stronger coupled dimer array

Ground state



Triplon



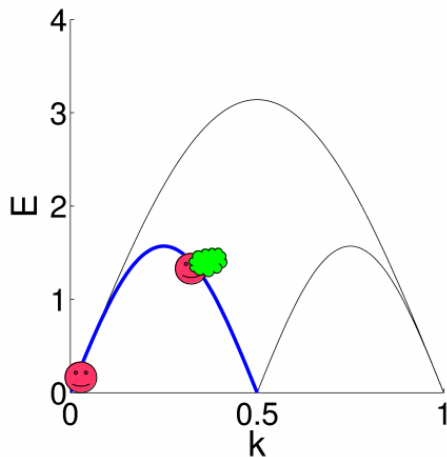
1D $S = \frac{1}{2}$ dimer array – Limit of uniform coupling



freely propagating spin $\frac{1}{2}$ particles: spinons

Two-particle excitation: Signature continuous scattering

Neutron excites **pairs** of **freely propagating spin $\frac{1}{2}$** particles



1-particle dispersion

 $E(k)$

neutron excites pair

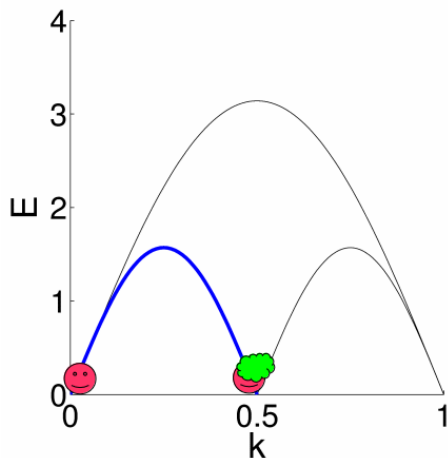
 =  + 

$Q = k_1 + k_2$

$E = E(k_1) + E(k_2)$

Two-particle excitation: Signature continuous scattering

Neutron excites **pairs** of **freely propagating spin $\frac{1}{2}$** particles



1-particle dispersion



$E(k)$

neutron excites pair



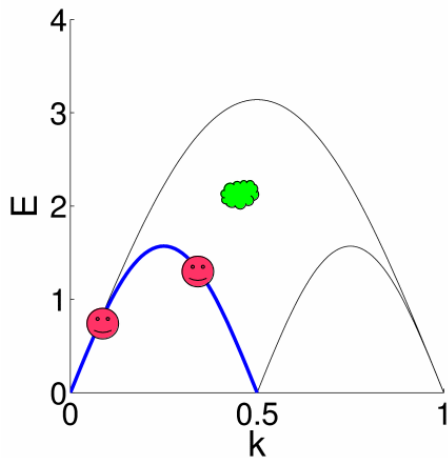
=  + 

$$Q = k_1 + k_2$$

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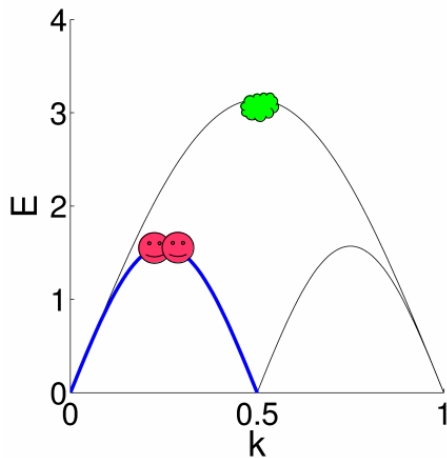
 =  + 

$Q = k_1 + k_2$

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Two-particle excitation: Signature continuous scattering

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1-particle dispersion

 $E(k)$

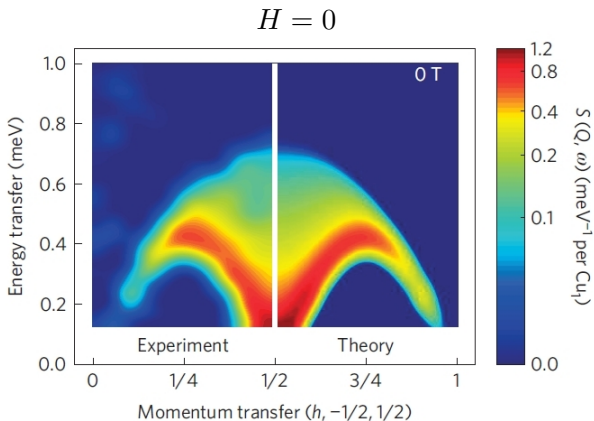
neutron excites pair

 =  + 

$Q = k_1 + k_2$

$E = E(k_1) + E(k_2)$

Spinon continuum in $\text{CuSO}_4 \cdot 5\text{D}_2\text{O}$

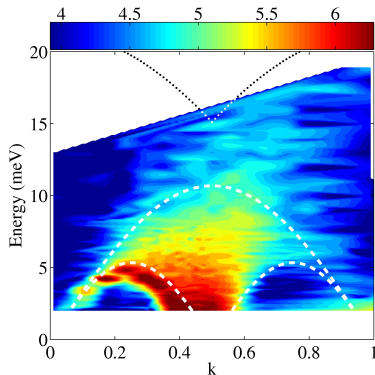


M. Mourigal, M.E. *et al.* Nat.Phys. **9** 435 (2013)

New many-particle states and excitations

2 zig-zag coupled 1D spin $\frac{1}{2}$ arrays

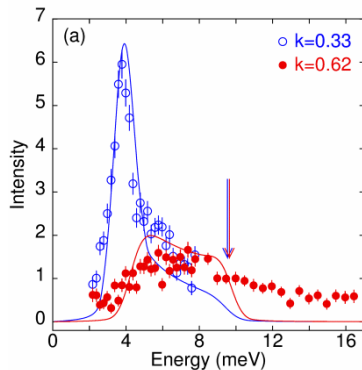
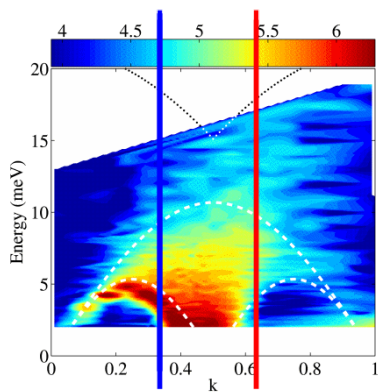
Continuum:
pairs of free particles
discrete branch:
bound particle-pairs



M.E. *et al.* PRL **104** 237207 (2010)

New many-particle states and excitations

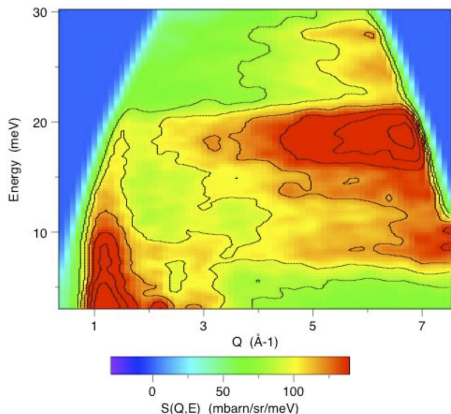
2 zig-zag coupled 1D spin $\frac{1}{2}$ arrays



M.E. *et al.* PRL **104** 237207 (2010)

Collective excitations – powder samples

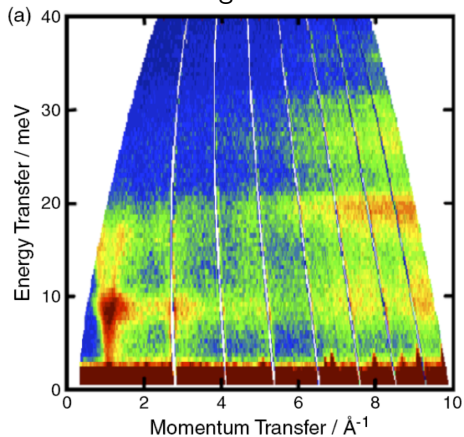
Continuum



B. Fåk *et al.* EPL **81** 17006 (2008)

Deuterium jarosite

magnons

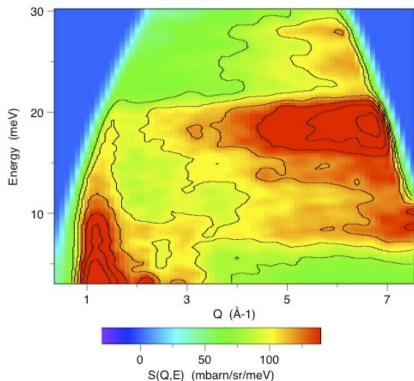


F. Coomer *et al.* JPCM **18** 8847 (2006)

K-jarosite

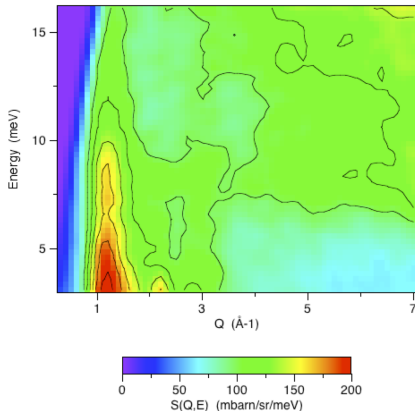
Collective excitations – powder samples

IN5: deuterium jarosite powder



magnetic only

Hydronium iron jarosite, T=15 K

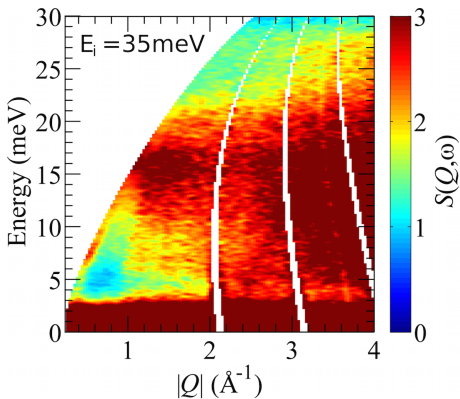


B. Fåk *et al.* EPL **81** 17006 (2008)

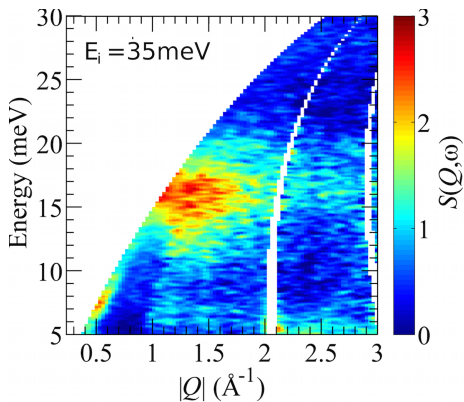
Malachite Inelastic neutron scattering on deuterated powder

MARI/ISIS

all data

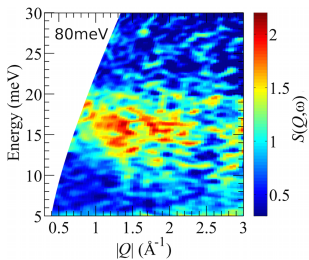


magnetic part

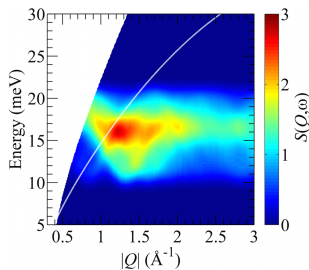


Extracting information from powder samples: Triplons

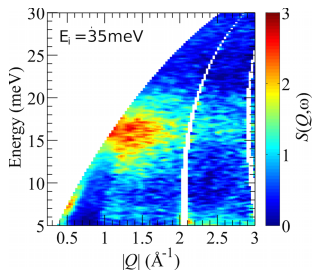
magnetic $E_i = 35\text{meV}$



model



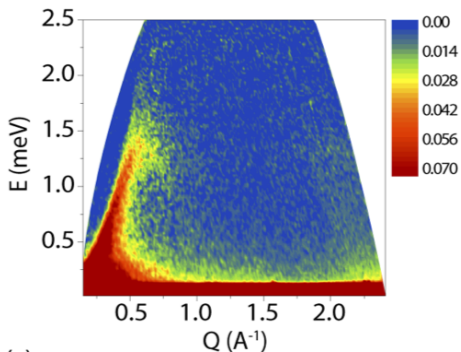
magnetic $E_i = 80\text{meV}$



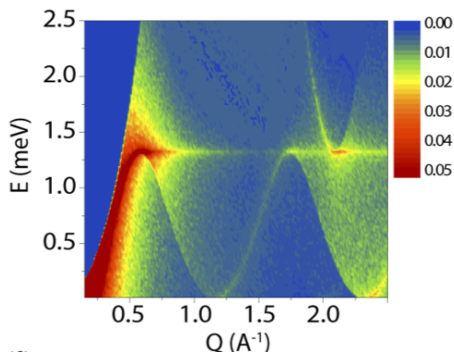
Collective excitations – powder samples: magnons

Extracting information from powder samples: Spinwaves/Magnons

IN5 Haydeite



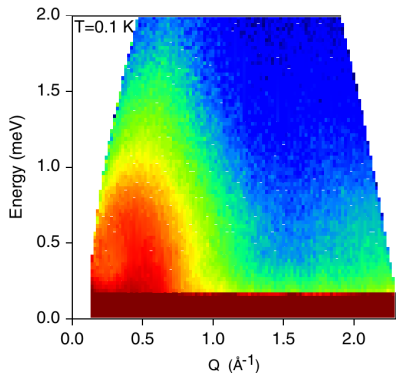
Spin wave theory



D. Boldrin, B. Fåk, M.E., *et al.* PRB **91** 220408 (2015)

Collective excitations – powder samples

Continuum

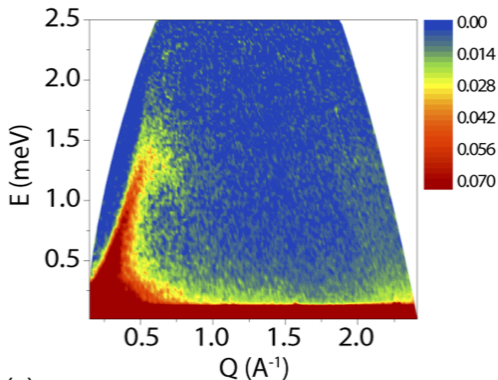


B. Fåk *et al.*

PRL **109** 037208 (2012)

IN5 Kapellasite

Magnons



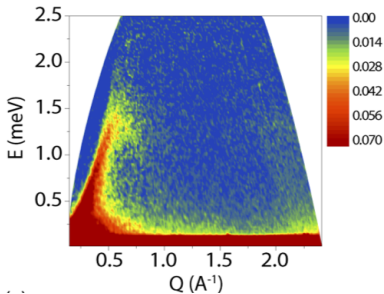
D. Boldrin, B. Fåk, M.E. *et al.*

PRB **91** 220408 (2015)

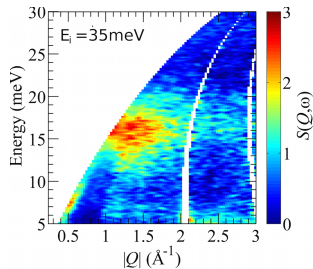
IN5 Haydeite

Collective excitations – powder samples

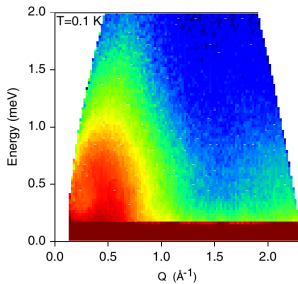
Magnons



Triplons

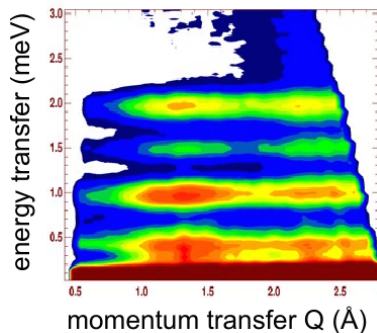


Continuum

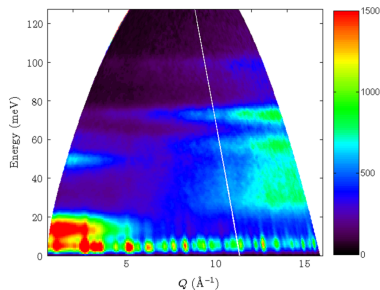


Collective excitations – powder samples

local excitations
(molecule-spin states)



local (Crystal field)
and phonons



Correlated Excitations – How do we measure them ?

- ▶ powder on TOF – valuable info
- ▶ single crystal TOF – large overview of Q-E-space
- ▶ Questions at specific Q/H,p,T: TAS
- ▶ Small single crystal: TAS
- ▶ inelastic polarized: TAS (today !)